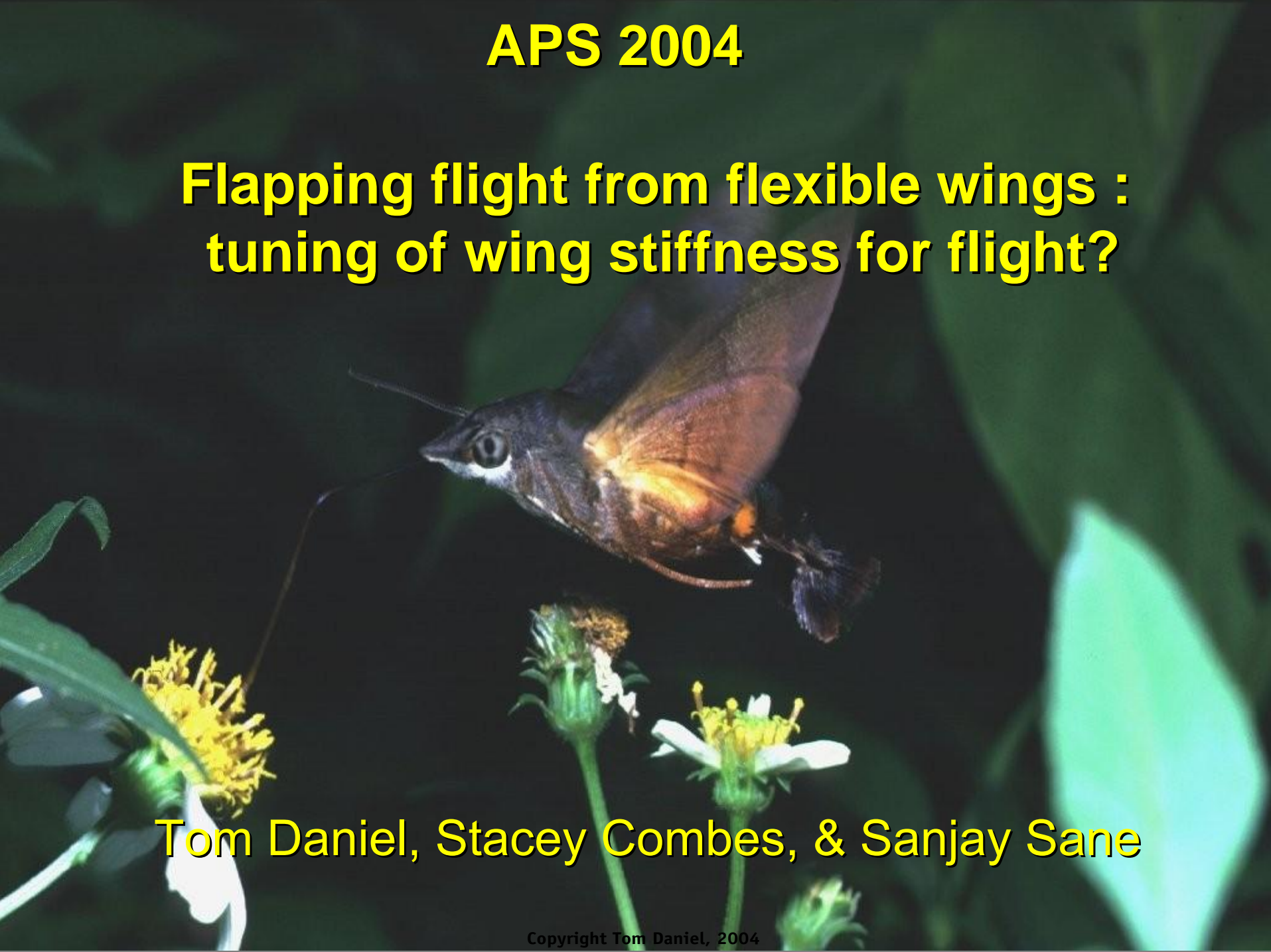
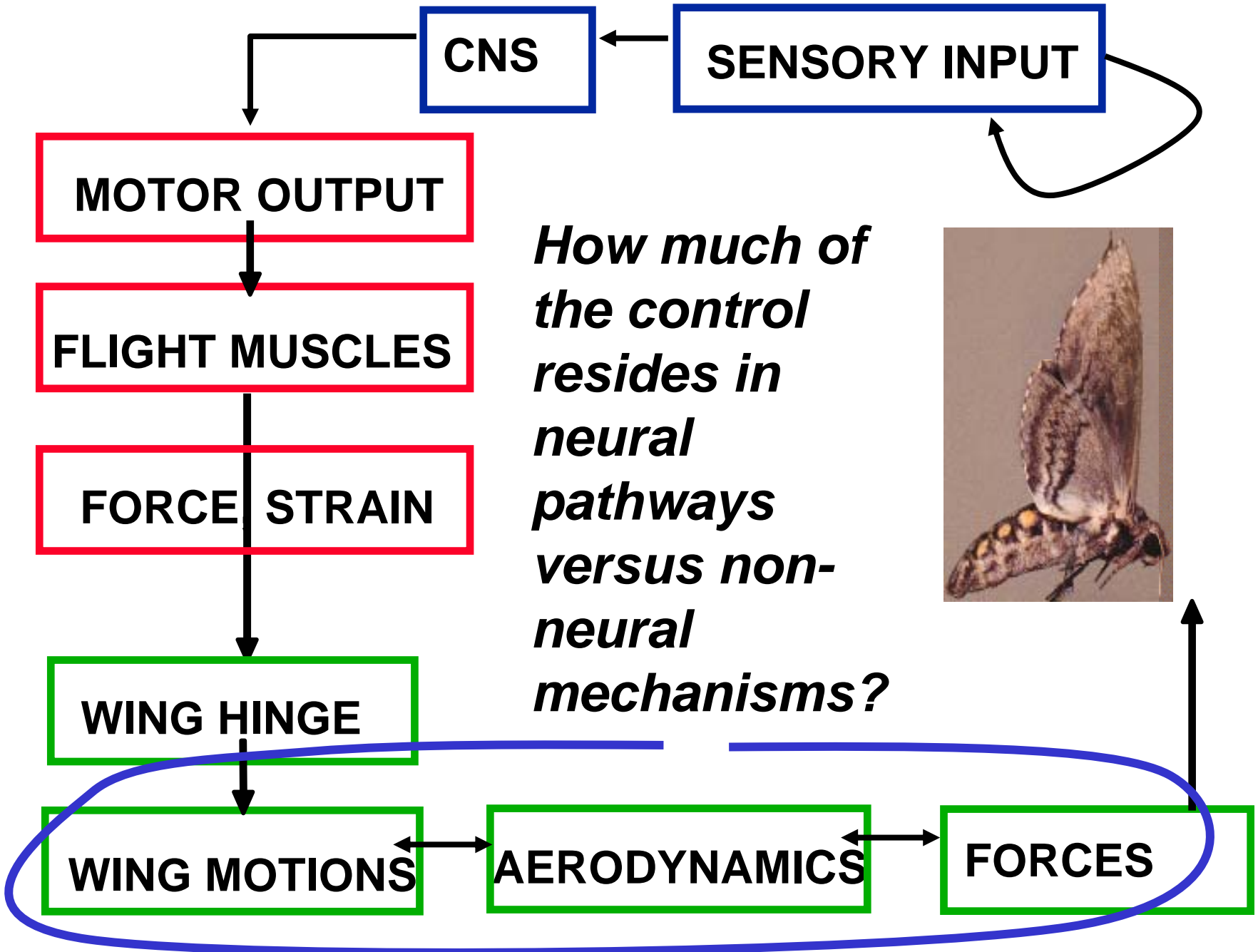


APS 2004

**Flapping flight from flexible wings :
tuning of wing stiffness for flight?**



Tom Daniel, Stacey Combes, & Sanjay Sane



A summary of insect flight issues

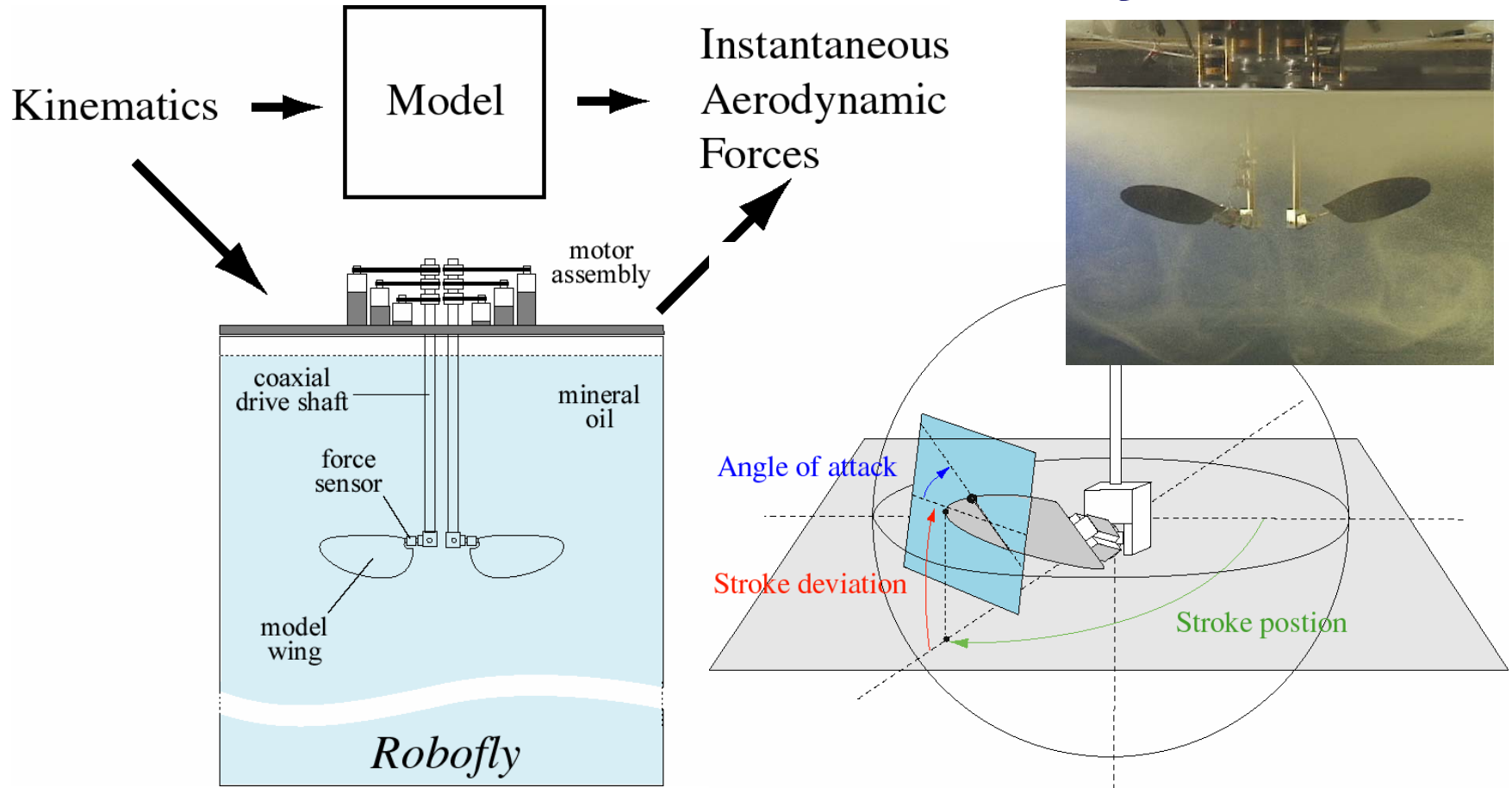
A thought experiment about wing or fin inertia

The coupled problem of fluid-solid interactions

Under what conditions can we ignore such interactions in air?

When we can ignore them, how might we proceed to analyze flight with compliant wings?

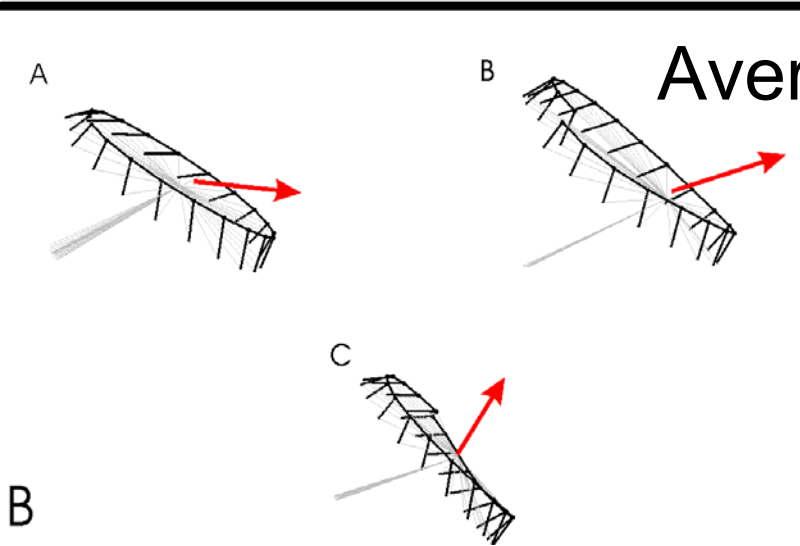
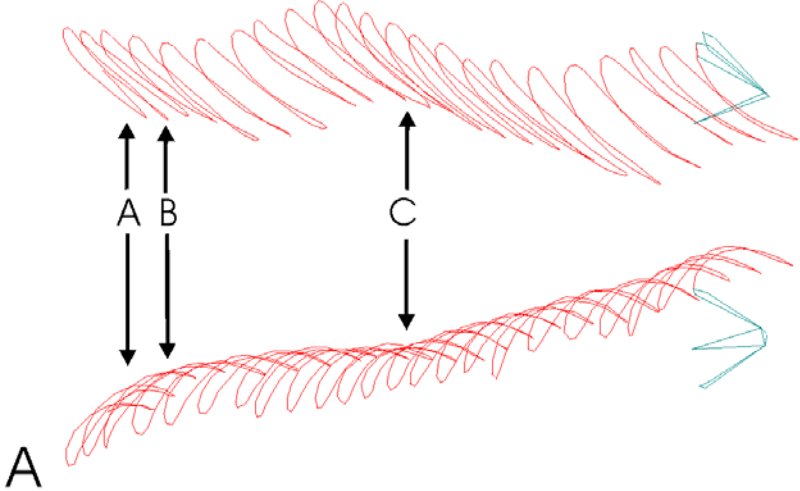
Dickinson's "Robo-fly"*



- Dynamical scaling: Reynolds number and reduced frequency parameter conserved
- Motors allow any arbitrary 3-D kinematic pattern
- Force sensors measure instantaneous forces on the wing

* Sanjay Sane, UW; Mark Willis, CWRU

Trajectory of forward flight and net aerodynamics forces measured by Robofly



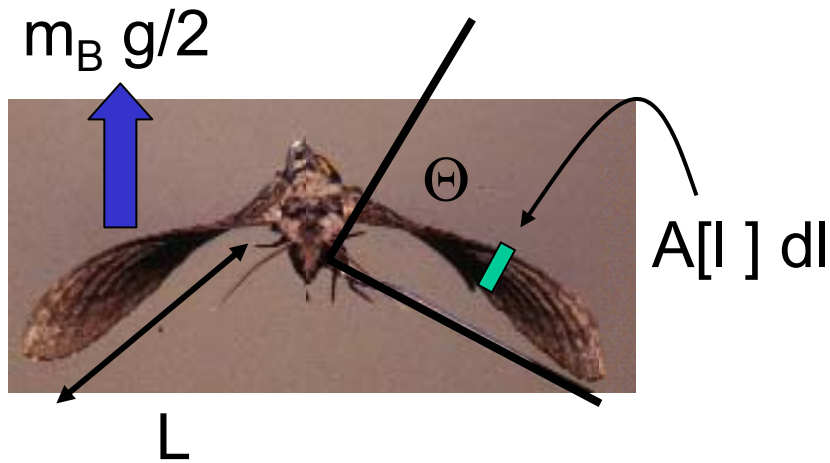
Average forces $\sim mg$



Such physical models work well for wings whose flexion is rather minimal. It is difficult to scale elastic and fluid dynamic stresses simultaneously

Many wings flex significantly





Scale question:
How large are the aerodynamic moments relative to inertial/elastic moments?

$$M_{AERO} \sim m_B g L/4$$

$$M_{INERT} \sim \rho_{app} \int l^2 \Theta \omega^2 \sin(\omega t) A[l] dl$$

$$\sim m_{app} L^2 \Theta \omega^2 / 3$$

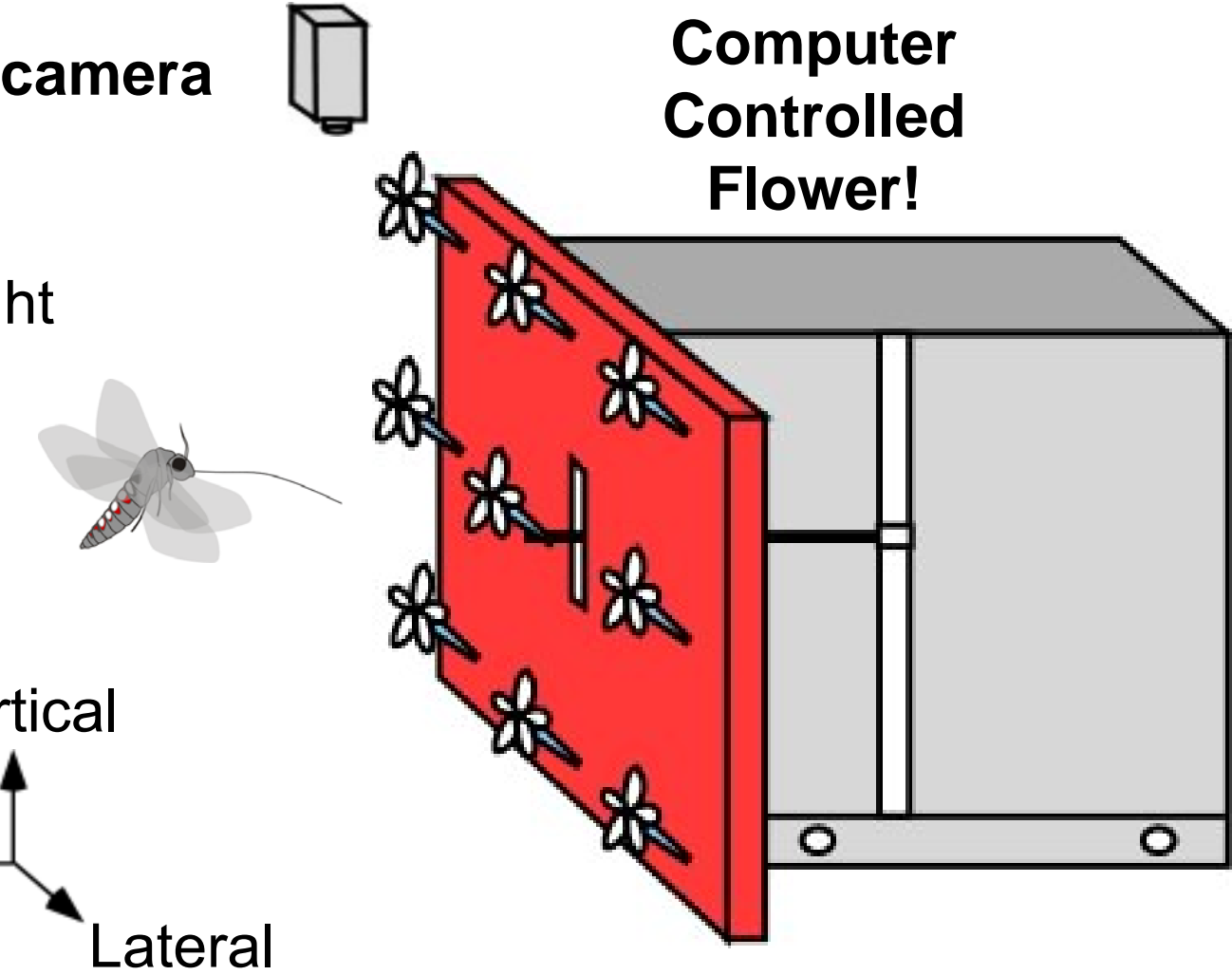
$$M_{RAT} = M_{INERT} / M_{AERO} \sim 5.0 \text{ Manduca}$$

$$\sim (m_{app}/m_B) L \Theta \omega^2 / g \sim 50.0 \text{ Drosophila}$$

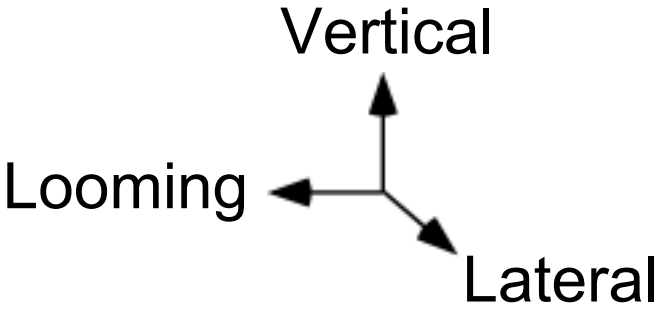
See as well Ennos '89, Zanker and Götz '90

Need high-speed videography of flapping wings during maneuvers.

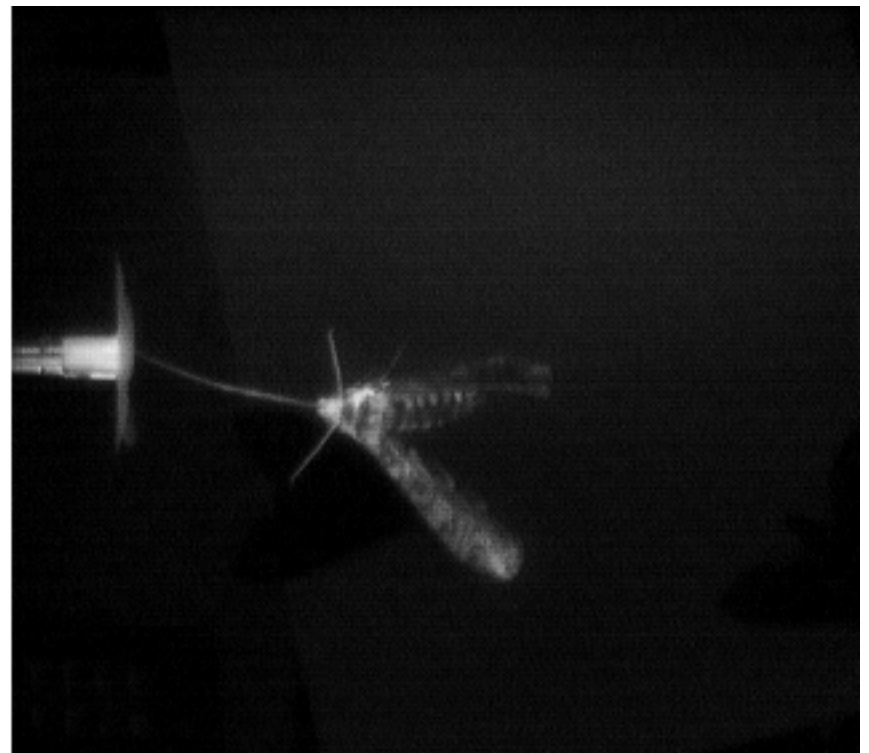
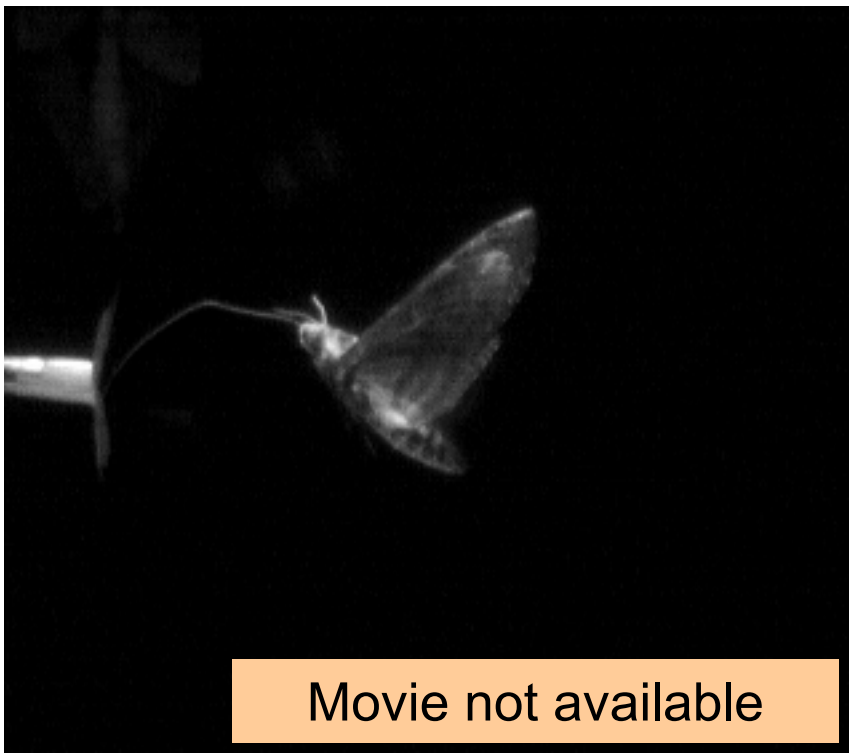
“Robo-Bush”



unfettered flight



Carlos Moreno

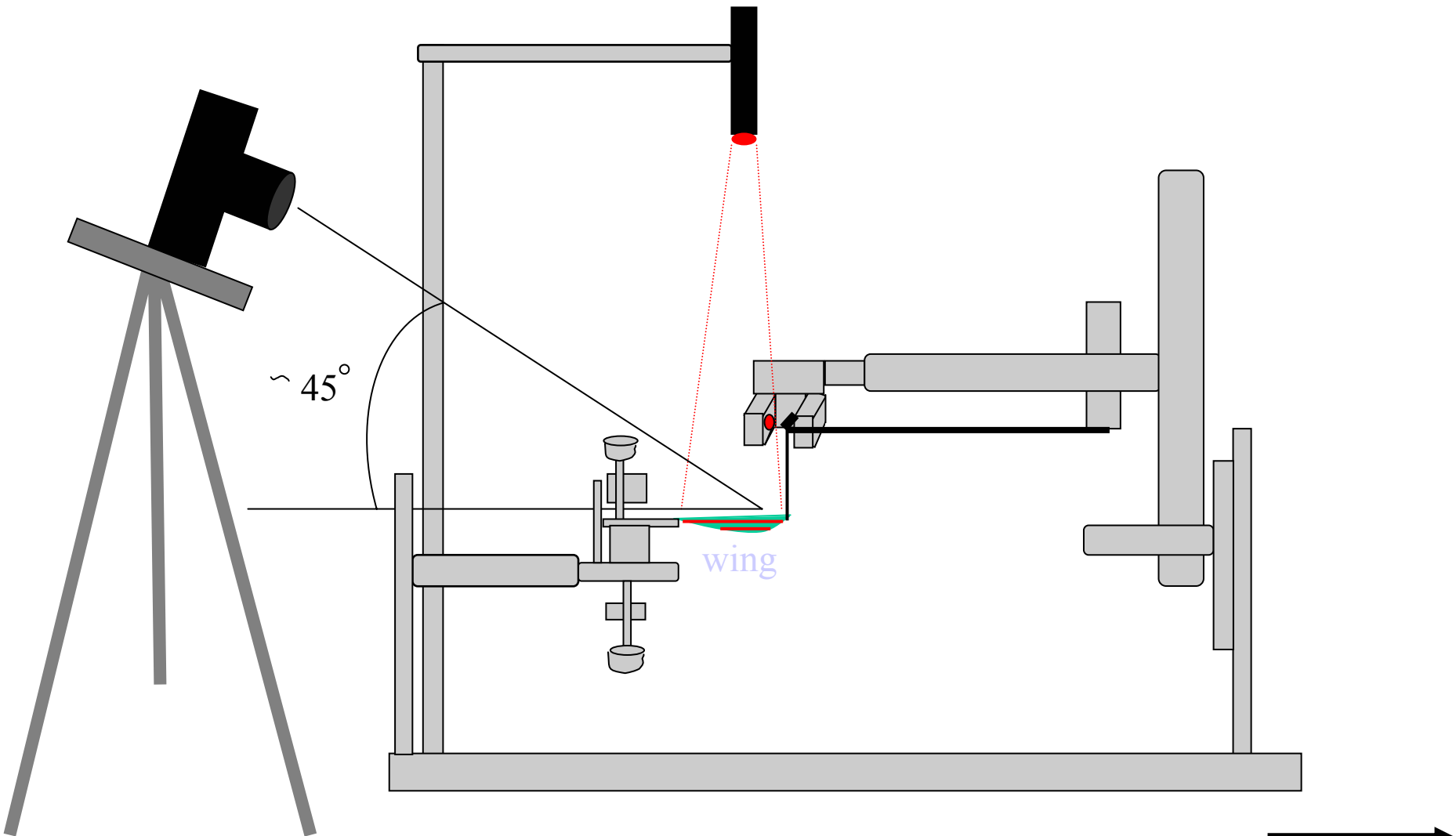


- To what extent are these motions determined by fluid dynamic events?
- What are the mechanical properties of these wings?

Michael Tu and Katarzyna Kodizczewska

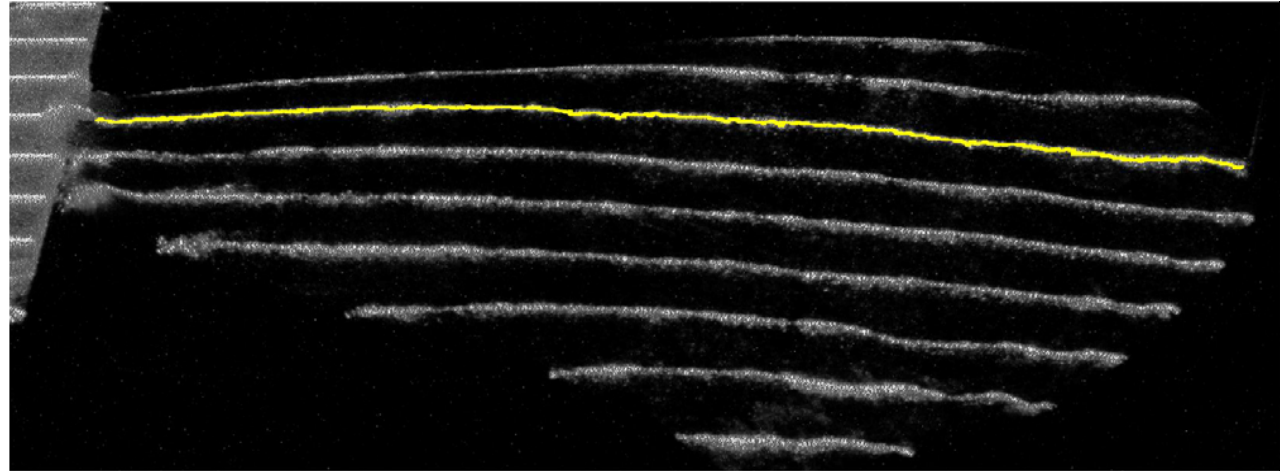
Copyright Tom Daniel, 2004

Measuring displacement continuously along a wing

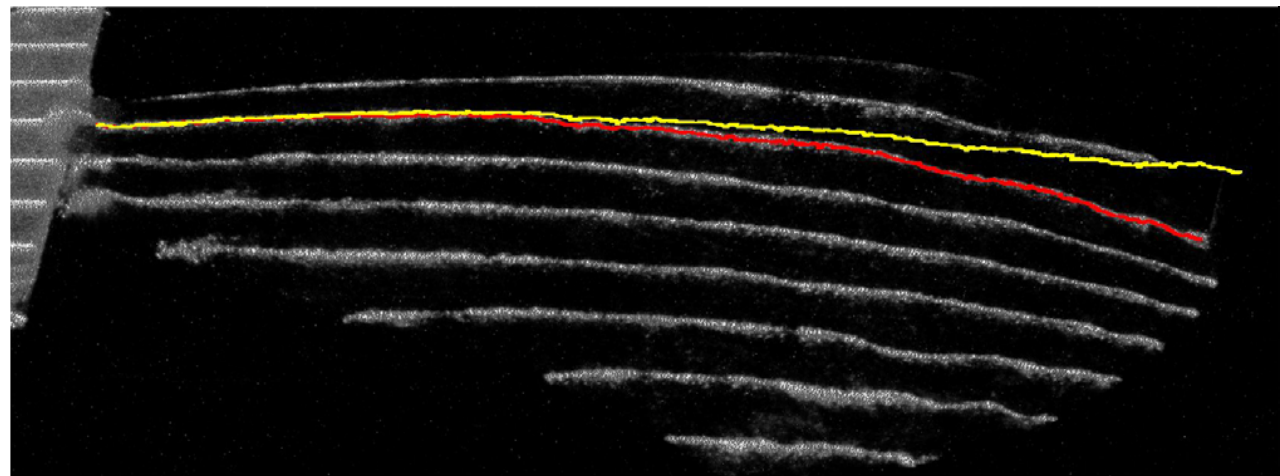


Changes in the y-direction of the picture correspond to bending in the z-direction of the wing

unloaded
wing

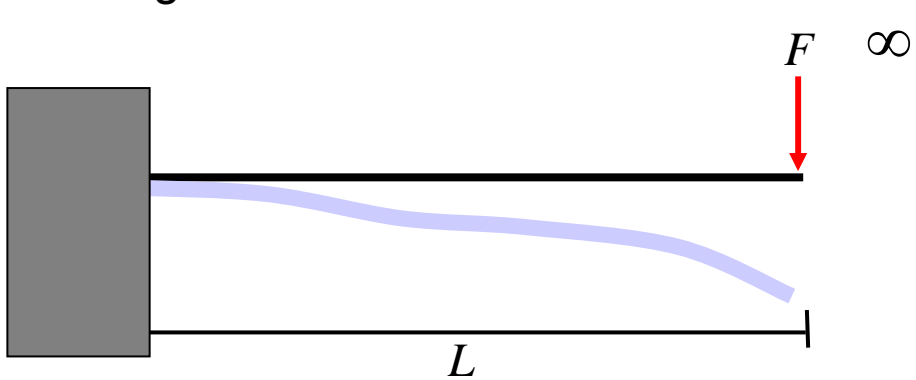


loaded
wing

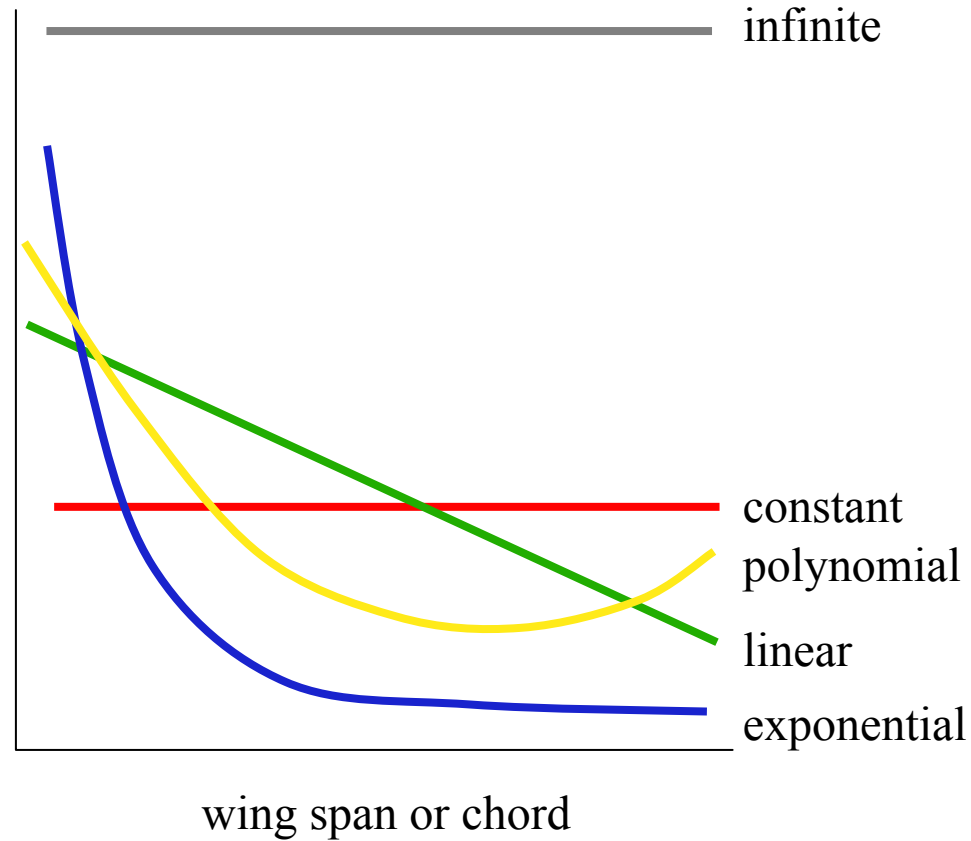
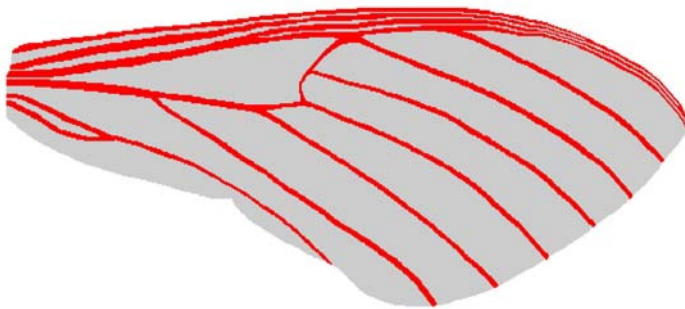


Possible patterns of spatial variation in wing stiffness

heterogeneous beam



wing
stiffness

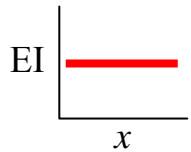
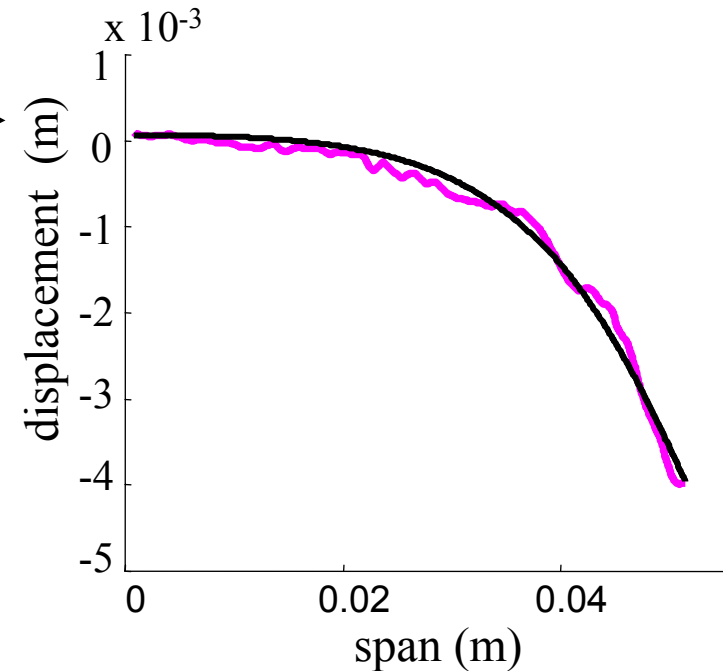


Solve for the EI distribution that best fits the measured wing displacement

$$EI(x) = \frac{F(L-x)}{d^2\delta/dx^2}$$

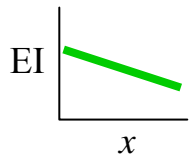
$$\delta(x) = \iint \frac{F(L-x)}{EI(x)} d^2x$$

simplex minimization



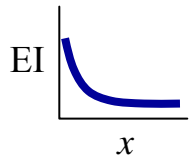
constant

$$[EI(x) = k]$$



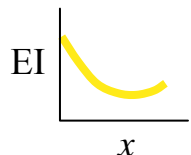
linear

$$[EI(x) = m x + b]$$



exponential

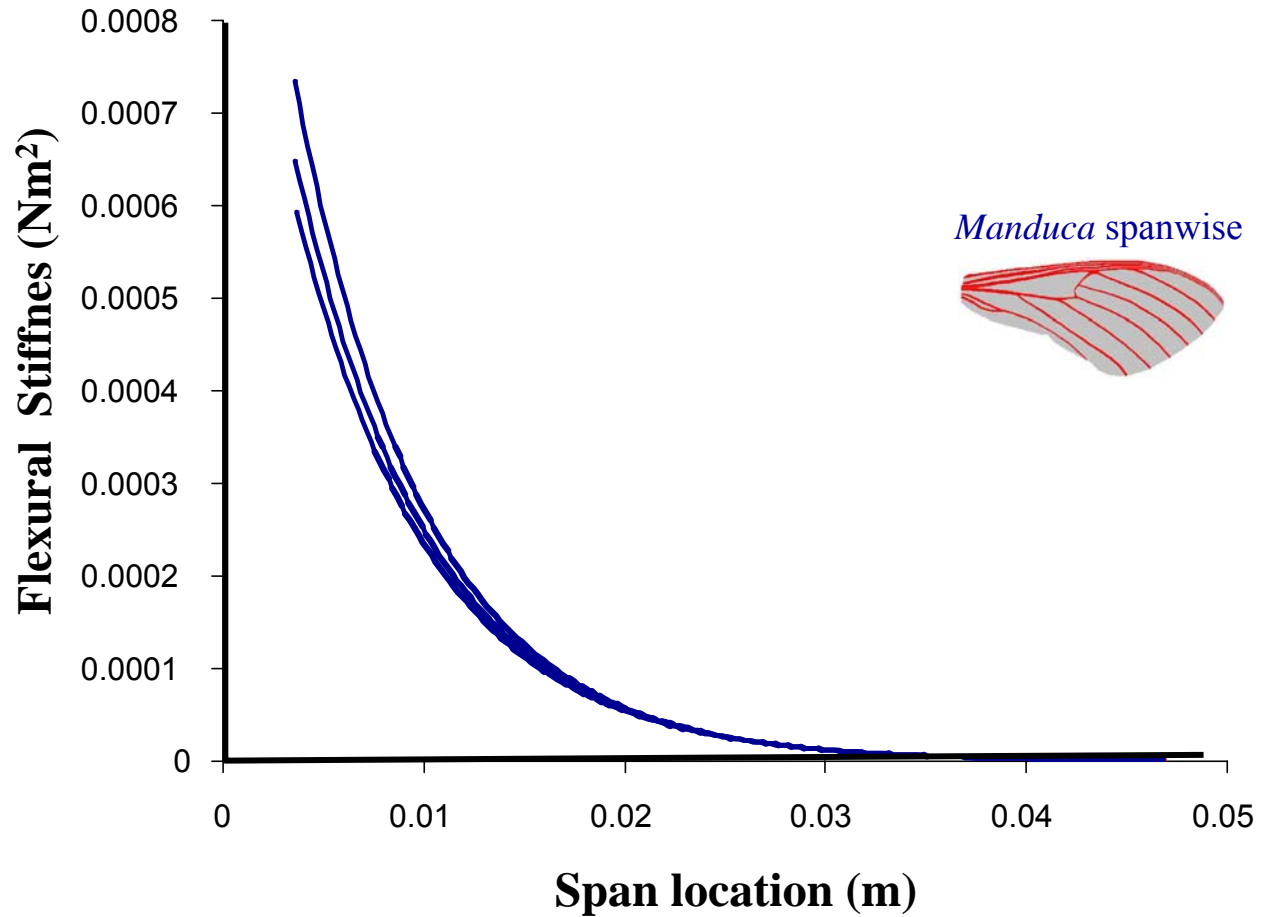
$$[EI(x) = c * \exp^{ax}]$$




polynomial

$$[EI(x) = px^2 + qx + r]$$

Spanwise wing stiffness flexural stiffness declines exponentially in span and chord directions



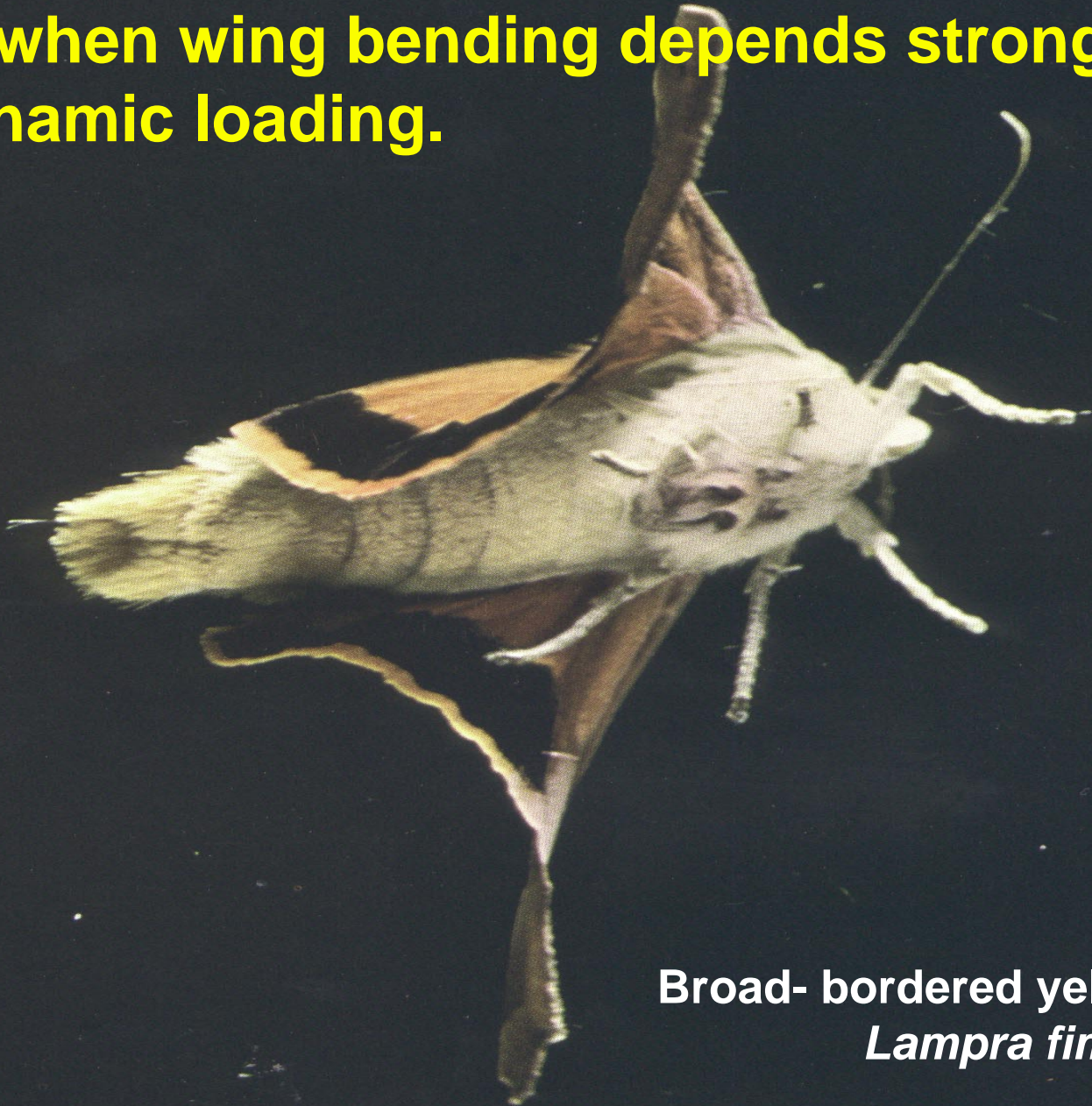


**Wings flex.
With measured
mechanical, geometric,
and kinematic
characters...**

.... use FEM to compute motions. From that compute aerodynamic forces

Movie not available

Aerodynamic force calculations from FEM are illegal when wing bending depends strongly on aerodynamic loading.



Broad- bordered yellow Underwing
Lampra fimbriata

(Dalton, 1975)

The basic aeroelastic problem

Shape
(curvature,
angle of
attack)
determines
the pressure
distribution.

Flexible wings
deform when
moved
dynamically.



Pressure
stresses
deform
flexible wings.

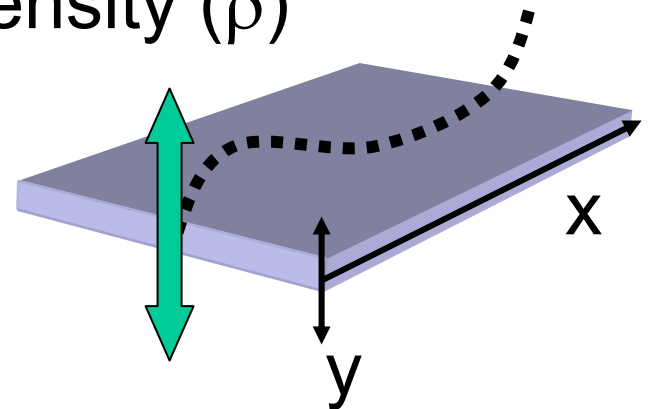
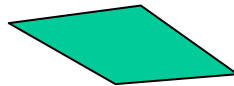
A scale argument for a thin flexing wing

Movie not available

A scale argument for a thin flexing wing

Impel with
Stiffness (E)
thickness (t)
width (w)
 EI (flexural stiffness)
density (ρ)

Movie not available



Impel with
 $A \sin(\omega t)$

What deformations -- $y(x,t)$ arise?

What bending moments follow from this $y(x,t)$?

A different tact :

Solve this wave equation
 $\frac{\partial^2 y}{\partial t^2} = -\left(\frac{EI}{\rho A}\right) \frac{\partial^4 y}{\partial x^4}$
with the right boundary
conditions

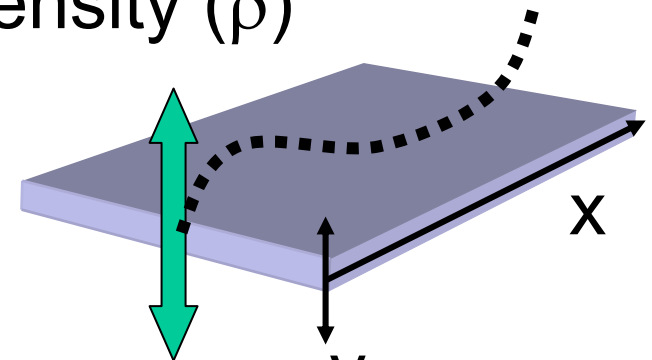


$$y(x,t)$$



$$\text{Moment} = EI \frac{\partial^2 y}{\partial x^2}$$

Imbue with
Stiffness (E)
thickness (t)
width (w)
EI (flexural stiffness)
density (ρ)



Impel with
 $A \sin(\omega t)$

What deformations -- $y(x,t)$ arise?

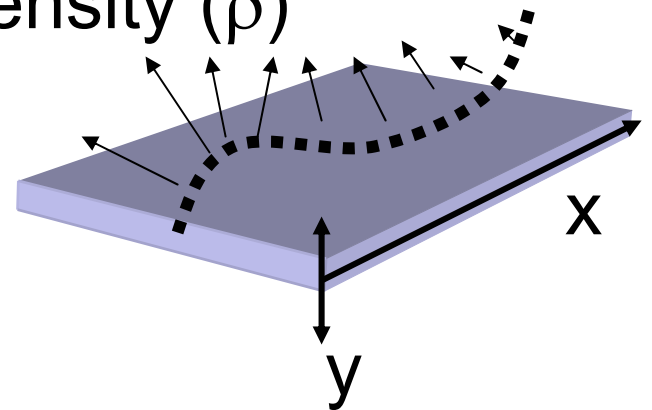
What bending moments follow from this $y(x,t)$?

A different tact :

Imbue with
Stiffness (E)
thickness (t)
width (w)
 EI (flexural stiffness)
density (ρ)

Inviscid blade-element
analysis (from Wu, 1971)

$$y(x,t)$$



$$p(x,t)$$

$$\rightarrow M_{\text{fluid}}(x,t)$$

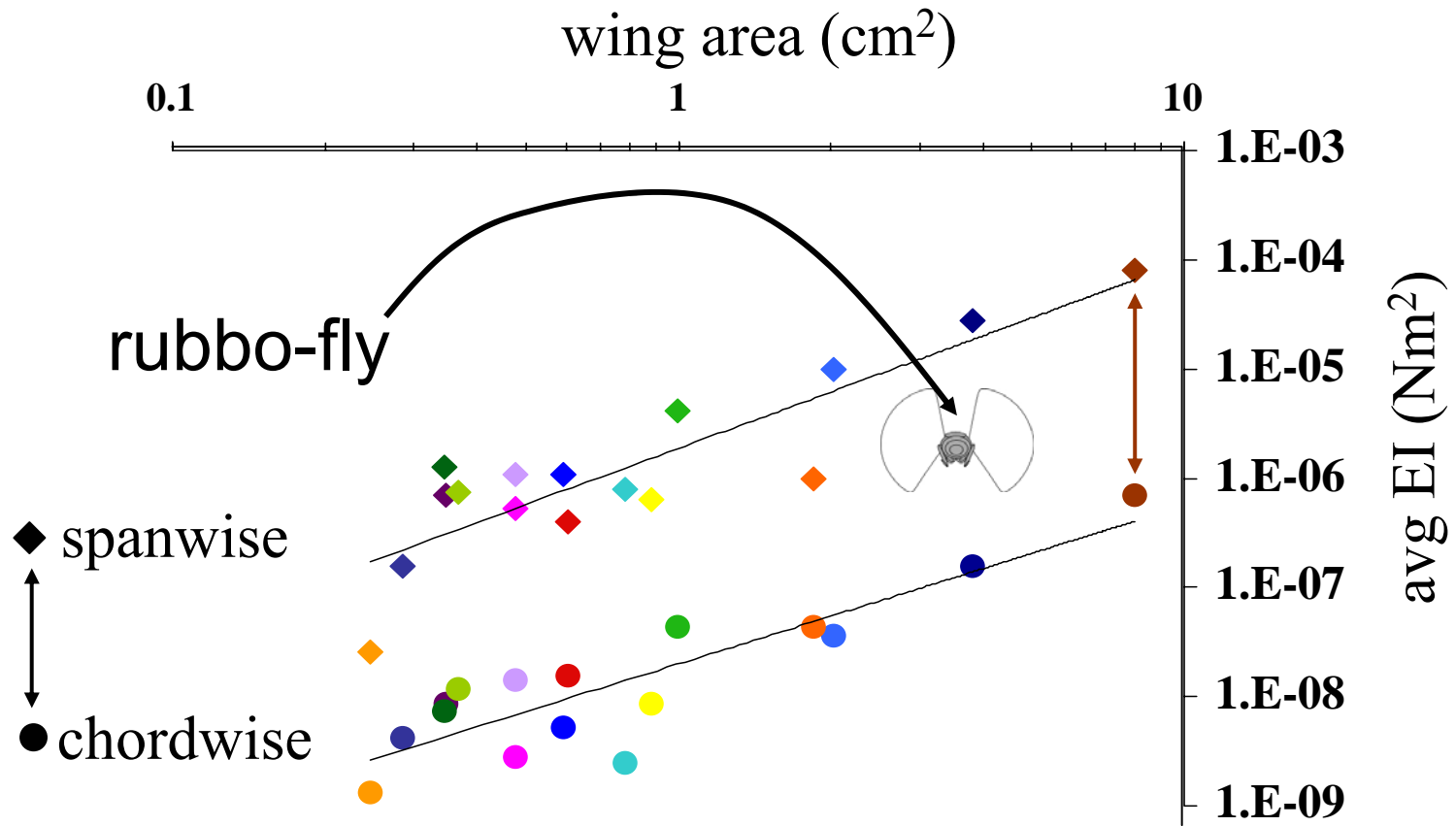
$$\rightarrow \iint M_{\text{fluid}}(x,t)$$

$$\rightarrow M_{\text{fluid}}$$

$$M_{\text{elastic}}$$

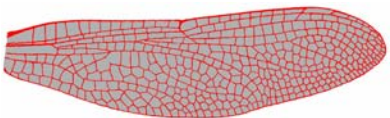
Manduca : $L = 0.03, w = 0.01, \omega = 2 \pi 25$
Wu 1971 set this up

Flexural stiffness data of Combes



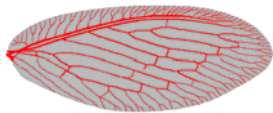
Odonates

- ◆ dragonfly
- ◆ perching dragonfly
- ◆ damselfly
- ◆ blue damselfly



Isopt/Neuropt

- ◆ termite
- ◆ lacewing



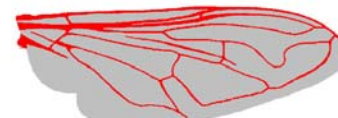
Lepidopterans

- ◆ Manduca
- ◆ cabbage white
- ◆ skipper



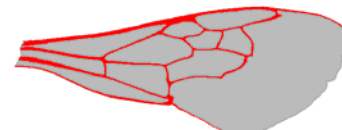
Dipterans

- ◆ cranefly
- ◆ calliphora
- ◆ syrphid
- ◆ bombyliid



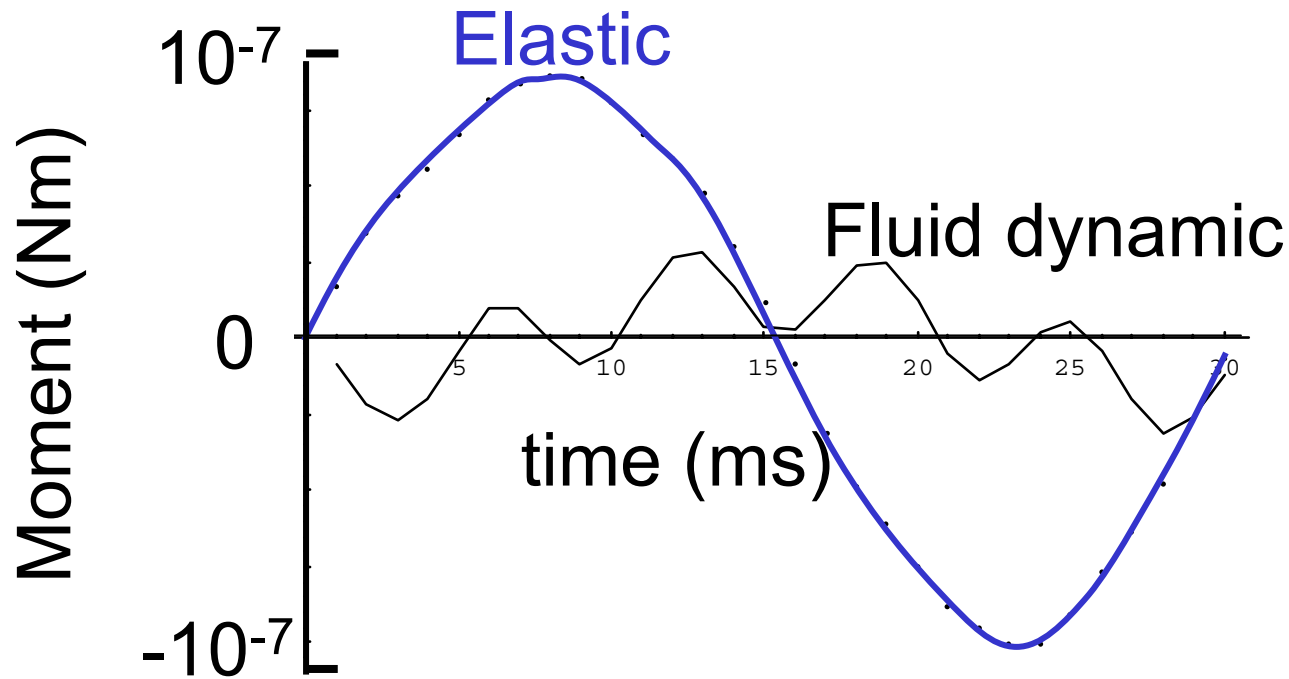
Hymenopterans

- ◆ bumblebee
- ◆ wasp
- ◆ spiderwasp



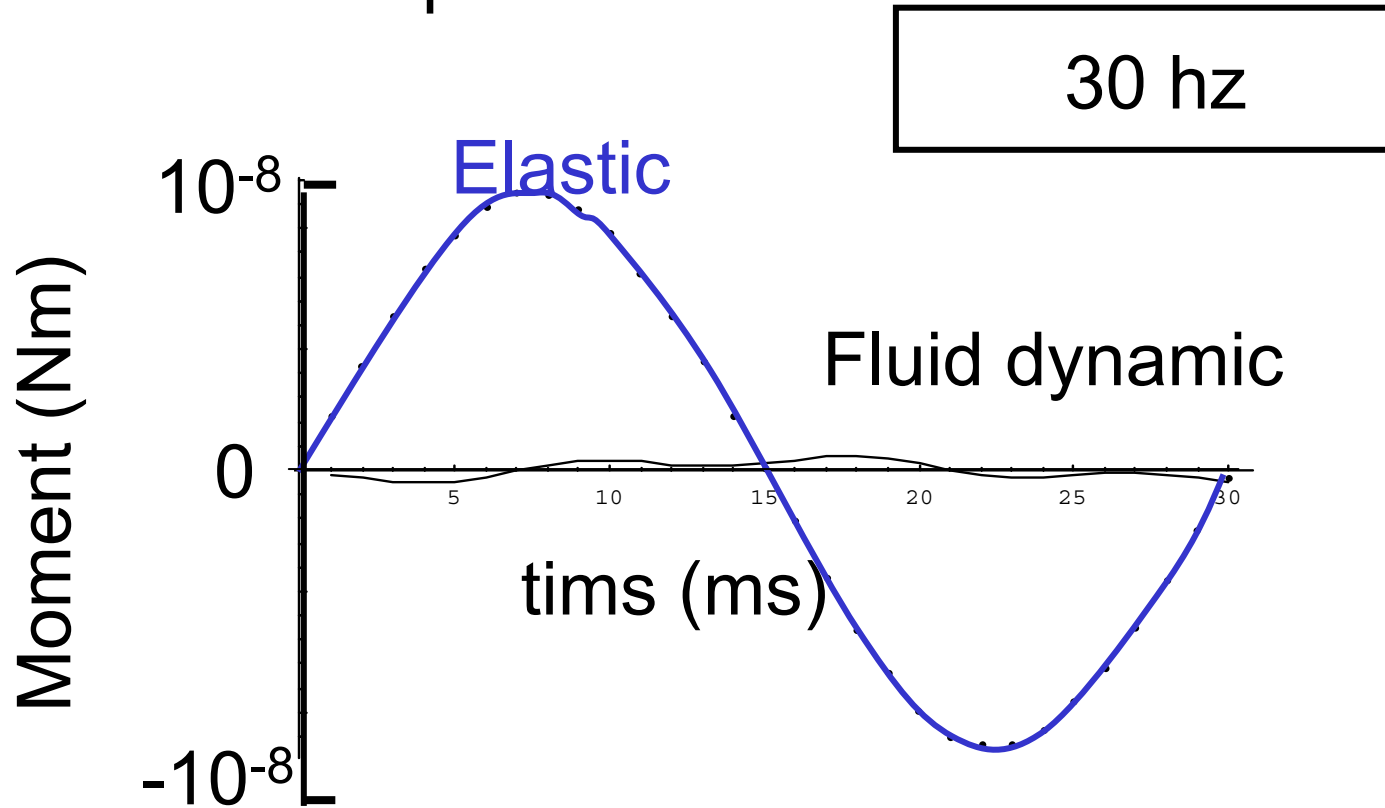
Dynamic bending moments are dominated by elastic/inertial phenomena

30 hz



$$EI = 6 \cdot 10^{-6} \quad \boxed{\text{Length} = 0.03, \text{ width} = 0.01}$$

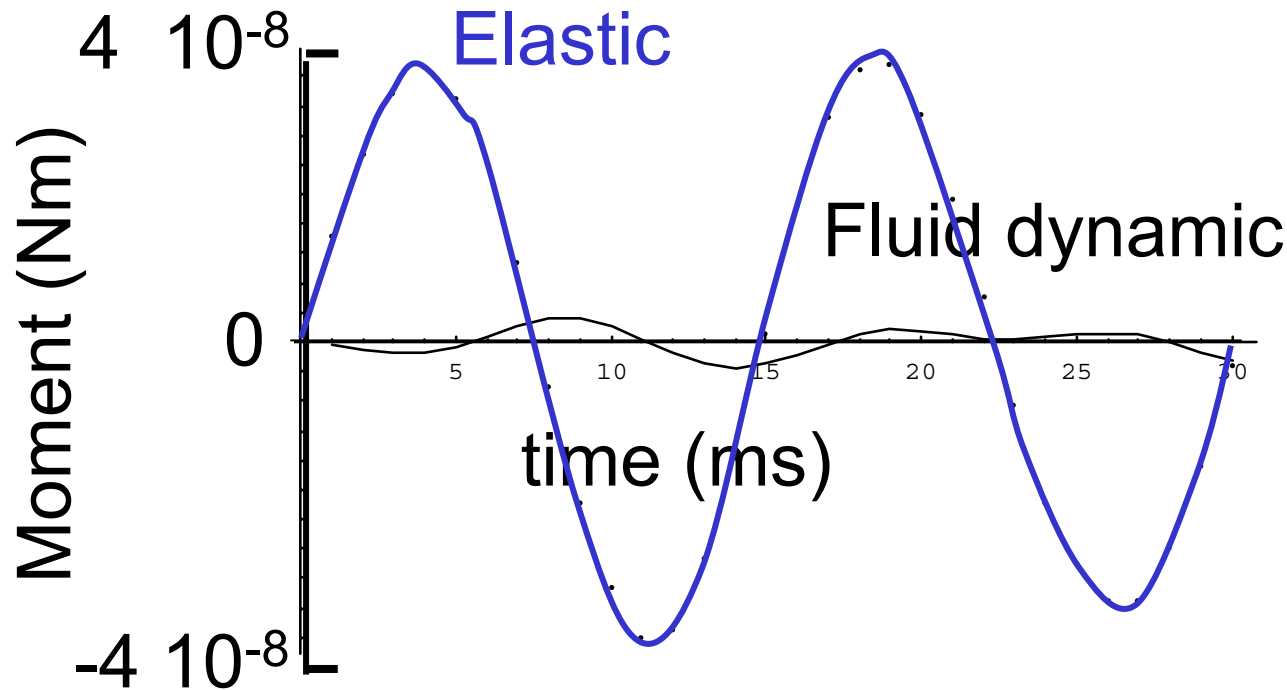
Dynamic bending moments are dominated by elastic/inertial phenomena



↓
 $EI = 6 \cdot 10^{-6}$ Length = 0.02, width = 0.01

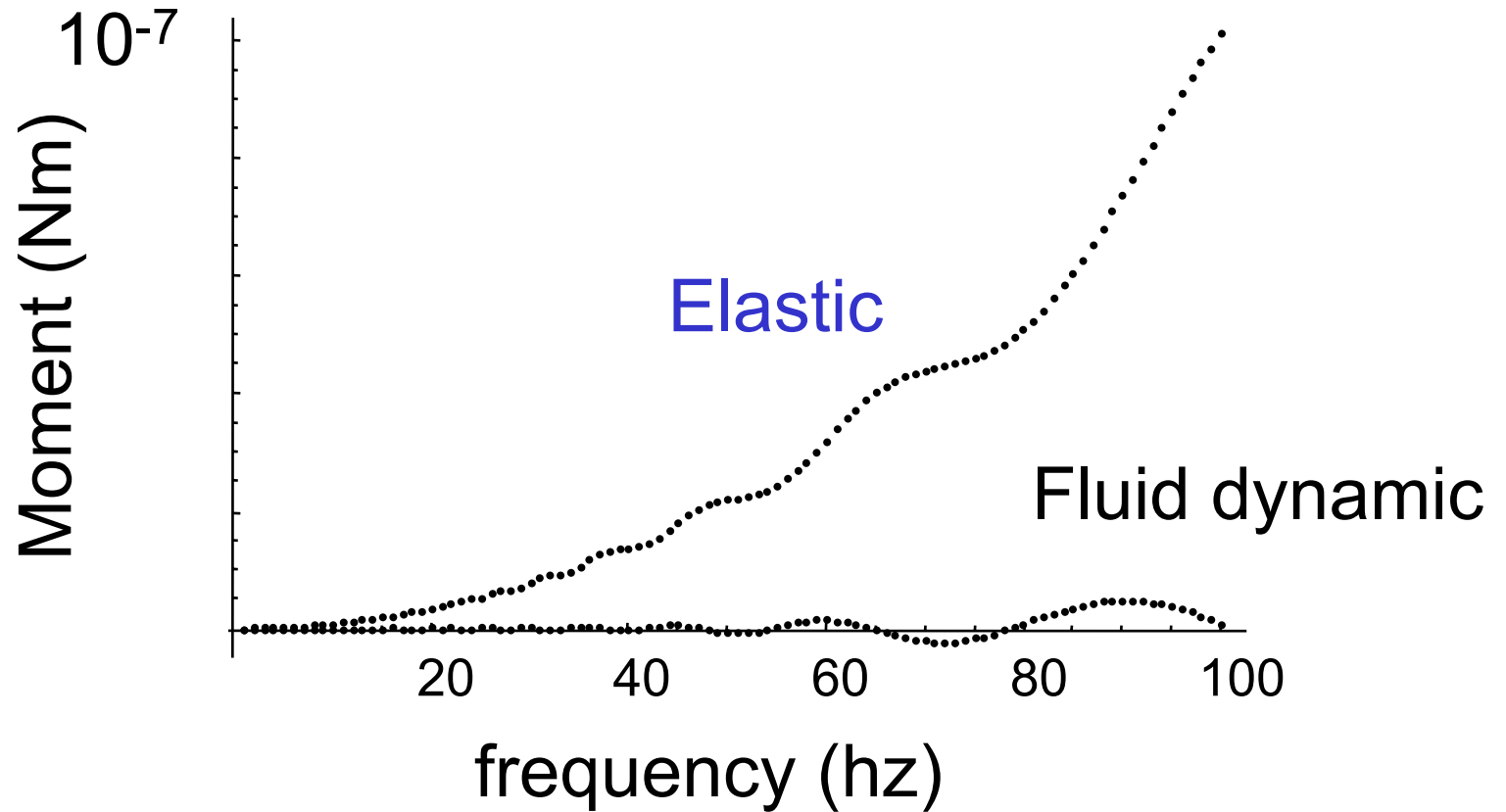
Dynamic bending moments are dominated by elastic/inertial phenomena

↓
60 hz



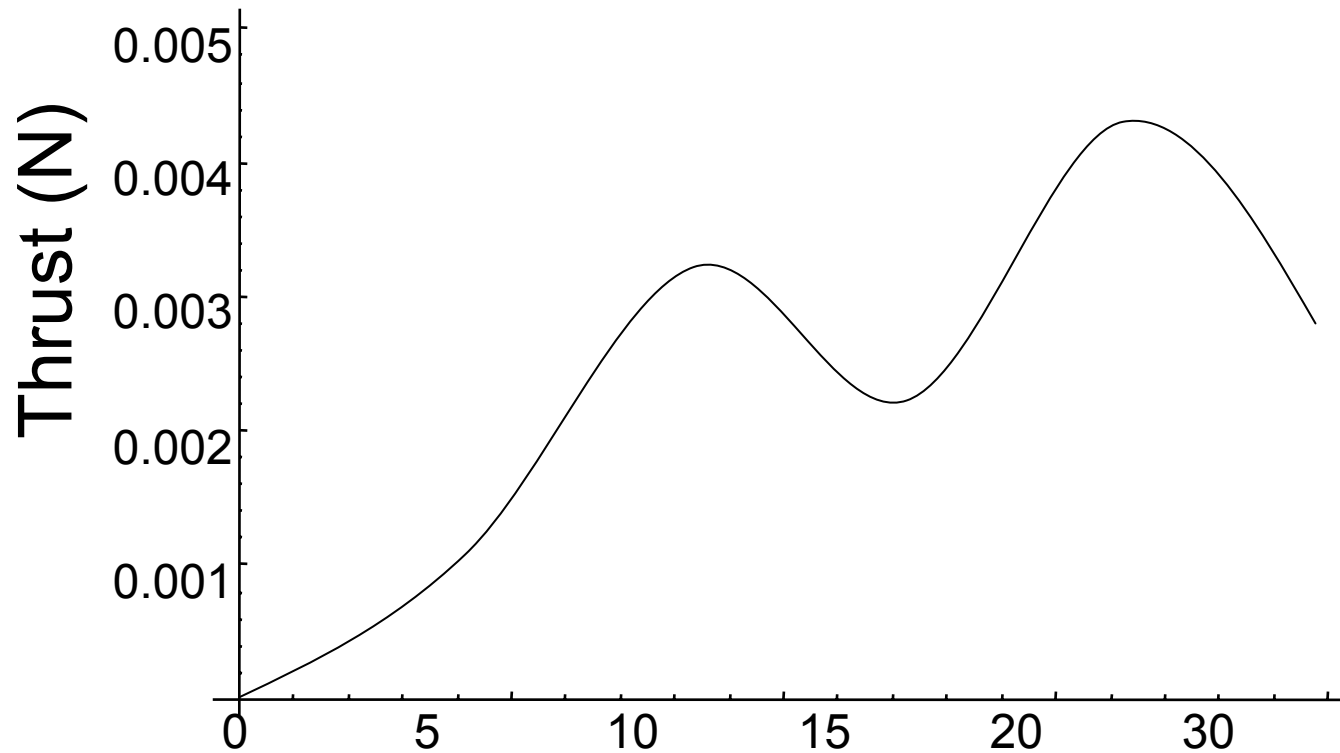
↓
 $EI = 6 \cdot 10^{-6}$ Length = 0.02, width = 0.01

Inertia is generally large



$$EI = 6 \cdot 10^{-6}$$

Thrust depends on emergent deformations (non-monotonically).



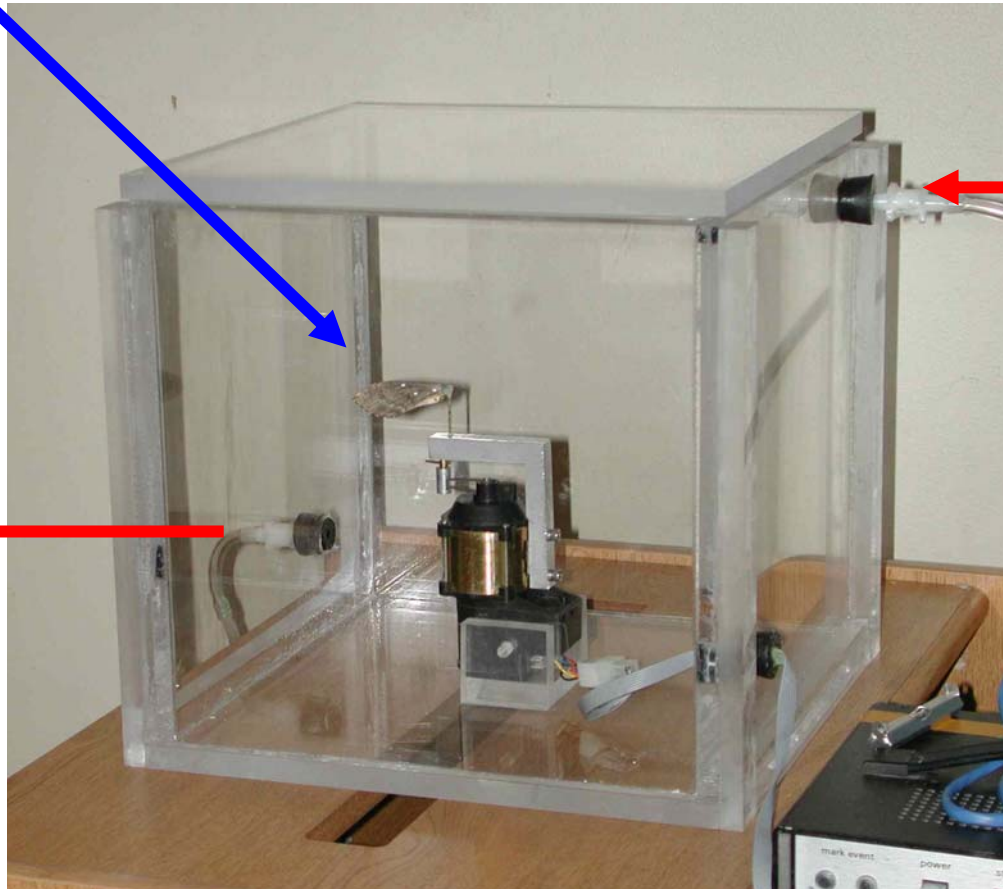
Frequency (hz)

$EI = 6 \cdot 10^{-6}$ Length = 0.03, width = 0.01

Can we trust the theoretical results?

Set density to as low as possible to eliminate fluid dynamic loading and query wing shape.

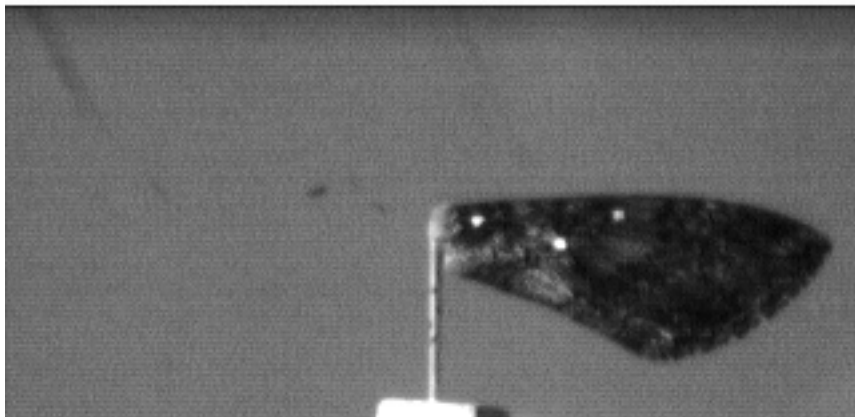
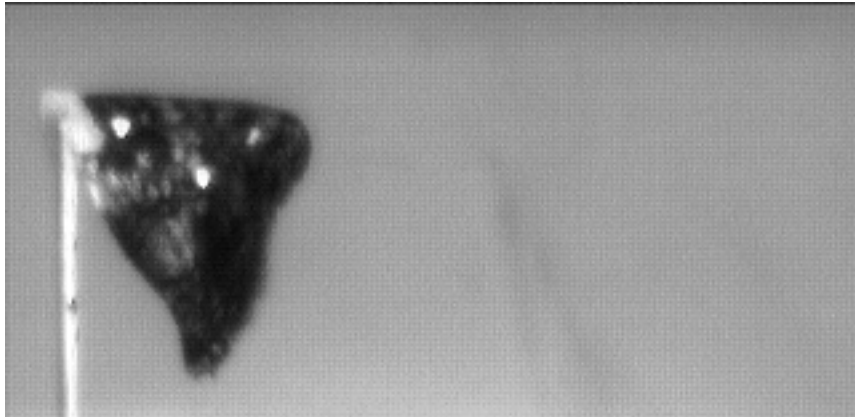
fresh *Manduca* wing on motor



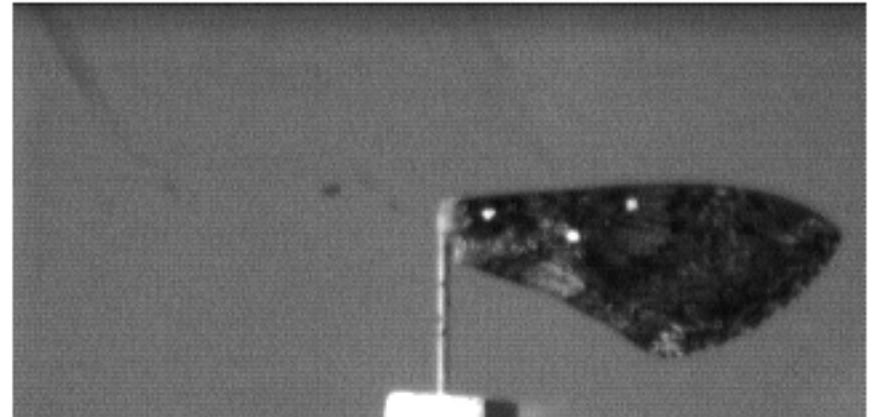
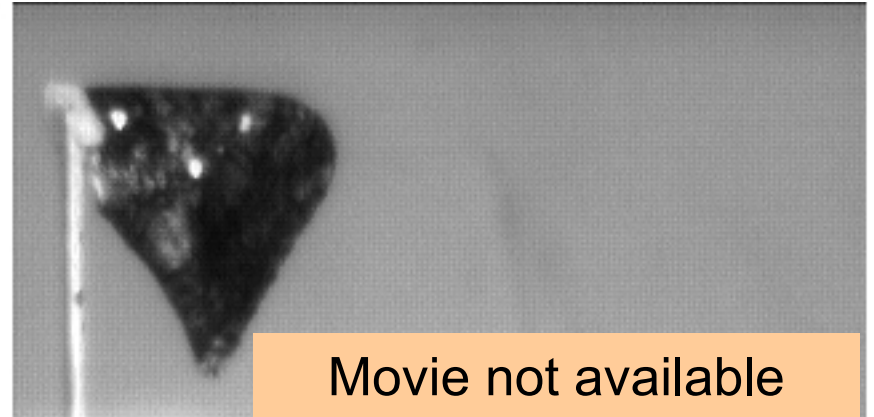
add Helium
(~20% air density)

remove 50%
of air volume

normal air density

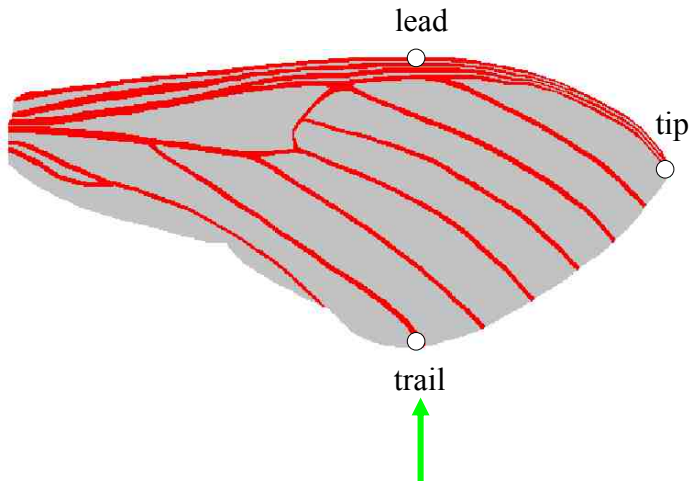
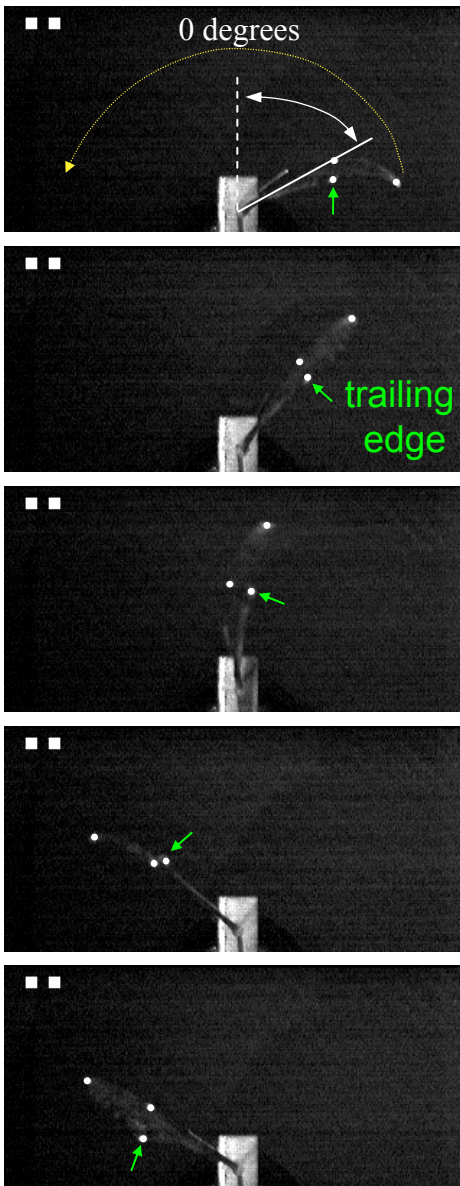


10% air density



Quantify wing bending at the wing tip, leading edge, and trailing edge

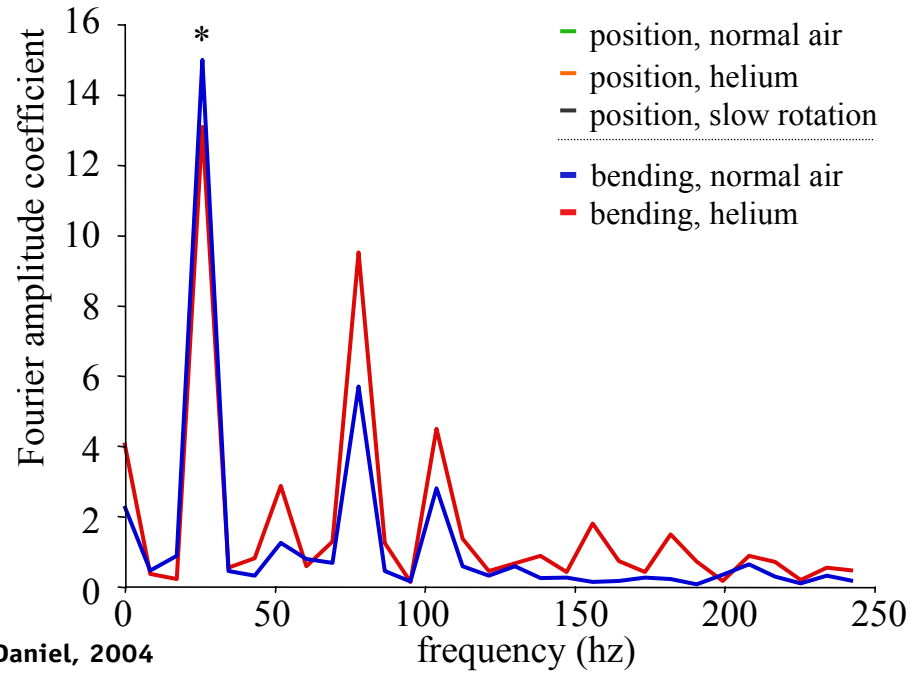
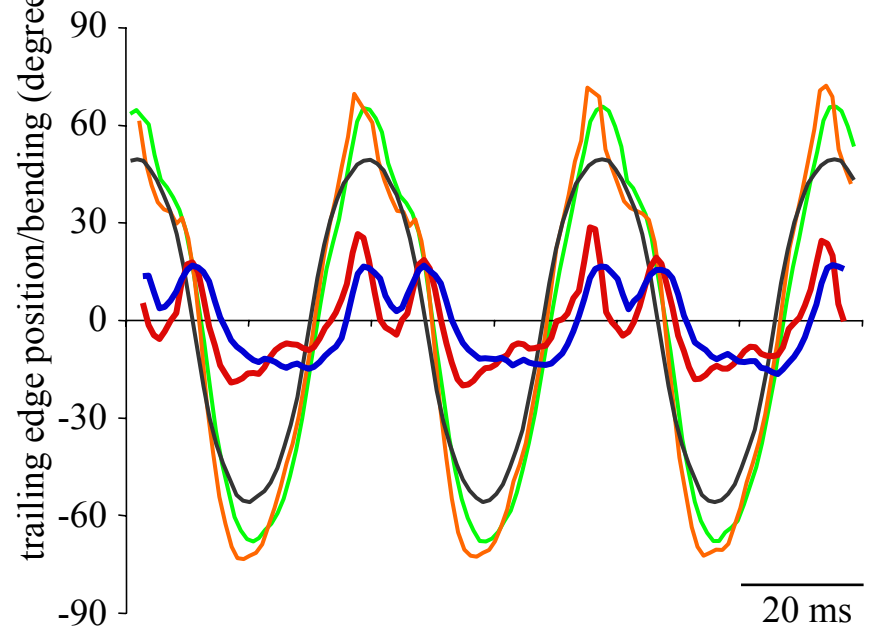
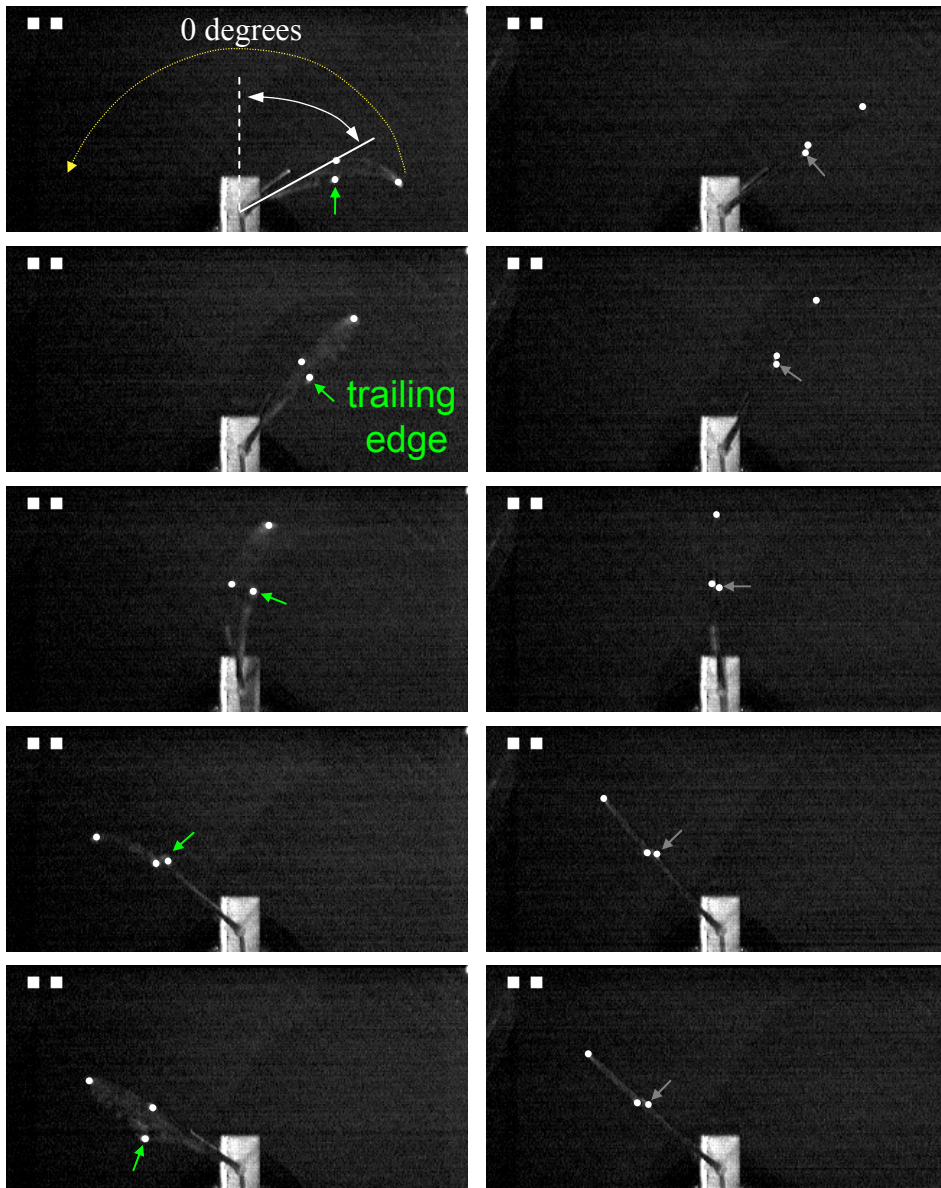
26 Hz, normal air



Quantify wing bending at the wing tip, leading edge, and trailing edge

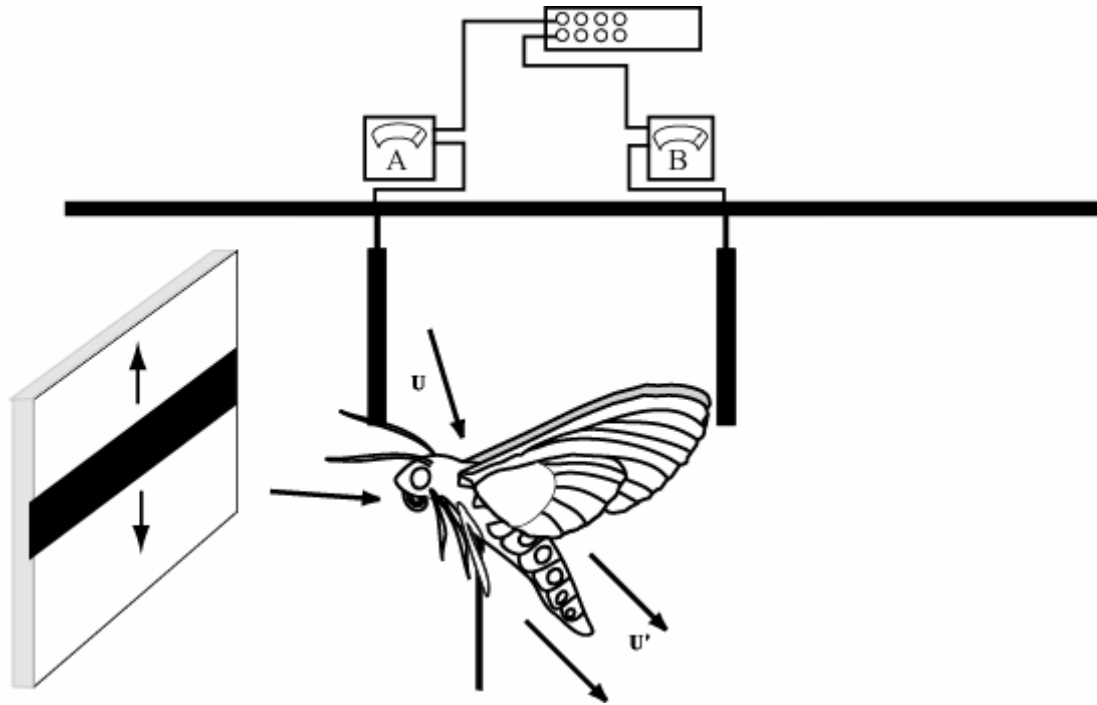
26 Hz, normal air

0.5 Hz



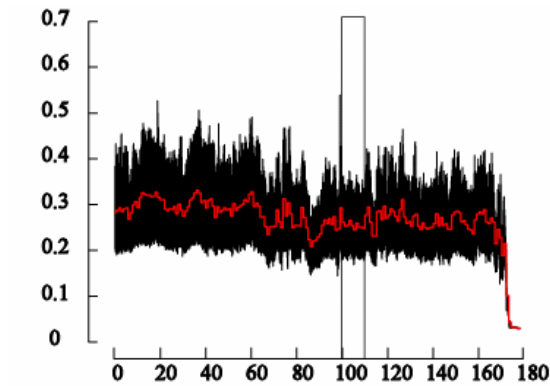
- position, normal air
- position, helium
- position, slow rotation
- bending, normal air
- bending, helium

Evidence of bending on the air flow? Measure self-generated flows

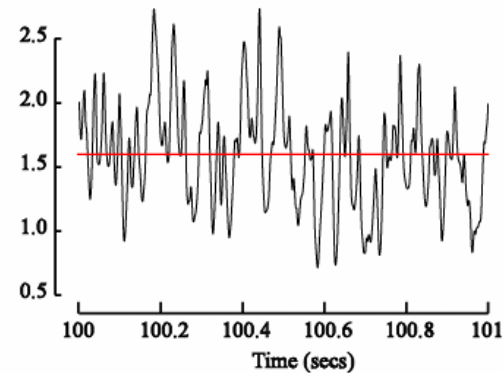
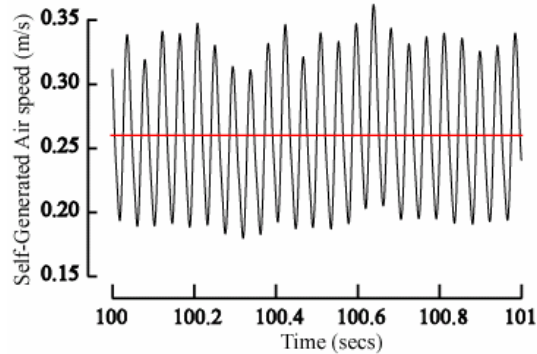
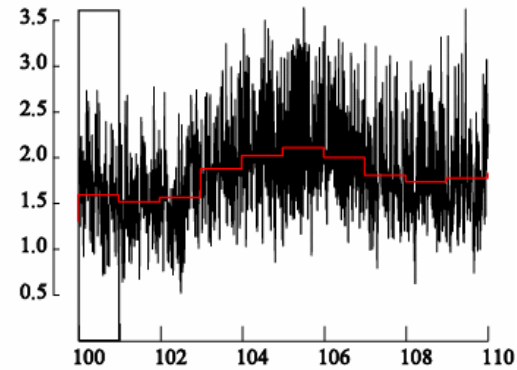
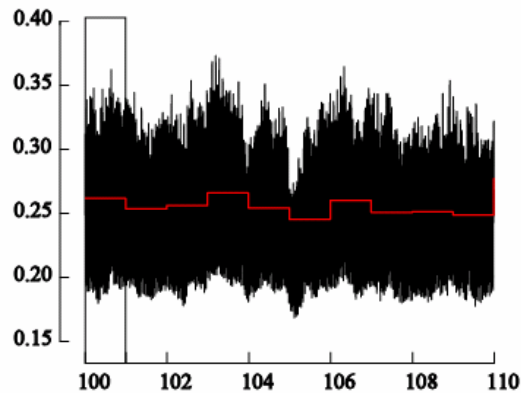
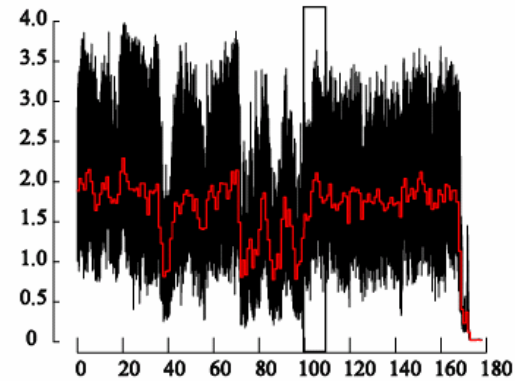


Raw data of self-generated airflow

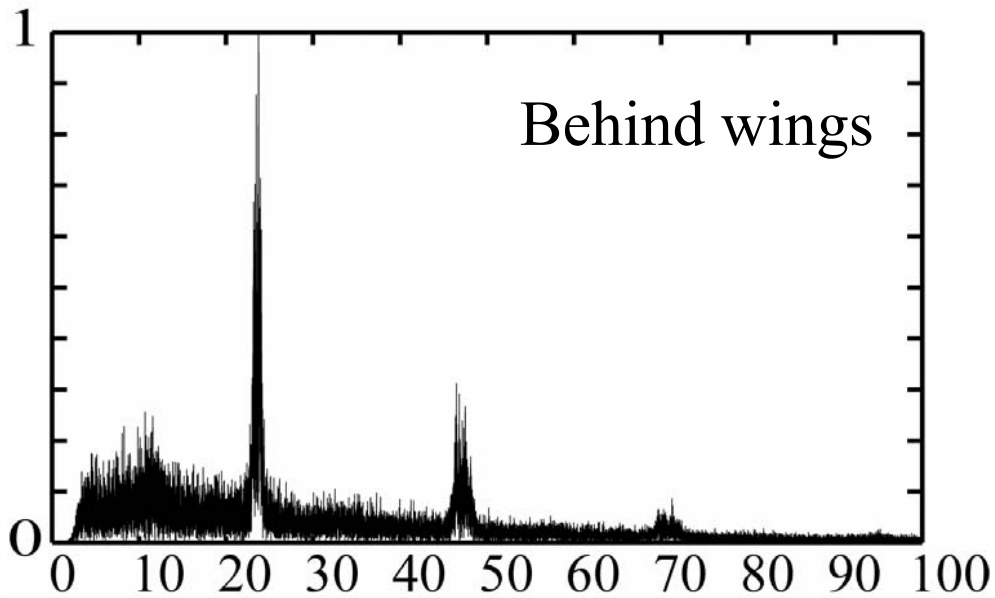
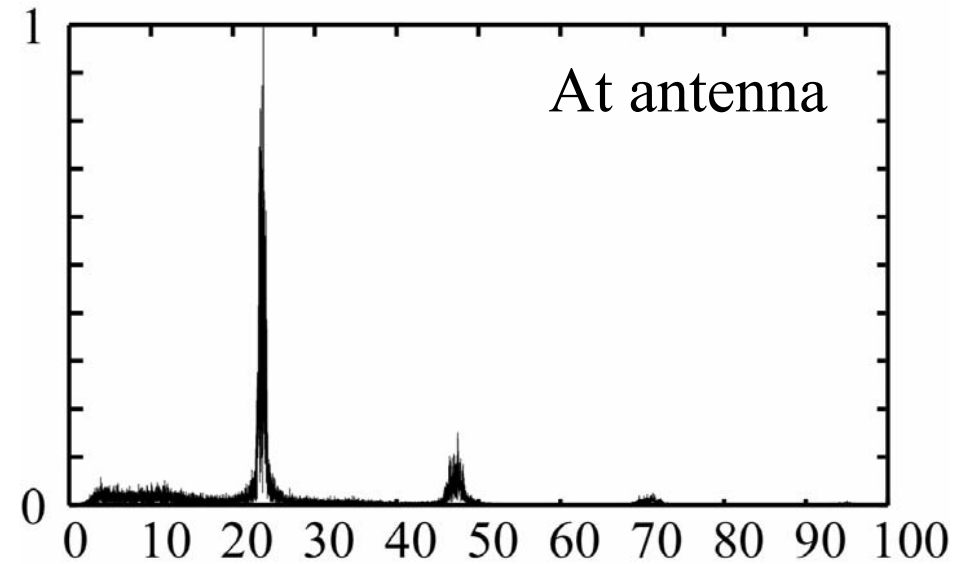
At Antennae



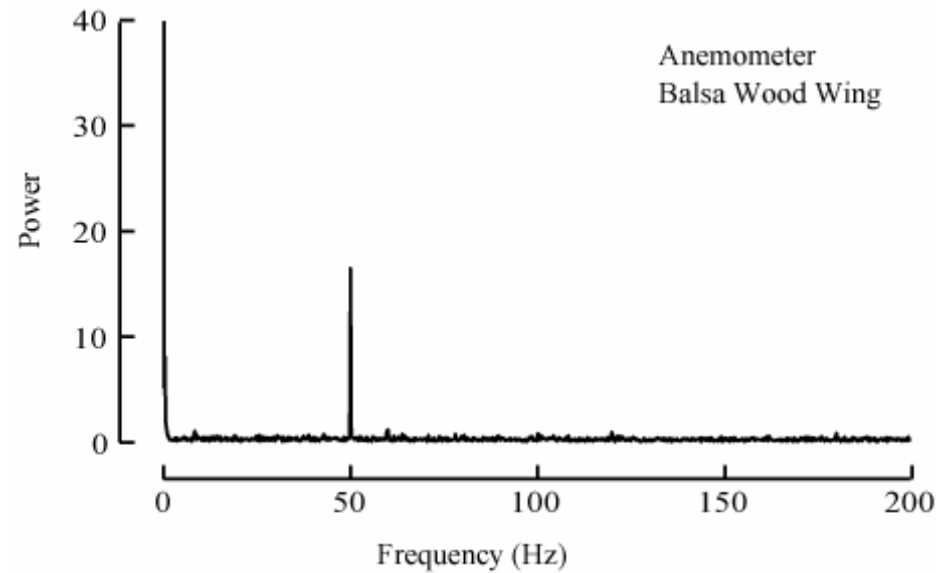
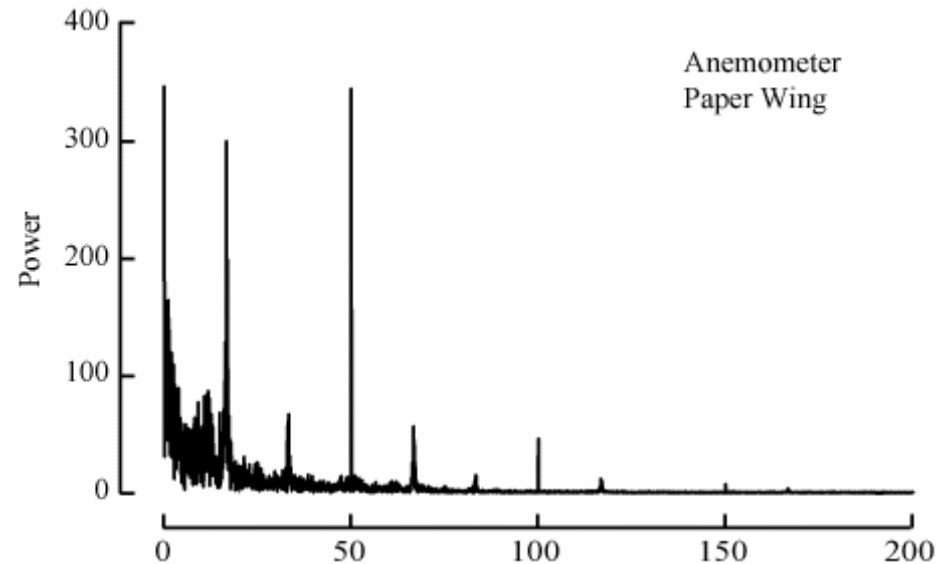
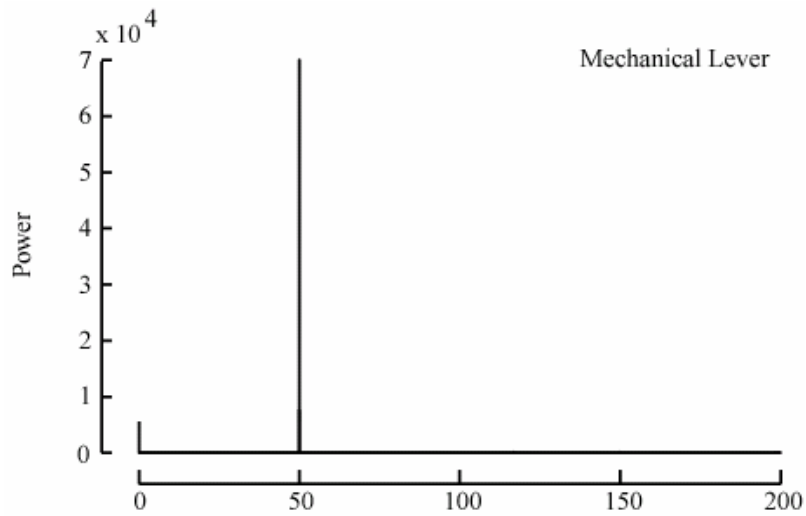
Behind wings



Spectra of recorded airflows

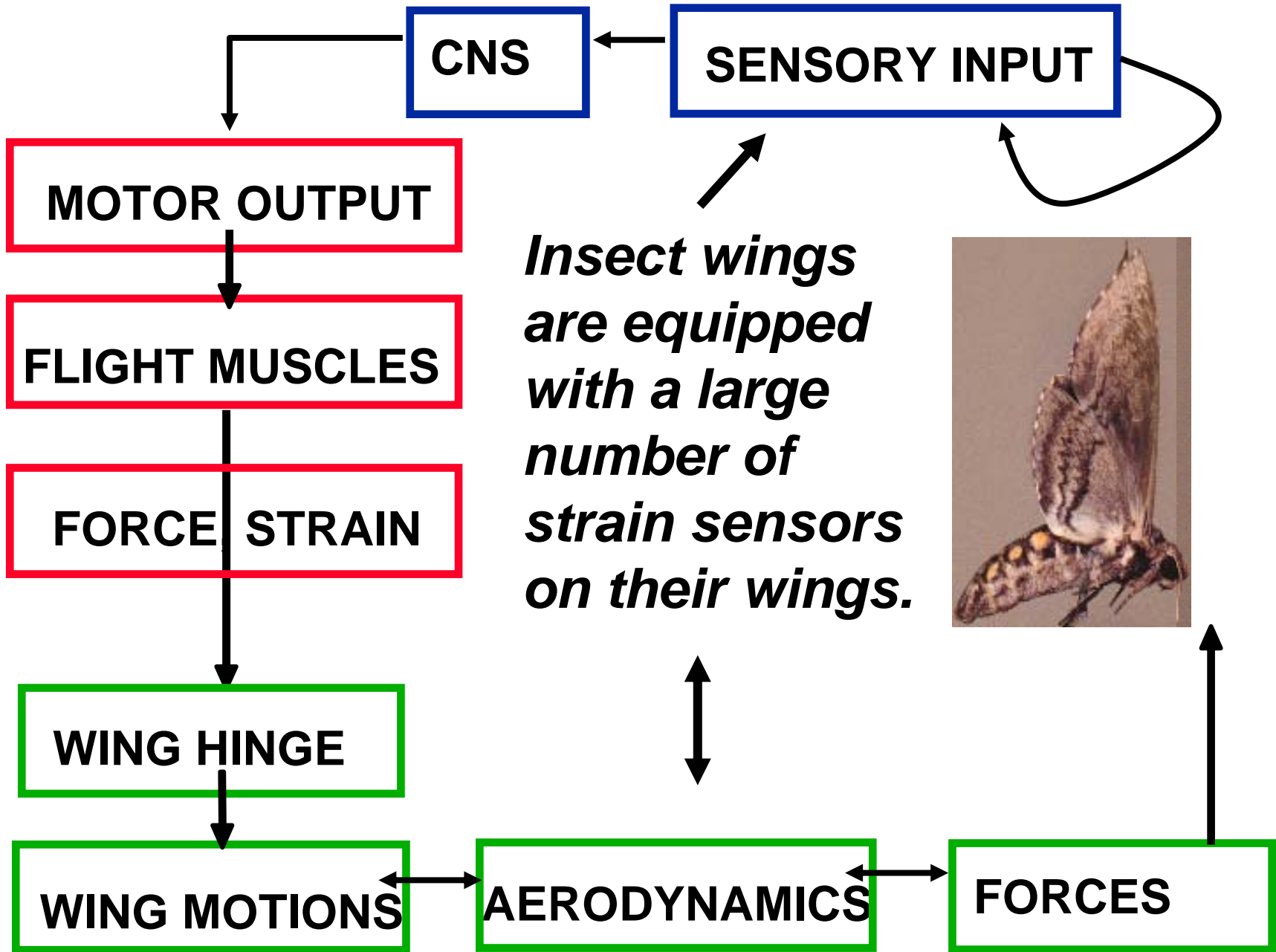


Aerodynamic signature of wing flexibility



Summary

- **Animal wings deform in response to both fluid dynamic loading and their own inertial mechanics.**
- **Simple scaling arguments suggest appendage inertia may dominate moments for “rigid” wings.**
- **Bending moments of wings are dominated by elastic/inertial mechanisms in air.**
- **There is a clear aerodynamic signature of bending wings.**
- **Thus we could use simple explicit methods for evaluating forces on flexible wings in air.**





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T.Y. Wu, Daniel Grunbaum

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NSF

ONR

MacArthur Foundation

Anemometer Calibration

