MORPHODYNAMICS OF RIVERS AND TURBIDITY CURRENTS:

AN ELEGANT CONVERSATION BETWEEN WATER AND SEDIMENT





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A CIVIL ENGINEER/GEOLOGIST GIVING AN INVITED TALK AT THE AMERICAN PHYSICAL SOCIETY

IS LIKE A COUNTRY PRIEST GRANTED AN AUDIENCE WITH THE POPE



http://www.broughtonhousegallery.co.uk/raverat/058-prodigal-son.jpg

Convright G Parker 2007

"PURE FLUID MECHANICS"

Haboob dust storm

Capillary waves Wind ripples **Roll waves** http://www.rikenresearch.riken.jp/research/223/images/2234070426115631.jpg

Image courtesy IOCC

http://www.rikenresearch.riken.jp/research/223/images/2234070426115631.jpg http://scribalterror.blogs.com/scribal_terror/images/2007/05/02/dust_2.jpg http://images.jupiterimages.com/common/detail/66/41/23354166.jpg

HYDRAULIC JUMPS AND BORES

Circular jump in kitchen sink



http://pasternack.ucdavis.edu/falls/aircontent/images/firstthreat.jpg http://upload.wikimedia.org/wikipedia/commons/thumb/f/f4/Hydraulic_jump_in_sink.jpg/391px-Hydraulic_jump_in_sink.jpg http://www.gomoncton.com/ENSite/Motorcoach/images/ImageBank/low/TidalBore_Web.jpg http://imgi.uibk.ac.at/mmetgroup/trex/webstyle/sierrawave.png

NON-SEDIMENT FLUID-BOUNDARY INTERACTION: MEANDERING CHANNELS IN ICE



THE EFFECT OF INCREASING THE WIDTH-DEPTH RATIO B/H

Flume with flow off



Image courtesy H. Ikeda

Courtesy National Geographic

Tributary of Amazon River

Flume with flow off

$B/H \rightarrow UP$

Rhine River, Switzerland



Flume with flow off

$B/H \rightarrow UP$

Fuefuki River, Japan



Courtesy H. Ikeda

Courtesy S. Ikeda

$B/H \rightarrow UP$

Flume with flow off

Ohau River, New Zealand



Courtesy H. Ikeda

RIVER DUNES



DUNES IN THE RHINE DELTA, THE NETHERLANDS



Image courtesy A. Wilbers and A. Blom

DUNE ASYMMETRY



Dunes in a channel at St. Anthony Falls Laboratory, University of Minnesota, USA

Dunes in a channel at Tsukuba University, Japan. 12 Image courtesy H. Ikeda.

FELIX EXNER: FATHER OF RIVER MORPHODYNAMICS

Exner's Question (1920, 1925): Why Are Dunes Asymmetric?

The parameters:

x = streamwise distance [L]

t = time [T]

 η = bed elevation [L]

 q_t = volume total sediment transport rate per unit stream width [L²/T]

 $\xi = H + \eta$ = water surface elevation [L]

 λ_p = bed porosity [1]

g = acceleration of gravity [L/T²]

H = flow depth [L]

U = depth-averaged flow velocity [L/T]

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q_w = UH = water discharge per unit stream width [L²/T]



OCCAM'S RAZOR: THE MIMINAL FORMULATION TO ANSWER THE QUESTION

Shallow-water inviscid equations of mass and momentum balance

$$\frac{\partial H}{\partial t} + \frac{\partial UH}{\partial x} = 0 \quad \rightarrow \quad UH = q_w = \text{constant}$$
$$\frac{\partial UH}{\partial t} + \frac{\partial U^2H}{\partial x} = -\frac{1}{2}gH\frac{\partial H}{\partial x} - \frac{1}{2}gH\frac{\partial \eta}{\partial x}$$

Quasi-steady assumption: $q_t/q_w \ll 1$

Exner's equation of conservation of bed sediment:

$$\boxed{(1-\lambda_{p})\frac{\partial\eta}{\partial t}=-\frac{\partial q_{t}}{\partial x}}$$

Relation between sediment transport rate and flow hydraulics:

$$\boldsymbol{q}_t = \boldsymbol{q}_t(\boldsymbol{U}) = \alpha \boldsymbol{U}^n \quad \text{,} \quad \boldsymbol{n} > \boldsymbol{0}$$

Exner's seminal contribution: if more sediment enters a reach than leaves, the bed elevation in the reach increases.

The phenomenon of sediment transport was poorly known in Exner's time. Exner guessed that a higher velocity caused a higher sediment transport rate. ¹⁴

REDUCTION

$$UH = q_w$$
 and $H = \xi - \eta \rightarrow U = \frac{q_w}{\xi - \eta}$

$$\begin{aligned} \frac{\partial U^{2}H}{\partial x} &= -\frac{1}{2}gH\frac{\partial H}{\partial x} - \frac{1}{2}gH\frac{\partial \eta}{\partial x} \quad \text{and} \quad H = \xi - \eta \quad \text{and} \quad U = \frac{q_{w}}{\xi - \eta} \\ \rightarrow \\ \frac{\partial H}{\partial x} &= -\frac{1}{(1 - Fr^{2})}\frac{\partial \eta}{\partial x} \quad \text{and} \quad \frac{\partial \xi}{\partial x} = -\frac{Fr^{2}}{(1 - Fr^{2})}\frac{\partial \eta}{\partial x} \\ \text{where} \\ Fr &= \frac{U}{\sqrt{gH}} = Froude number \end{aligned}$$

Range for dunes: low Froude number: **Fr**² << 1

$$\boxed{\frac{\partial \xi}{\partial \mathbf{x}} = -\frac{\mathbf{Fr}^2}{(1 - \mathbf{Fr}^2)} \frac{\partial \eta}{\partial \mathbf{x}} \cong \mathbf{0} \quad \therefore}$$

Constant water surface elevation

MORE REDUCTION

$$\begin{array}{ll} U = \displaystyle \frac{q_w}{\xi - \eta} & \text{and} & q_t = \alpha U^n & \text{and} & \displaystyle \frac{\partial H}{\partial x} = \displaystyle -\frac{1}{1 - \mathbf{Fr}^2} \displaystyle \frac{\partial \eta}{\partial x} \\ \\ \text{and} & \mathbf{Fr}^2 << 1 & \text{and} & \xi = \text{constant} \end{array}$$

substituted into

$$(1 - \lambda_{p})\frac{\partial \eta}{\partial t} = -\frac{\partial q_{t}}{\partial x}$$

yields

$$\frac{\partial \eta}{\partial t} + c(\eta) \frac{\partial \eta}{\partial x} = 0$$

$$c(\eta) = \alpha q_w^n (\xi - \eta)^{-(n+1)}$$

Since ξ = constant. q_w = constant and n > 0, c > 0 is an increasing function of η !

THE RESULT

Dunes migrate downstream, and migration speed increases with bed elevation





THE FLOW AND THE BED TALK TO EACH OTHER

The field of **sediment morphodynamics** consists of the class of problems for which the flow over a bed interacts strongly with the shape of the bed, both of which evolve in time.



Quasi-steady assumption:

The flow naturally talks fast, but can also talk slow.

The bed naturally talks slow.

The only part of the flow's talk that the bed hears is the slow part.

(Quasi-steady assumption: $q_t/q_w <<1$)

THE CONVERSATION



SCALES



LONGITUDINAL STREAKS





LONGITUDINAL STREAKS: LINEAR STABILITY ANALYSIS



$$\begin{split} V \frac{\partial U}{\partial y} + W \frac{\partial U}{\partial z} &= 1 + \frac{\partial \tau_{xy}}{\partial y} + \frac{\partial \tau_{xz}}{\partial z}, \\ V \frac{\partial V}{\partial y} + W \frac{\partial V}{\partial z} &= -\frac{\partial P}{\partial y} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{yz}}{\partial z}, \\ V \frac{\partial W}{\partial y} + W \frac{\partial W}{\partial z} &= -\frac{\partial P}{\partial z} + \frac{\partial \tau_{yz}}{\partial y} + \frac{\partial \tau_{zz}}{\partial z}, \\ \frac{\partial V}{\partial y} + \frac{\partial W}{\partial z} &= 0, \end{split}$$



3D non-isotropic closure for Reynolds-averaged Navier-Stokes equations: Speziale.

Closure for sediment transport rates q_x and q_z in terms of bed shear stress and slope vectors.

$$\tau_{ij} = -\frac{2}{3}k\delta_{ij} + 2\nu_t D_{ij} + C_D l^2 (D_{im} D_{mj} - \frac{1}{3}D_{mn} D_{mn}\delta_{ij}) + C_E l^2 (\widehat{D}_{ij} - \frac{1}{3}\widehat{D}_{mm}\delta_{ij}).$$

Here D_{ij} is the mean rate of strain tensor, $v_t = \frac{1}{2}k^{1/2}l$ is the eddy viscosity and

$$\widehat{D}_{ij} = \frac{\mathrm{D}D_{ij}}{\mathrm{D}t} - \frac{\partial U_i}{\partial x_k} D_{kj} - \frac{\partial U_j}{\partial x_k} D_{ki}$$
²²

DUNES, ANTIDUNES



DEFINITION OF DUNES AND ANTIDUNES

Dunes are 1D (or quasi-1D) bedforms for which the water surface fluctuations are approximately *out of phase* with the bed fluctuations. That is, the water surface is high where the bed is low and vice versa. As is shown below dunes migrate downstream.



Antidunes are 1D (or quasi-1D) bedforms for which the water surface fluctuations are approximately *in phase* with the bed fluctuations. That is, the water surface is high where the bed is high and vice versa. As shown below, most antidunes migrate upstream, but there is a regime within which they can migrate downstream.



REGIME DIAGRAM: POTENTIAL FLOW OVER A WAVY BED

- x = streamwise direction
- y = vertical direction
- u = streamwise velocity
- v = vertical velocity
- p = pressure
- g = gravitational acceleration



$$\begin{split} &\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0\\ &u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = -\frac{1}{\rho}\frac{\partial p}{\partial x} - g\frac{\partial \eta}{\partial x}\\ &u\frac{\partial v}{\partial x} + v\frac{\partial v}{\partial y} = -\frac{1}{\rho}\frac{\partial p}{\partial v} - g\\ &\eta = \eta_o \sin(kx) \quad , \quad k = \frac{2\pi H_o}{\lambda} \end{split}$$

 η_o = amplitude of bed perturbation H_o = unperturbed depth

Linearized potential flow analysis is sufficient to explain existence regimes, but not formation (gives neutral stability)

PHASE DIAGRAM FOR DUNES AND ANTIDUNES BASED ON LINEAR POTENTIAL THEORY OVER A WAVY BED



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FLOW IN THE DUNE REGIME

 $Fr_o < [tanh(k)/k]^{1/2}$ $k = 2\pi H/\lambda$ H = dWater surface is out of phase with the bed.Depth variation is out of phase with the bedFlow accelerates from trough to crest.Sediment transport increases from trough to crest.Bedform migrates downstream.Bedform becomes asymmetric.

flow





FLOW IN THE UPSTREAM-MIGRATING ANTIDUNE REGIME

 $[\tanh(k)/k]^{1/2} < \mathbf{Fr}_o < [k \tanh(k)]^{-1/2}$ Water surface is in phase with the bed. Depth variation is in phase with the bed Flow decelerates from trough to crest. Sediment transport decreases from trough to crest. Bedform migrates upstream (or hardly at all). Bedform stays symmetric.





FLOW IN THE DOWNSTREAM-MIGRATING ANTIDUNE REGIME

 $[k \tanh(k)]^{-1/2} < Fr_{o}$

Water surface is in phase with the bed.

Depth variation is out of phase with the bed.

Flow accelerates from trough to crest.

Sediment transport increases from trough to crest.

Bedform migrates downstream.

Bedform becomes asymmetric.

These are antidunes that look like dunes: not too common, but they are observed.



No shallow-water limit as $k \rightarrow 0$.

STABILITY ANALYSIS FOR DUNES AND ANTIDUNE FORMATION: OCCAM'S RAZOR

$$\begin{split} & \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \\ & u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - g \frac{\partial \eta}{\partial x} + \frac{\partial}{\partial x} \left(v_t \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial x} \left(v_t \frac{\partial u}{\partial y} \right) - g \frac{\partial \eta}{\partial x} \\ & u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial v} - g + \frac{\partial}{\partial x} \left(v_t \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial x} \left(v_t \frac{\partial v}{\partial y} \right) - g \frac{\partial \eta}{\partial x} \\ & \eta = \eta_o e^{\alpha t} \sin(kx) \quad , \quad k = \frac{2\pi H_o}{\lambda} \end{split}$$

Closure for v_t : a constant value that gives a result close to the logarithmic law

In sediment transport law, $\tau_{\rm b}$ = bed shear stress

INSTABILITY MECHANISM FOR DUNES

Consider flow into a Venturi contraction.

The favorable pressure gradient on the upstream side intensifies the bed shear stress.

The adverse pressure gradient on the downstream side suppresses shear stress.



peaks a little before the bed perturbation peak

NET DEPOSITION AT APEX: LINEAR MODEL

The bed shear stress perturbation, and thus the sediment transport rate perturbation, lead the bed elevation perturbation.

There is thus net deposition at the apex (and net erosion at the trough), and so amplitude increases in time.

A nonlinear analysis including flow separation on the lee side of dunes is necessary to explain nonlinear equilibrium: numerical, e.g. $k-\epsilon$



Bed perturbation: black solid

sediment transport rate perturbation: red dashed

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NONLINEAR PHENOMENON OF ANTIDUNES



SINGLE-ROW AND MULTIPLE-ROW ALTERNATE BARS

Occam's razor minimal analysis: 2D shallow water equations + 2D sediment transport formulation

Controlling parameter: width-depth ratio B/H No bars \rightarrow single-row bars \rightarrow multiple-row bars

Naka River, Japan



Hii River, Japan



Image courtesy H. Takebayashi








http://www.athabascalake.com/ecoexped/william_river_braided.jpg



Copyright G. Parker, 2007 BRAIDING MECHANISM: CONFLUENCES



NONLINEAR INTENSIFICATION OF SEDIMENT **TRANSPORT RATE AT CONFLUENCES: SCOUR**



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DOWNSTREAM, THE FLOW EXPANDS AND DEPOSITS A MINI-FAN



DOWNSTREAM, THE FLOW EXPANDS AND DEPOSITS A MINI-FAN



AS THE FLOW GETS WIDER AND SHALLOWER, IT BECOMES UNSTABLE AND BIFURCATES INTO ONE OR MORE CHANNELS

Image courtesy P. Ashmore

AS THE FLOW GETS WIDER AND SHALLOWER, IT BECOMES UNSTABLE AND BIFURCATES INTO ONE OR MORE CHANNELS

Image courtesy P. Ashmore

MEANDERING





MEANDERING MECHANISM

Occam's razor first analysis:

2D shallow-water equations corrected for effect of helical flow in bends (2.5D formulation)

+

Relation for channel migration:



ONLY BRAIDING IS POSSIBLE IN THE ABSENCE OF **BANK STABILIZATION**

Image courtesy B. Murray



Braided stream on the North Slope, Brooks Range, Alaska

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SWEET LITTLE LIES

Yes, honey, I'm with you.



http://images.google.com/imgres?imgurl=http://jeroenarendsen.nl/pics/Conversation-Icelanderspianist.gif&imgrefurl=http://jeroenarendsen.nl/category/countries/&h=327&w=387&sz=94&hl=en&start=14&um=1&tbnid= 4OxIA6BGtduRcM:&tbnh=104&tbnw=123&prev=/images%3Fq%3Dconversation%26ndsp%3D21%26svnum%3D10%26 um%3D1%26hl%3Den%26client%3Dfirefox-a%26rls%3Dorg.mozilla:en-US:official%26sa%3DN



Inside bank to outside bank:

"Yes, I'm following you."



Inside bank to outside bank:

"Yes, I'm following you."



Yeah, while you were pretending to listen, *look at the mess we got ourselves into!*



Image courtesy H. Johannesson

BEND SKEWING: SUBCRITICAL BIFURCATION OF NONLINEAR STABILITY ANALYSIS



SLUMPING ON OUTSIDE SLOWS DOWN EROSION SO TRAPPING OF SEDIMENT BY VEGETATION ON INSIDE CAN KEEP UP





Do we talk to each other?

I trap

Vermilion River, USA

NOW FOR A TOUR OF MORPHODYNAMIC PHENOMENA WITHOUT DETAIL AS TO HOW THEY ARE SOLVED

Yes, they are tractable to various degrees



SCROLL BARS





Strickland River, Papua New Guinea

ALLUVIAL FANS AND FAN-DELTAS



THE OKAVANGO INLAND FAN, BOTSWANA, AFRICA



Graben: subsidence

THE FAN-DELTA OF THE KUROBE RIVER, JAPAN



THE FAN-DELTA OF THE IOCC IRON MINE, LABRADOR, CANADA



THE FAN IN THE DELTA



FANS AND FAN-DELTAS AT VARIOUS SCALES



Laboratory fan-delta, ~ 3 m. 62 Image taken at St. Anthony Falls Laboratory, University of Minnesota USA.

FANS AND FAN-DELTAS AT VARIOUS SCALES contd.



Fan created by runoff from cultivated field; ~ 6 m. Image taken by author near Pigeon Point, California.

FANS AND FAN-DELTAS AT VARIOUS SCALES contd.



Fan in Idaho, USA created by runoff from burned hillside, ~ 50 m.

FANS AND FAN-DELTAS AT VARIOUS SCALES contd.



Copper Creek Fan, Death Valley, USA; ~ 10 km. Image courtesy Roger Hooke.

FANS AND FAN-DELTAS AT VARIOUS SCALES contd.



https://zulu.ssc.nasa.gov/mrsid/

Kosi River Fan, India; ~ 125 km.

RIVER MIGRATION AND AVULSION MAKES FANS



https://zulu.ssc.nasa.gov/mrsid/

Yellow River Fan-delta, China



CONCAVE BANK BENCHES



SELF-CHANNELIZATION: NATURAL LEVEES

Image courtesy National Geographic

https://zulu.ssc.nasa.gov/mrsid/

Missisippi River, USA



SEA LEVEL ROSE SOME 120 M SINCE THE END OF THE LAST GLACIATION



How does a river mouth respond to sea level rise?

- Does a delta continue to prograde into the ocean?
- Or does the sea drown the delta and invade the river valley (transgression)?

DELTAS AND SEA LEVEL RISE

Experiment on effect of base level rise on delta

Image courtesy T. Muto



AUTORETREAT
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HOW DID THE DELTAS OF MAJOR RIVERS RESPOND?





BEDROCK INCISION

Somewhere in Bolivia



SUBMARINE MORPHODYNAMICS DUE TO TURBIDITY CURRENTS



California Margin

Image courtesy MBARI



CANYON EXCAVATION



MEANDERING OF SUBMARINE CHANNELS



CONGO DEEP-SEA FAN



EM12 Bathymetry of the Pleistocene to Present Zaire Deep-Sea Fan.

FANS AND CANYONS: STEPPED PROFILES



SELF-CONFINEMENT AND LEVEE CONSTRUCTION

Turbidity currents are adept at confining themselves between levees.



Channel on Amazon Submarine Fan Damuth and Flood (1985)

Toyama Submarine Channel Kubo and Nakajima (2002)

SELF-CONTAINMENT

Cut-off Loop

Submarine meandering channels contain themselves between levees over 100's ~ 1000's of km and scores ~ 100's of bends.





CYCLIC STEPS: A UNIVERSAL BEDFORM OF **FROUDE-SUPERCRITICAL FLOW** IN RIVERS AND TURBIDITY CURRENTS FLOWING **OVER ERODIBLE BEDS**



Images courtesy M. Neumann, H. Capart and L. Pratson

TRAIN OF HYDRAULIC JUMPS



Trains of cyclic steps in a coastal outflow channel on a beach in Calais, France. Image courtesy H. Capart.

The steps move upstream

THE IDEA

Steady, uniform (normal) Froude-supercritical flow ($Fr_n > 1$) over a freely-erodible bed of sand might be unstable,

and within an appropriate range might not devolve to ephemeral, short-wave $(L/h \sim 1)$ antidunes, but instead would devolve to

orderly, sustained trains trains of long-wave (L/h << 1) cyclic steps, with regions of subcritical and supercritical flow bounded by hydraulic jumps



FULLY NONLINEAR PERIODIC SOLUTION OF PERMANENT FORM WITH CONSTANT UPSTREAM MIGRATION

Sufficiently supercritical flow over a plane bed is subject to a *long-wave* instability that devolves into upstream-migrating supercritical and subcritical regions bounded by hydraulic jumps.



LIKE THIS



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LET'S LOOK AT THIS IMAGE AGAIN



THE SAME CYCLIC STEP INSTABILITY IS FOUND IN INCISING BEDROCK STREAMS



Image courtesy H. Ikeda

CYCLIC STEPS IN BEDROCK: This one is too beautiful not to show



Ojiro River, Japan

WHAT ARE THESE WASHBOARD-LIKE FEATURES IN THE DEEP SEA?

Seabed "sediment waves" off the California margin

Image courtesy MBARI

Computer generated image of the topograhy onshore (brown) and offshore (blue) Central California. Prepared by Norman M. Maher and Robert K. Hall.

Southern

anta Cruz

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106

ion Seameur

lorthern

U.S. Goologie is Surve

124.0°W

Pioneer S

Marine Sanctuary

Gulf of the Farallones National Marine Sanctuary

Cordell Bank National

Monterey Bay National Marine Sanctuary

50 km







SUBAQUEOUS DEPOSITIONAL AND EROSIONAL CYCLIC STEPS



$\mathsf{EARTH} \to \mathsf{TITAN}$





European Space Agency

Water \rightarrow liquid methane Granitic rock \rightarrow ice as a "rock"

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ALLUVIAL GRAVEL-BED RIVERS ON TITAN?



The evidence suggests that at least near where Huygens touched down, there is a **plethora of alluvium in the gravel and sand sizes**. The **gravel** presumably consists of **water ice** and appears to be **fluvially rounded**.⁹⁵

AN EXCITING FUTURE WAITS

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COLUMN TO STREET