



# Spectroscopic Ellipsometry:

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**What it is, what it will do,  
and what it won't do**

by

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- Introduction
- Fundamentals
- Anatomy of an ellipsometric spectrum
- Analysis of an ellipsometric spectrum
- What you can do, and what you can't do

# Perspective

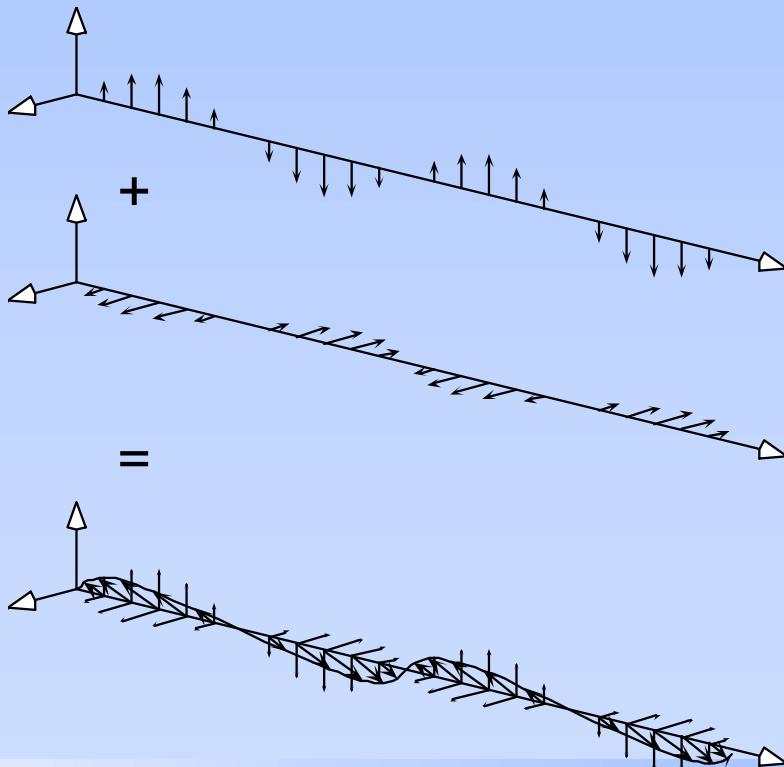
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- Spectroscopic Ellipsometry is an optical technique used for analysis and metrology
- A light beam is reflected off of the sample of interest
- The light beam is then analyzed to see what the sample did to the light beam
- We then draw conclusions about the sample
  - thickness
  - optical constants
    - microstructure
- Model based
  - all measurement techniques are model based

# Polarized Light

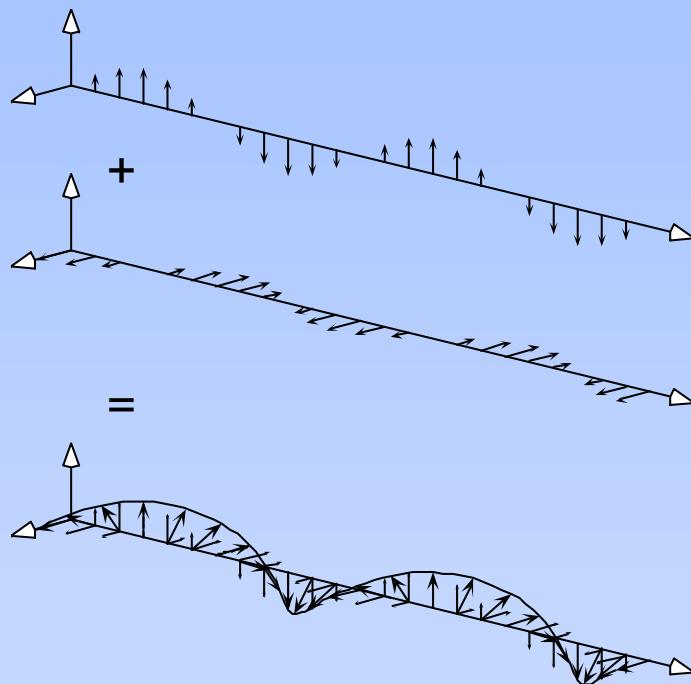
- The Name
  - “Ellipsometry” comes from “elliptically polarized light”
  - better name would be “polarimetry”

- Linearly Polarized
  - combining two light beams in phase, gives *linearly polarized light*



## Polarized Light (continued)

- Elliptically Polarized
  - combining two light beams out of phase, gives *elliptically polarized light*
- Two ways
  - pass through a retarder
  - reflect off a surface
    - absorbing material
    - substrate with film



# Laws of Reflection and Refraction

- Reflection

$$\phi_i = \phi_r$$

- Refraction (Snell's law)

- for dielectric, i.e.  $k = 0$

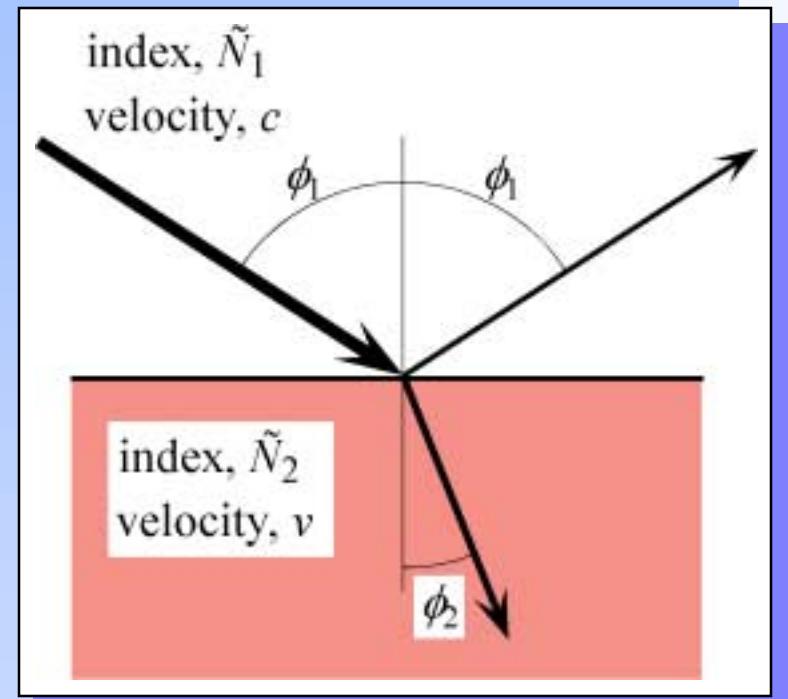
$$n_1 \sin \phi_1 = n_2 \sin \phi_2$$

- in general

$$\tilde{N}_1 \sin \phi_1 = \tilde{N}_2 \sin \phi_2$$

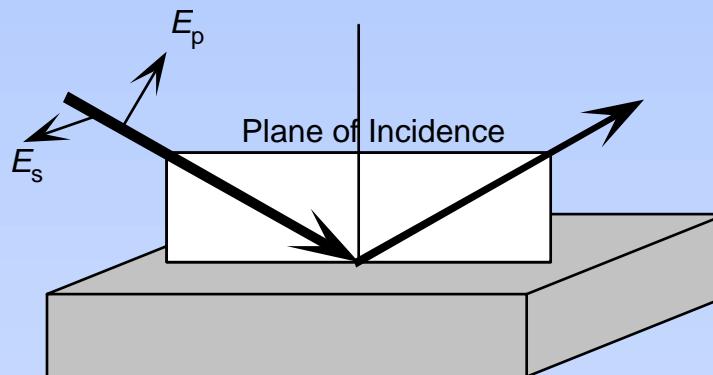
- sine function is complex
- corresponding complex cosine function

$$\sin^2 \phi_2 + \cos^2 \phi_2 = 1$$



# Reflections (orientation)

- Electric Field Vector
- Plane-of-Incidence
  - incoming
  - normal
  - outgoing
- s-waves and p-waves
  - “senkrecht” and “parallel”



# Equations of Fresnel

- Fresnel reflection coefficients,  $r_{12}^p$      $r_{12}^s$ 
  - complex numbers
- ratio of Amplitude of outgoing to incoming
- different for p-waves and s-waves

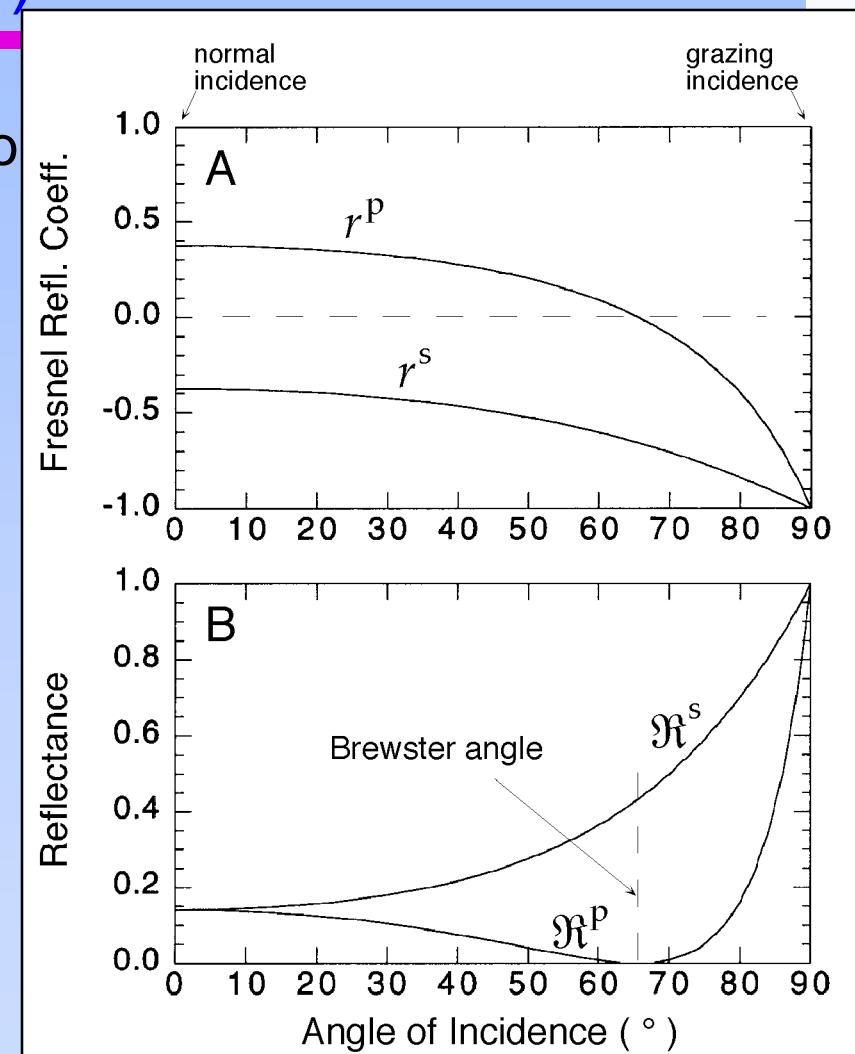
$$r_{12}^p = \frac{\tilde{N}_2 \cos \phi_1 - \tilde{N}_1 \cos \phi_2}{\tilde{N}_2 \cos \phi_1 + \tilde{N}_1 \cos \phi_2} \quad r_{12}^s = \frac{\tilde{N}_1 \cos \phi_1 - \tilde{N}_2 \cos \phi_2}{\tilde{N}_1 \cos \phi_1 + \tilde{N}_2 \cos \phi_2}$$

- Reflectance  $\mathfrak{R}$ 
  - ratio of Intensity
  - square of Amplitude
  - for a single interface

$$\mathfrak{R}^p = |r_{12}^p|^2 \quad \mathfrak{R}^s = |r_{12}^s|^2$$

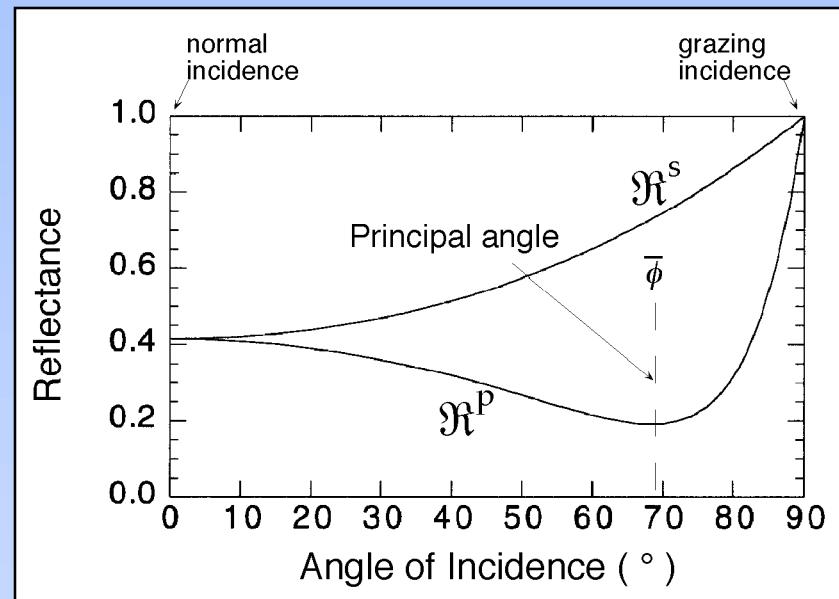
# Brewster Angle (for dielectrics)

- $r^s$  always negative and non-zero
- $r^p$  passes through zero
- $\Re^p$  goes to zero
- The Brewster Angle
  - sometimes called the principal angle, polarizing angle
- Reflected light is s-polarized
- ramifications
  - $\tan \phi_B = \frac{n_2}{n_1}$
  - $\cos \phi_2 = \sin \phi_B$



## “Brewster” Angle, for metals

- if  $k$  is non-zero,  $r^s$  and  $r^p$  are complex
- cannot plot  $r^s$  and  $r^p$  vs angle of incidence
- However, we can still plot the Reflectance
- $\Re^p$  has a minimum, although not zero
- Actually called the “principal angle”

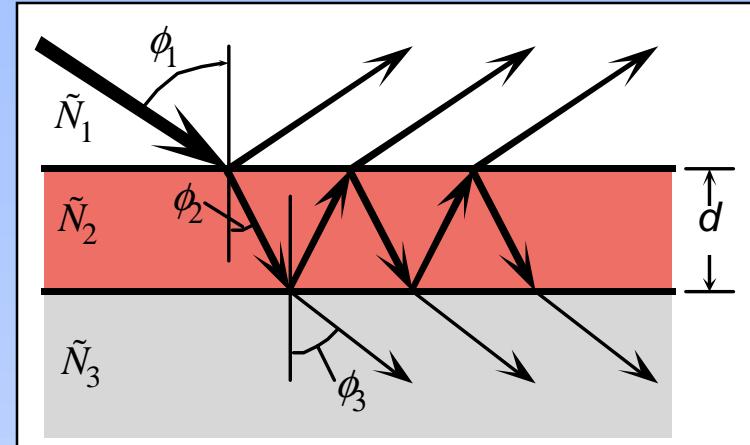


# Reflections with Films

- Ellipsometry,
  - Amplitude, phase of outgoing vs incoming
- Reflectometry
  - Intensity of outgoing vs incoming
- Total Reflection Coefficient
  - corresponds to Fresnel Coefficients
  - complex number

$$R^p = \frac{r_{12}^p + r_{23}^p \exp(-j2\beta)}{1 + r_{12}^p r_{23}^p \exp(-j2\beta)}$$

- $\beta$  is phase change from top to bottom of film



$$R^s = \frac{r_{12}^s + r_{23}^s \exp(-j2\beta)}{1 + r_{12}^s r_{23}^s \exp(-j2\beta)}$$

$$\beta = 2\pi \left( \frac{d}{\lambda} \right) \tilde{N}_2 \cos \phi_2$$

# Ellipsometry and Reflectometry definitions

- Reflectance  $\Re^p = |R^p|^2 \quad \Re^s = |R^s|^2$
- Delta, the phase difference induced by the reflection
  - if  $\delta_1$  is the phase difference before, and  $\delta_2$  the phase difference after the reflection then  $\Delta = \delta_1 - \delta_2$
  - ranges from zero to  $360^\circ$  (or  $-180$  to  $+180^\circ$ )
- Psi, the ratio of the amplitude diminutions
  - ranges from zero to  $90^\circ$
- The Fundamental Equation of Ellipsometry

$$\tan \Psi = \frac{|R^p|}{|R^s|}$$

$$\rho = \frac{R^p}{R^s} \quad \rho = \tan \Psi e^{j\Delta}$$

$$\tan \Psi e^{j\Delta} = \frac{R^p}{R^s}$$

# More Perspective

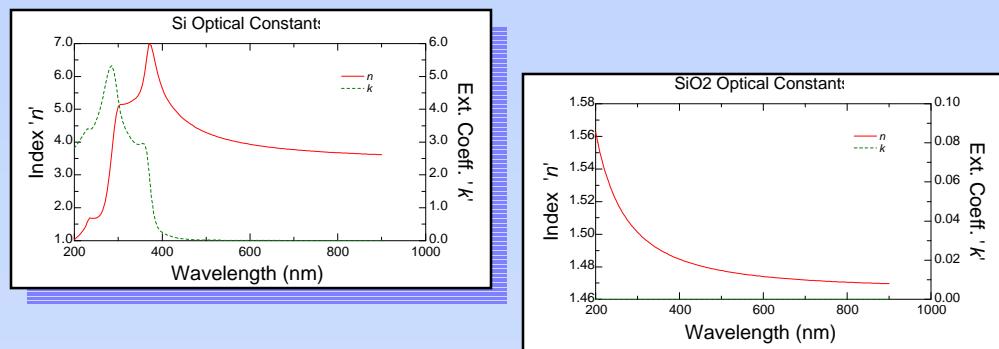
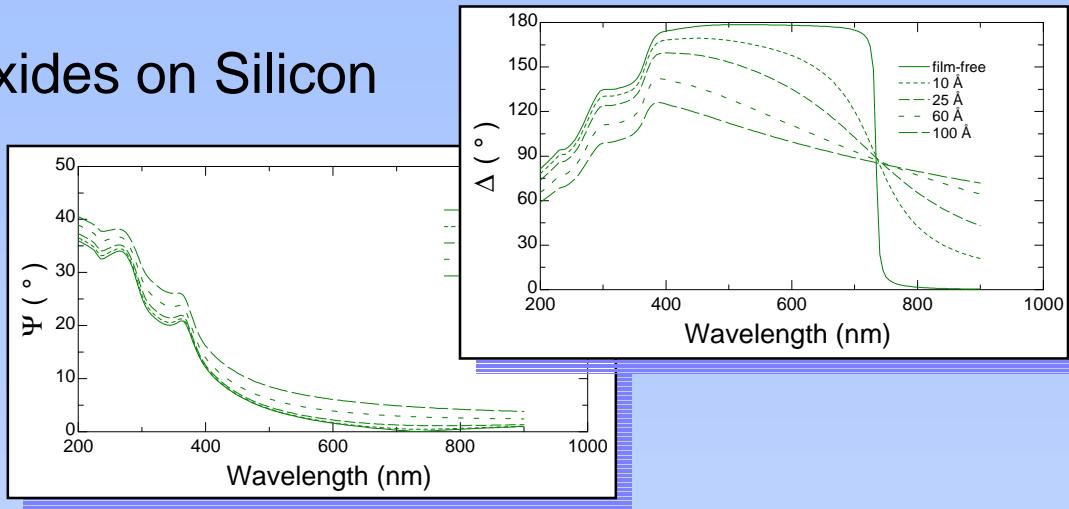
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- Ellipsometers measure  $\Delta$  and  $\Psi$  (sometimes only  $\cos \Delta$ )
  - Properties of the probing beam
- Quantities such as thickness and index of refraction are calculated quantities, based on a model.
  - Properties of the sample
- Values of  $\Delta$  and  $\Psi$  are always correct
- Whether thickness and index are correct depend on the model
- Both precision and accuracy for  $\Delta$  and  $\Psi$
- Precision for thickness
- Accuracy, ???

# The Anatomy of an Ellipsometric Spectrum

## Examples

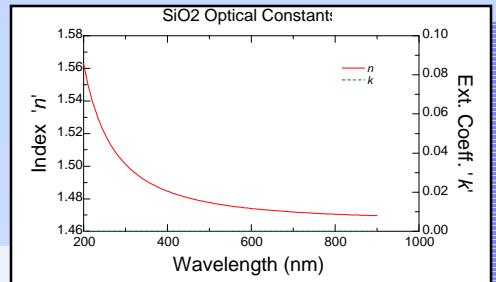
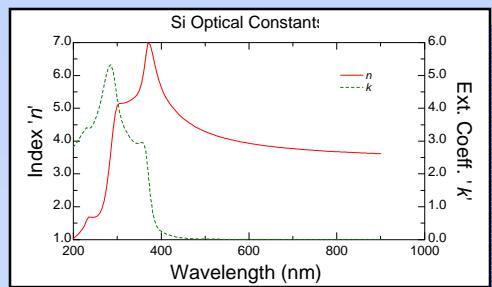
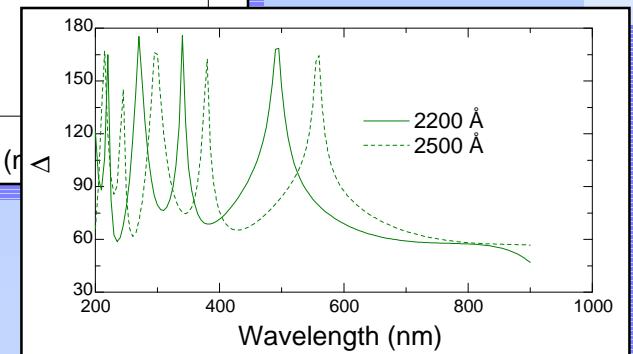
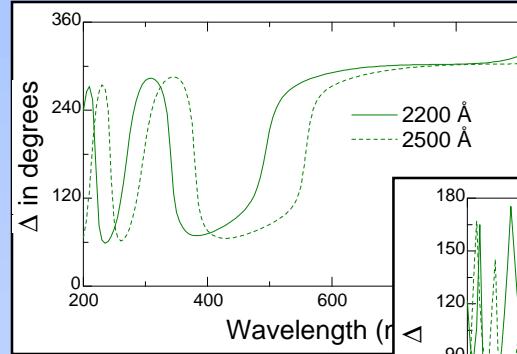
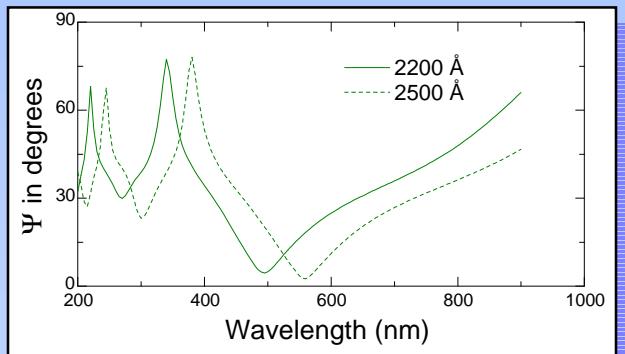
- Thin oxides on Silicon



# The Anatomy of an Ellipsometric Spectrum

## Examples

- Thicker oxide on Silicon

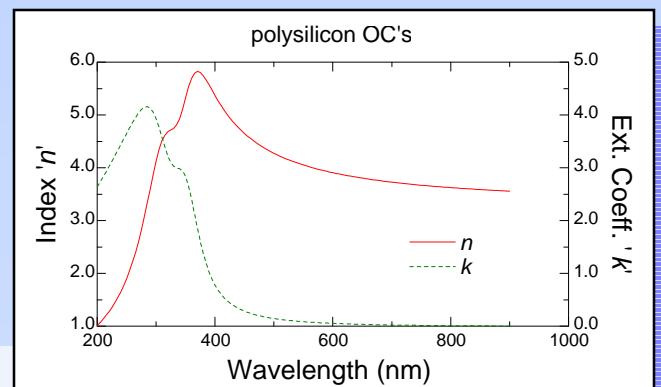
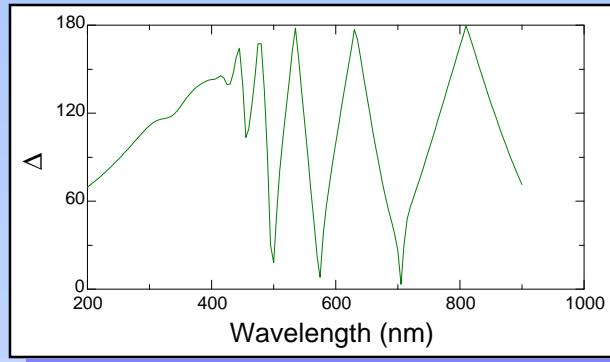
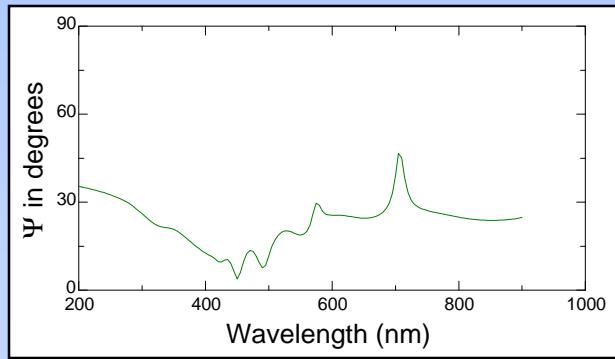


# The Anatomy of an Ellipsometric Spectrum

## Examples

- Polysilicon on oxide on silicon

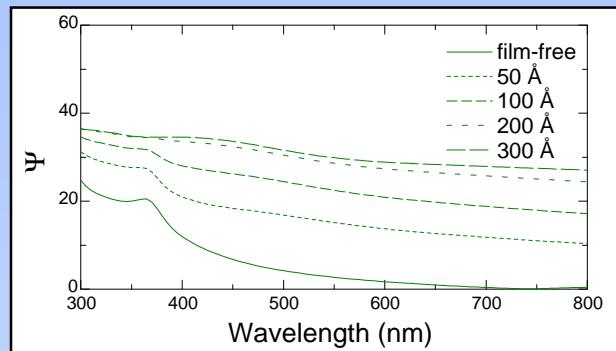
3 srough	25 Å
2 polysilicon	3000 Å
1 sio2	1000 Å
0 si	1 mm



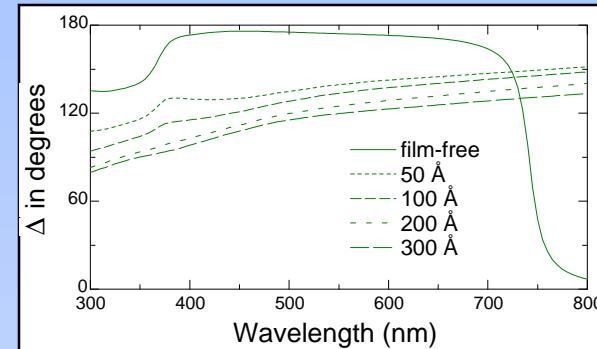
# The Anatomy of an Ellipsometric Spectrum

## Examples

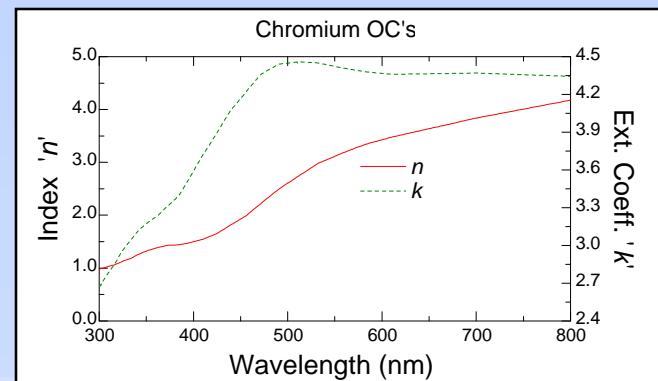
- Thin chromium on silicon



1	cr	300 Å
0	si	1 mm



- caveats



# Analysis of an Ellipsometric Spectrum

## Determining Film properties from SE spectra

- Except for substrates, we cannot do a direct calculation

What Ellipsometry Measures:

Psi ( $\Psi$ )  
Delta ( $\Delta$ )

What we are interested in:

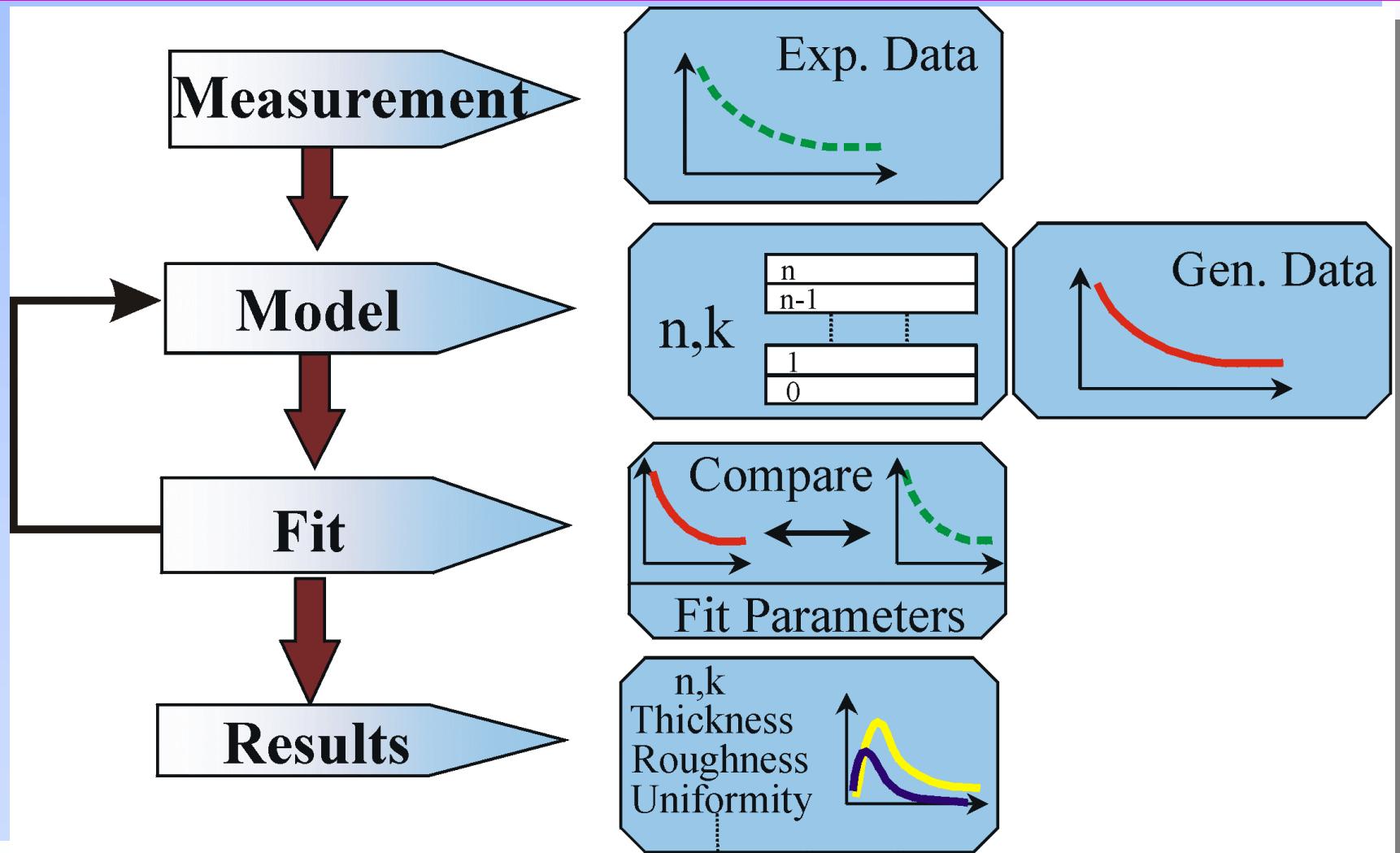
Film Thickness  
Refractive Index  
Surface Roughness  
Interfacial Regions  
Composition  
Crystallinity  
Anisotropy  
Uniformity

Desired information must be extracted  
Through a model-based analysis using  
equations to describe interaction of  
light and materials



# Analysis of an Ellipsometric Spectrum

## How we analyze data:



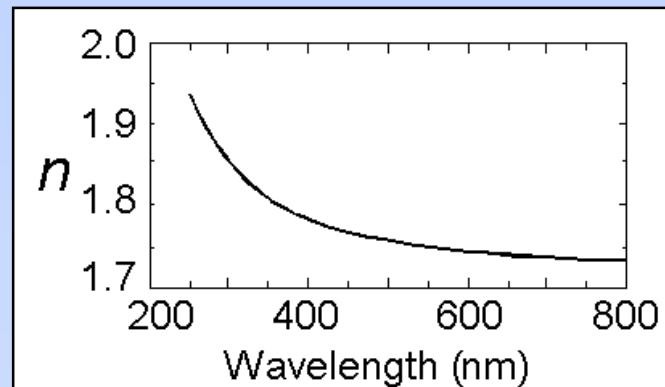


# Analysis of an Ellipsometric Spectrum

## Building the model

- Optical Constants
  - Tabulated list
    - when OC's are very well known
    - single-crystal
    - thermal oxide of Si, LPCVD nitride
  - Dispersion Equation
    - Cauchy equation
      - dielectrics, primarily
      - empirical
      - not K-K consistent

$$n(\lambda) = A_n + \frac{B_n}{\lambda^2} + \frac{C_n}{\lambda^4}$$

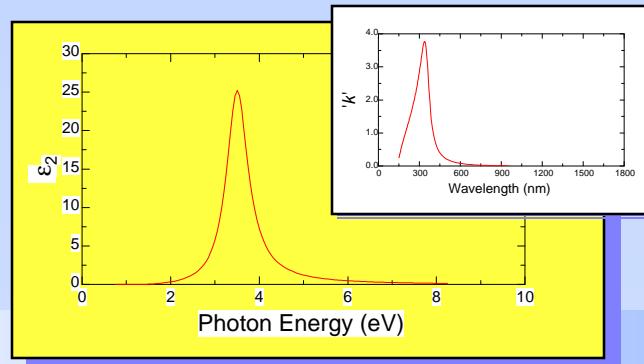
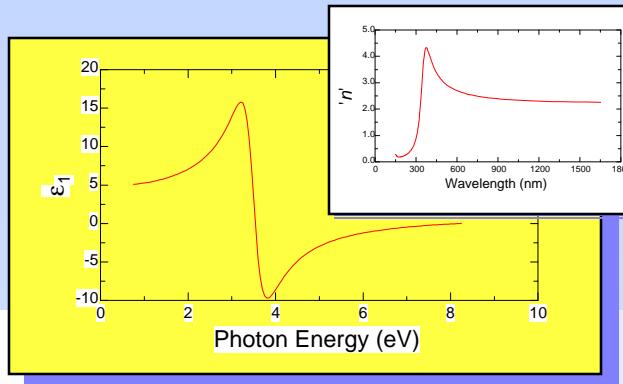
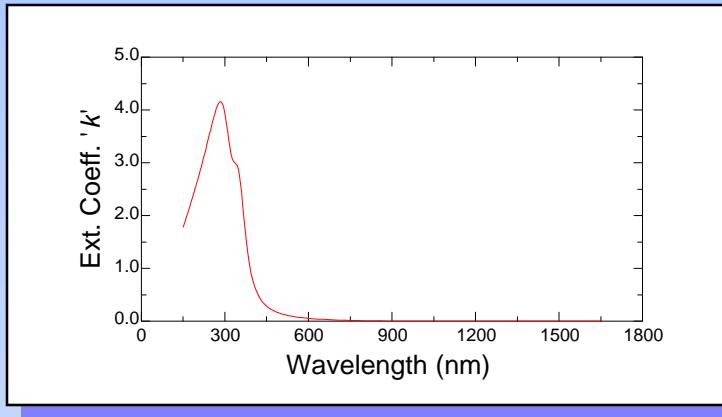
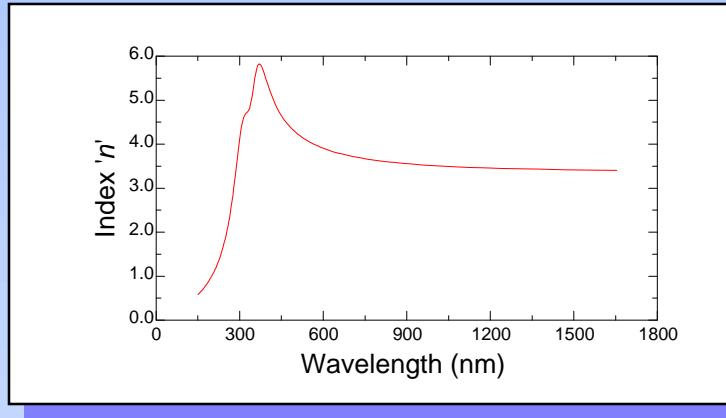


# Analysis of an Ellipsometric Spectrum

## Building the model

- Optical Constants
  - Dispersion Equation
    - Oscillator equation

2	polysilicon	0 Å
1	sio2	1000 Å
0	si	1 mm



# Analysis of an Ellipsometric Spectrum

## Building the model

- Optical Constants
  - Mixture
    - EMA, effective medium approximation

3	srough	0 Å
2	polysilicon	2000 Å
1	sio2	1000 Å
0	si	1 mm

- Graded Layers
- Anisotropic Layers
- Superlattice



# Analysis of an Ellipsometric Spectrum

## Building the model

- Seed Values
  - Thickness
    - process engineer's guess
    - analyst's guess
    - trial-and-error
      - till it looks good
  - Cauchy coefficients
    - $A_n$  between ~ 1.4 and 2.2
    - higher for poly or a\_Si
  - Oscillators
    - tough
    - "GenOsc" formalism

A wise old sage once said:

“The best way to solve a problem is to have solved one just like it yesterday.”

# Analysis of an Ellipsometric Spectrum

## The regression process

- Don't turn all the variables loose to begin with
  - e.g. for a Cauchy
    - thickness first
    - then  $A_n$  and thickness
    - then include  $B_n$
    - add in extinction coefficient
- For a stack
  - don't try to determine thicknesses and OC's simultaneously
    - creative deposition
- “done” is a relative term
  - does it make sense



A wise old sage once said:

“You *can* have it all, you just can’t have it all at once.”



## What you can do, and what you can't do

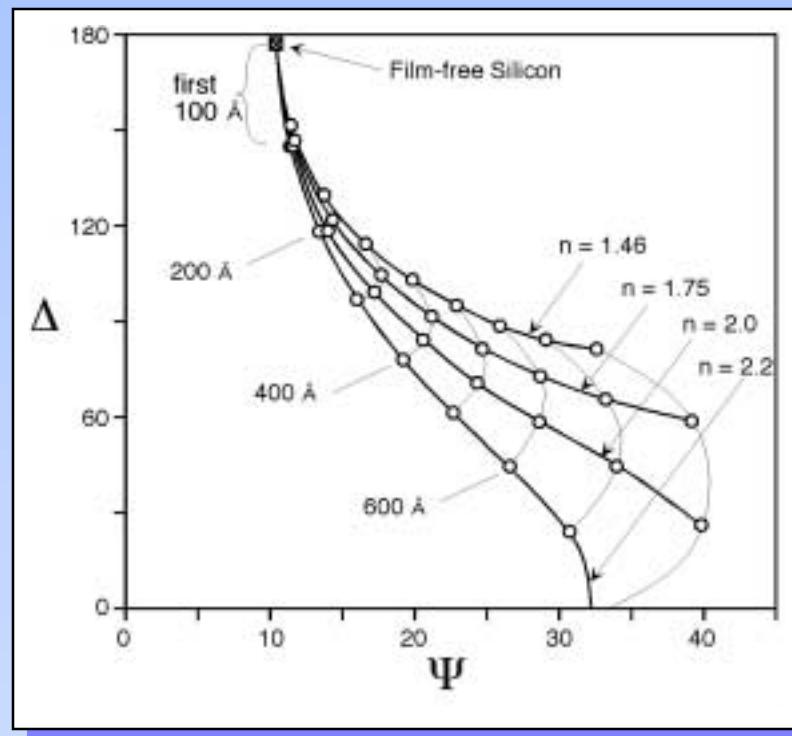
### Requirements

- plane parallel interfaces
  - roughness
- film must be uniform
  - graded layers
  - anisotropic layers
- multilayers
  - need to know something about OC's
- coherence
  - patterned wafers
  - non-uniform thickness
  - macroscopic roughness
- helps if the film-of-interest is on top
- optical contrast
  - polymer on glass

## What you can do, and what you can't do

### Optical Constants of Very Thin Films

- consider a single wavelength (632.8 nm) at 70°
- oxynitride on silicon
- Delta/Psi trajectories
- below 100Å, very difficult to determine index,  $n$ 
  - distinguishing one material from another
  - determining thicknesses in a stack
    - e.g., ONO
- however, if you're willing to assume  $n$ , can determine thickness of very thin film
  - classic experiment of Archer
  - how far can you be off?



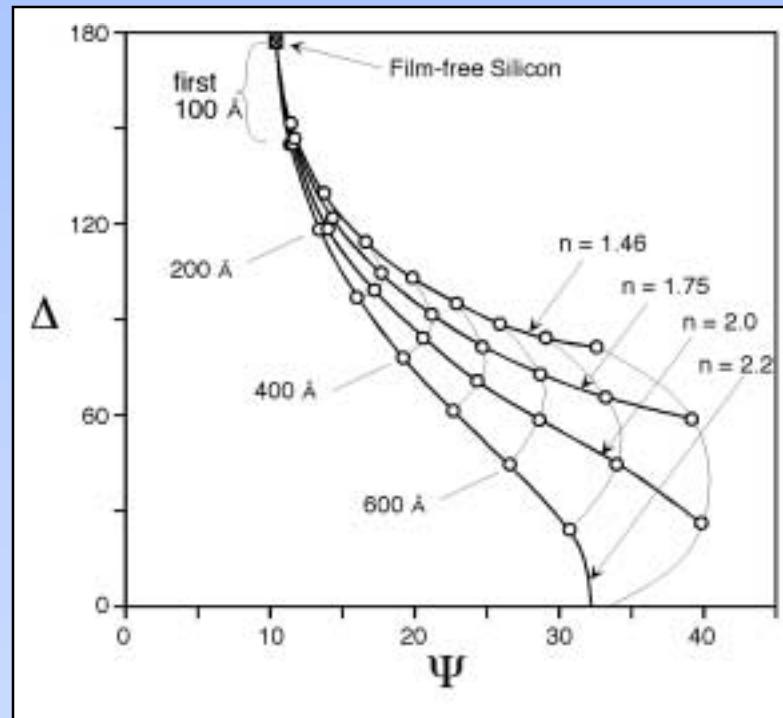


## What you can do, and what you can't do

### Optical Constants of Very Thin Films

making it better ➔ directions

- DUV or VUV
  - shorter wavelengths
  - extinction coefficient often nonzero
- IR
  - absorption bands are different for different materials



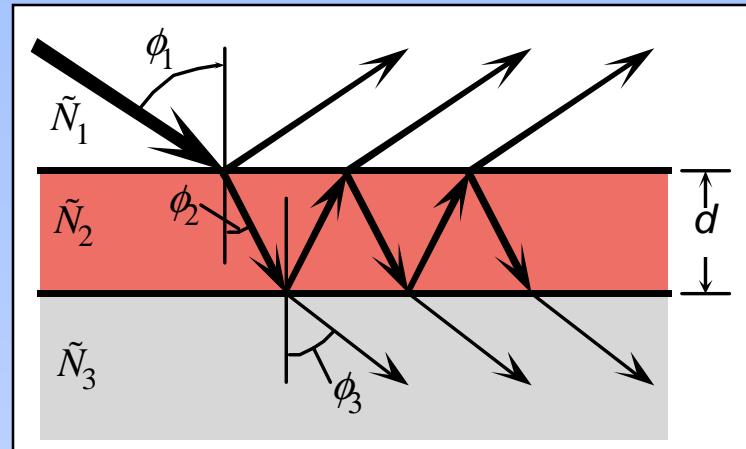


## What you can do, and what you can't do

# Optical Constants of Very Thin Films

### Fundamental Limitation

- Our ability to make films with:
  - plane parallel interfaces
  - uniformity





## Acknowledgements

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