



APS Mid-Atlantic Senior Physicists Group

Supersymmetry

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SYMMETRY PRINCIPLES IN SELECTED
PROBLEMS OF FIELD THEORY

by

SYLVESTER JAMES GATES, JR.

B.S., Massachusetts Institute of Technology
(June 1973)

B.S., Massachusetts Institute of Technology
(September 1973)

SUBMITTED IN PARTIAL FULFILLMENT
OF THE REQUIREMENTS FOR THE
DEGREE OF

DOCTOR OF PHILOSOPHY

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY
(June 1977)

$$\text{————— } M_{F^0}^2 \cong g^2 M_G^2 \left[d^2 + \frac{1}{2} (1 + \frac{1}{2} \alpha^2) \right]$$

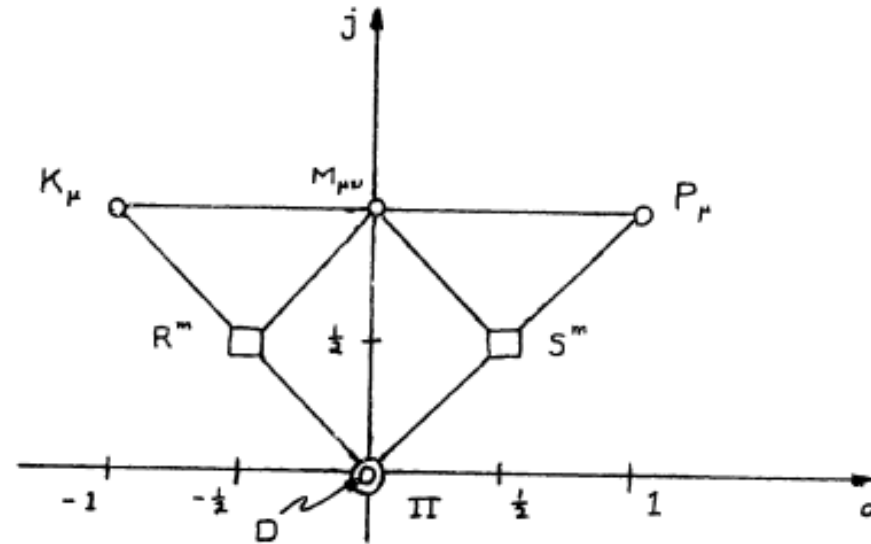
$$\text{————— } M_{F^{\pm}}^2 \cong g^2 M_G^2 \left(\frac{1}{\alpha} \right)^2$$

$$\text{————— } M_{G^0}^2 \cong g^2 M_G^2 \left[b^2 + \frac{5}{18} (1 + \frac{1}{2} \alpha^2) \right]$$

$$\text{————— } M_{Z^0}^2 \cong 5 g^2 M_G^2 \left(1 + \frac{1}{2} \alpha^2 \right)$$

$$\text{————— } M_{W^{\pm}}^2 \cong g^2 M_G^2 \left(1 + \frac{1}{2} \alpha^2 \right)$$


$$\text{————— } M_A^2$$



○ ≡ Bosonic generator

□ ≡ Fermionic generator

Diagram illustrating the generators of the superconformal group. The classification of these operators has been made according to intrinsic spin and dimensionality.



Superstring Theory: The DNA of Reality

Web:

<http://www.teach12.com/ttcx/coursedesclong2.aspx?cid=1284>

One Theorist's Bucket List

- (a.) Higgs Boson
- (b.) Gravitational Waves
- (c.) Superpartners
- (d.) Evidence of Superstrings

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From The
SM To The
With Higgs

The Standard Model (SM)

FERMIONS

matter constituents
spin = 1/2, 3/2, 5/2, ...

Leptons spin = 1/2		
Flavor	Mass GeV/c ²	Electric charge
ν_e electron neutrino	$<1 \times 10^{-8}$	0
e electron	0.000511	-1
ν_μ muon neutrino	<0.0002	0
μ muon	0.106	-1
ν_τ tau neutrino	<0.02	0
τ tau	1.7771	-1

Quarks spin = 1/2		
Flavor	Approx. Mass GeV/c ²	Electric charge
u up	0.003	2/3
d down	0.006	-1/3
c charm	1.3	2/3
s strange	0.1	-1/3
t top	175	2/3
b bottom	4.3	-1/3

BOSONS

force carriers
spin = 0, 1, 2, ...

Unified Electroweak spin = 1		
Name	Mass GeV/c ²	Electric charge
γ photon	0	0
W^-	80.4	-1
W^+	80.4	+1
Z^0	91.187	0

Strong (color) spin = 1		
Name	Mass GeV/c ²	Electric charge
g gluon	0	0

PROPERTIES OF THE INTERACTIONS

Property \ Interaction	Gravitational	Weak	Electromagnetic	Strong	
		(Electroweak)		Fundamental	Residual
Acts on:	Mass - Energy	Flavor	Electric Charge	Color Charge	See Residual Strong Interaction Note
Particles experiencing:	All	Quarks, Leptons	Electrically charged	Quarks, Gluons	Hadrons
Particles mediating:	Graviton (not yet observed)	W^+ W^- Z^0	γ	Gluons	Mesons
Strength relative to electromag for two u quarks at:	10^{-41}	0.8	1	25	Not applicable to quarks
for two protons in nucleus	10^{-41}	10^{-4}	1	60	Not applicable to hadrons
	10^{-36}	10^{-7}	1	Not applicable to hadrons	20

The Standard Model (SM)

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BOSONS

force carriers
spin = 0, 1, 2, ...

Unified Electroweak spin = 1		
Name	Mass GeV/c ²	Electric charge
γ photon	0	0
W^-	80.4	-1
W^+	80.4	+1
Z^0	91.187	0
H^0	125	0

Strong (color) spin = 1		
Name	Mass GeV/c ²	Electric charge
g gluon	0	0

PROPERTIES OF THE INTERACTIONS

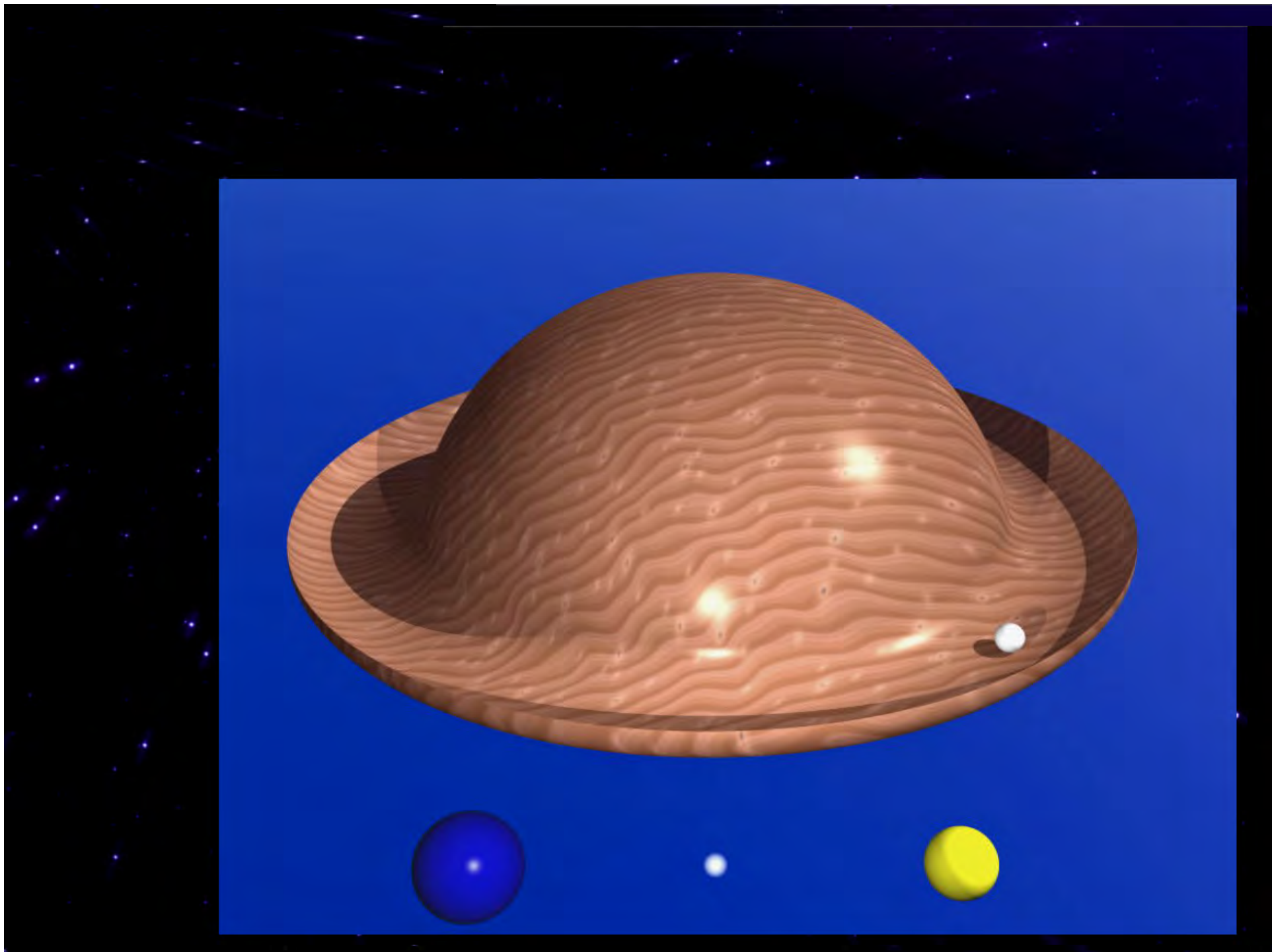
Property \ Interaction	Gravitational	Weak	Electromagnetic	Strong	
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The Higgs
And
The LHC

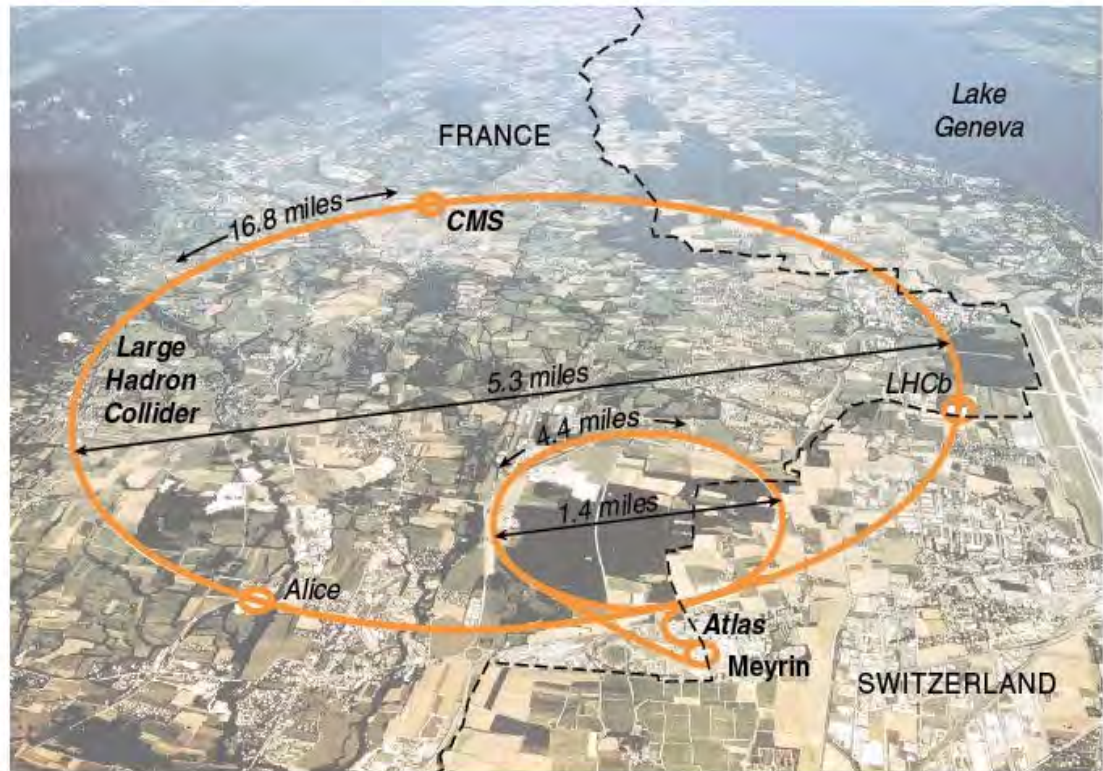
Higgs, Carrier Mass & Goldstone Bosons





The Large Hadron Collider of Cern (European Organization for Nuclear Research)

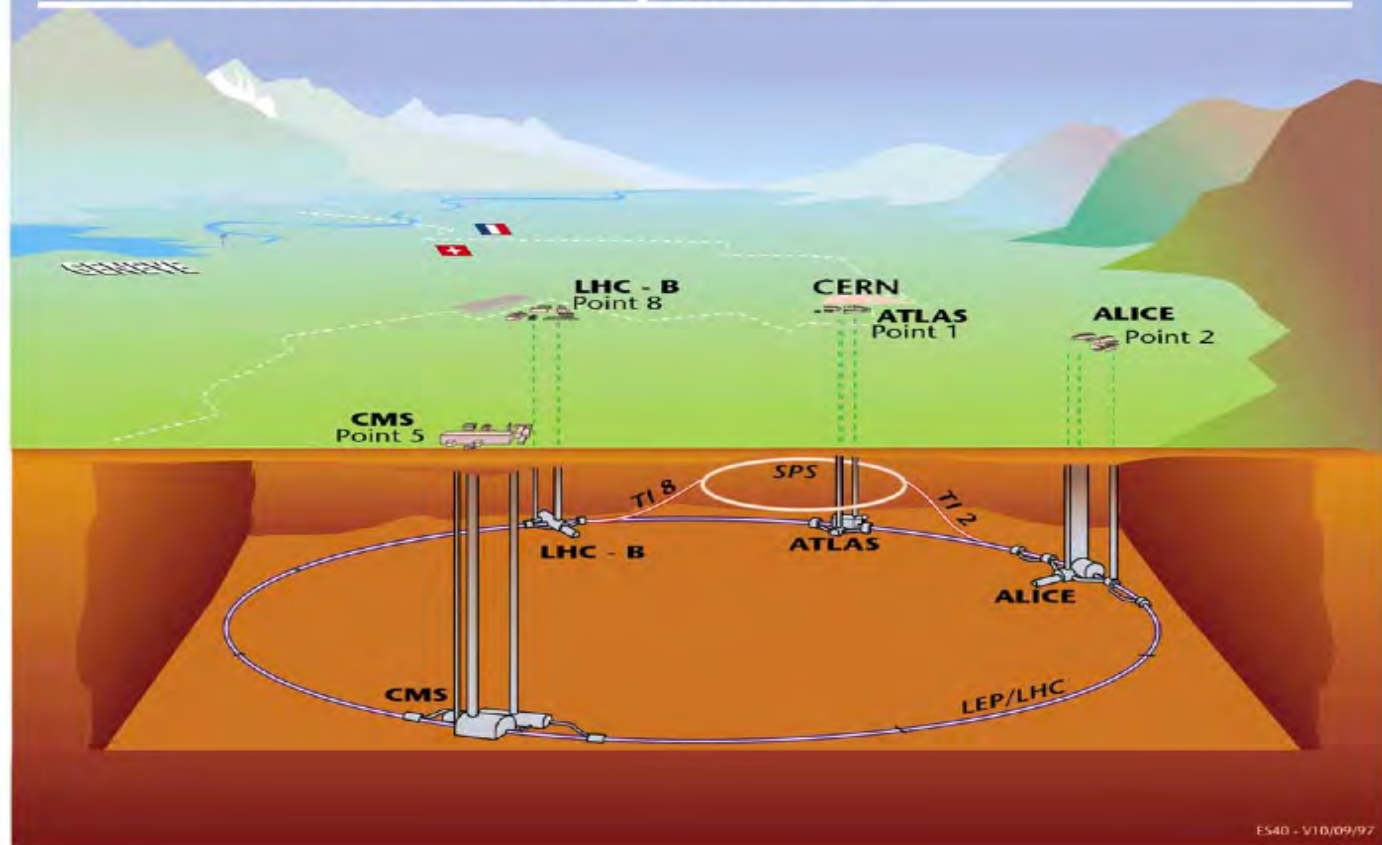
In a tunnel 300 feet below Switzerland and France, scientists are putting the final touches on a 16.8-mile long particle accelerator that will smash protons together in an attempt to create forces and particles that existed shortly after the Big Bang and rarely, if ever, today.



Source: Cern; Physics World, Sept. 2004; Lawrence Berkeley National Laboratory

Graham Roberts, David Constantine, Mika Gröndahl, Erin Aigner/ The New York Times

Overall view of the LHC experiments.

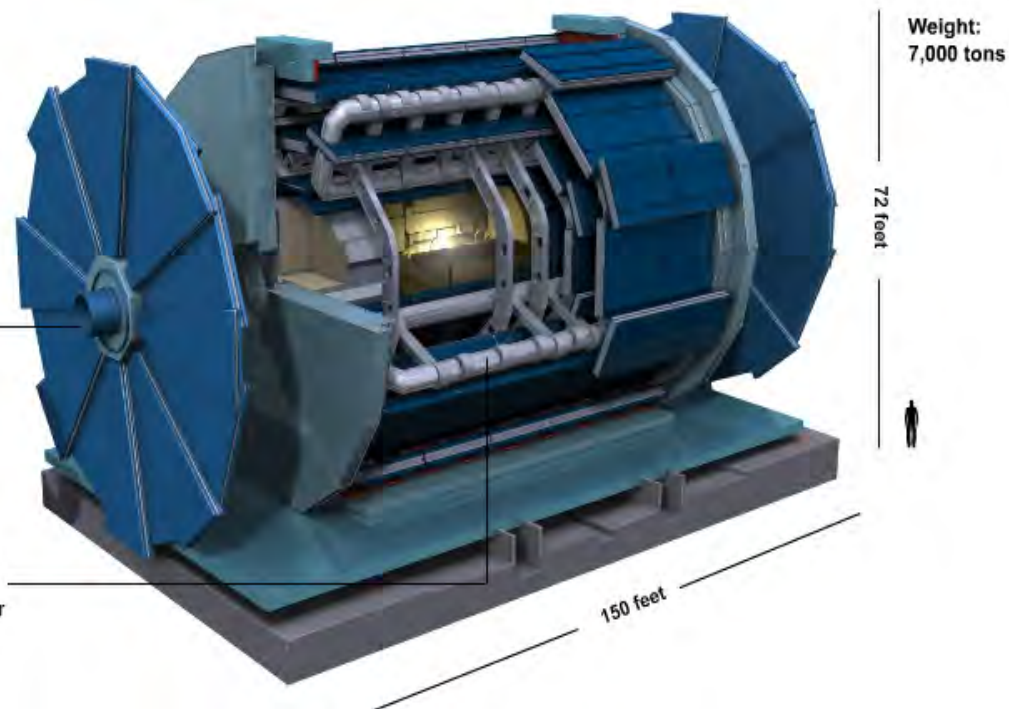


Atlas

The second of two large particle physics detectors, it will also go online in the summer of 2008. Approximately 1,800 people from 34 countries and 150 institutes took part in the collaboration. The team is led by Peter Jenni of Cern.

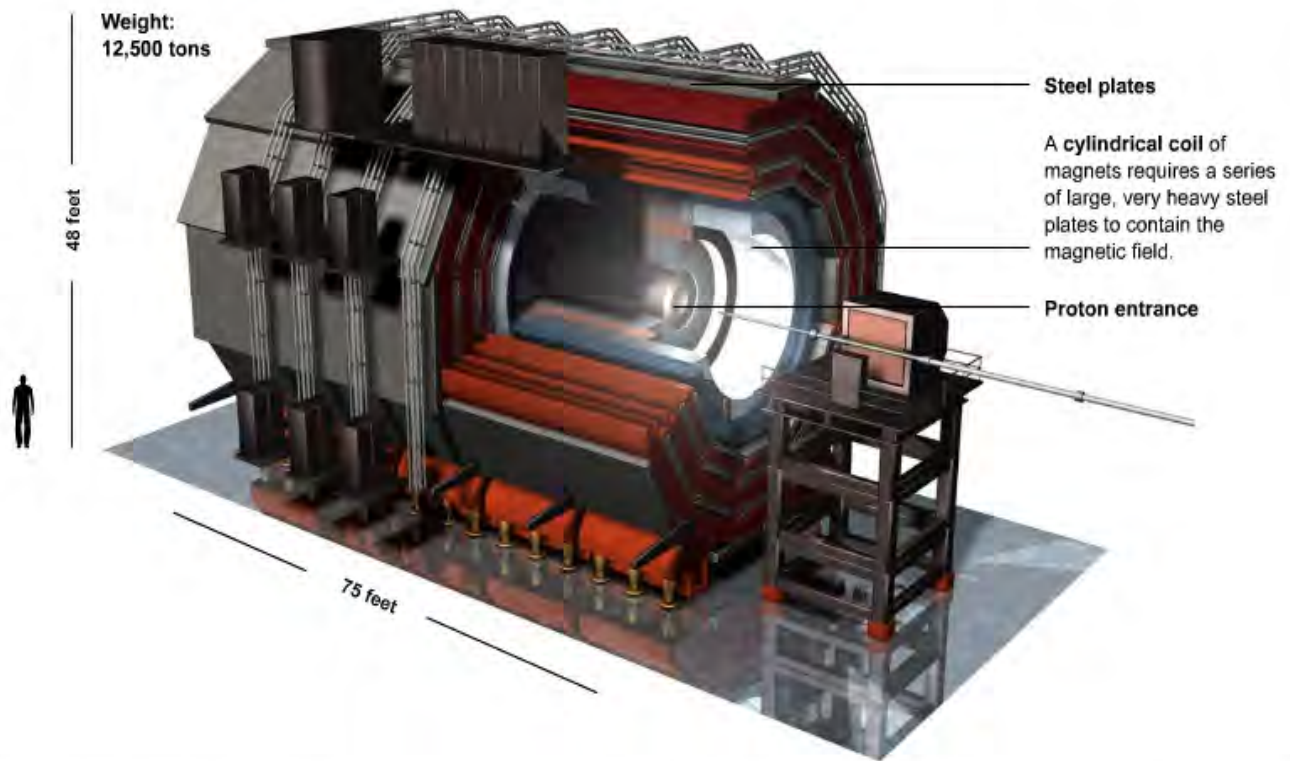
Proton entrance

Racetrack shaped magnets don't require steel yokes to contain the magnetic field, allowing the detector to be much larger and weigh less.

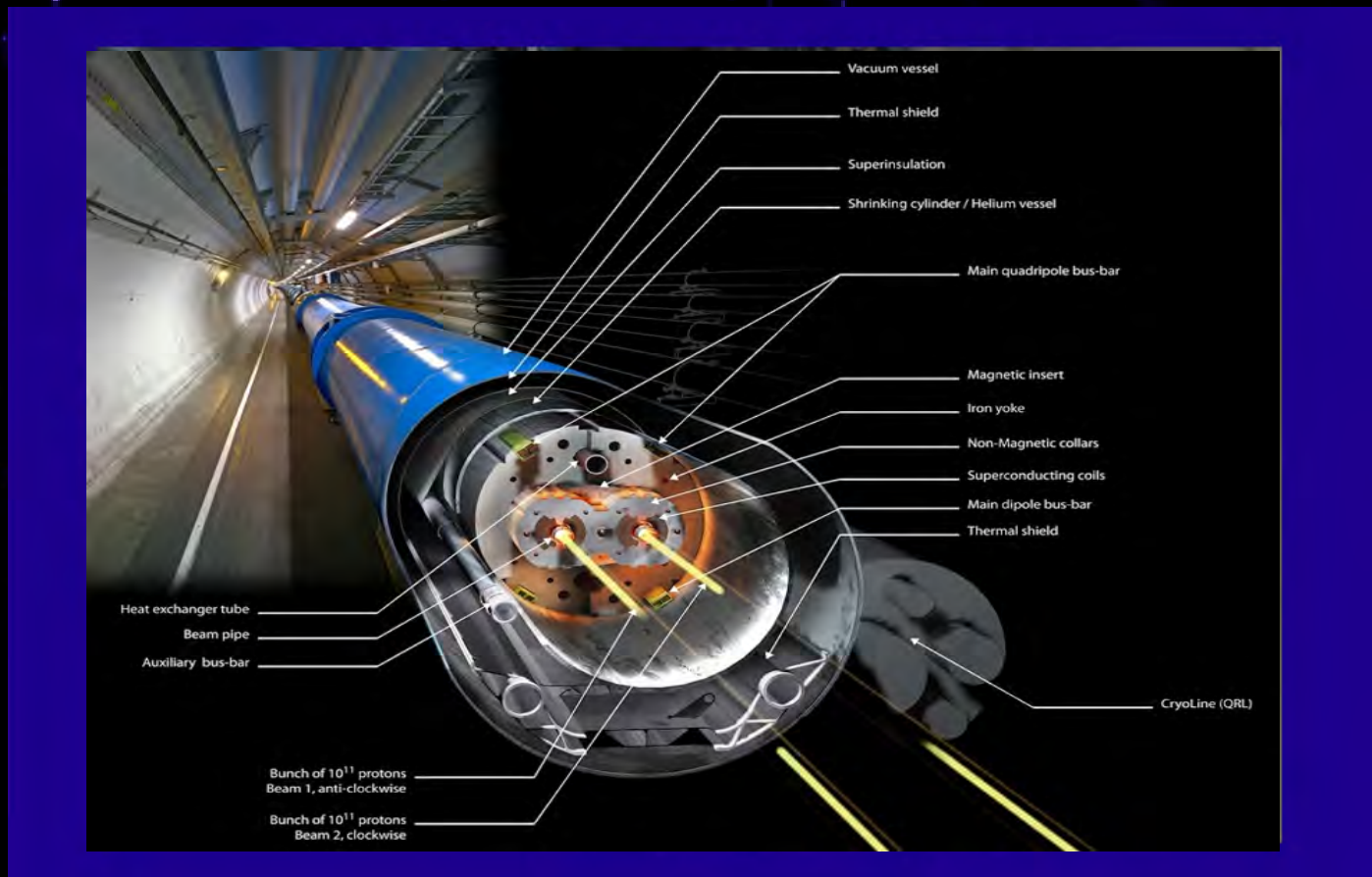


Compact Muon Solenoid (CMS)

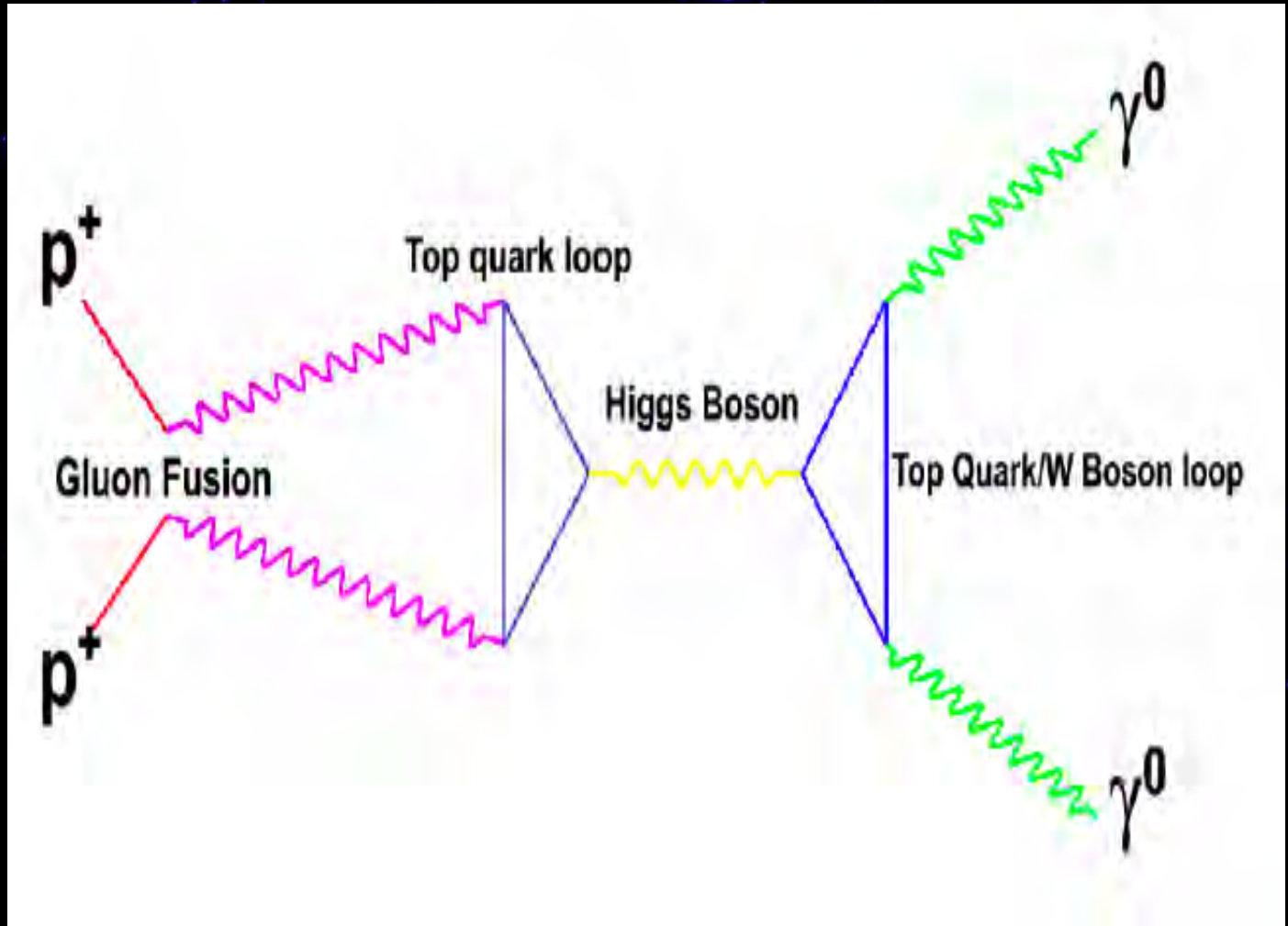
One of two large general-purpose particle physics detectors to go online in 2008. Approximately 2,500 people from 37 countries and 155 institutes form the collaboration building it. The team is led by Jim Virdee of Imperial College London and Cern.



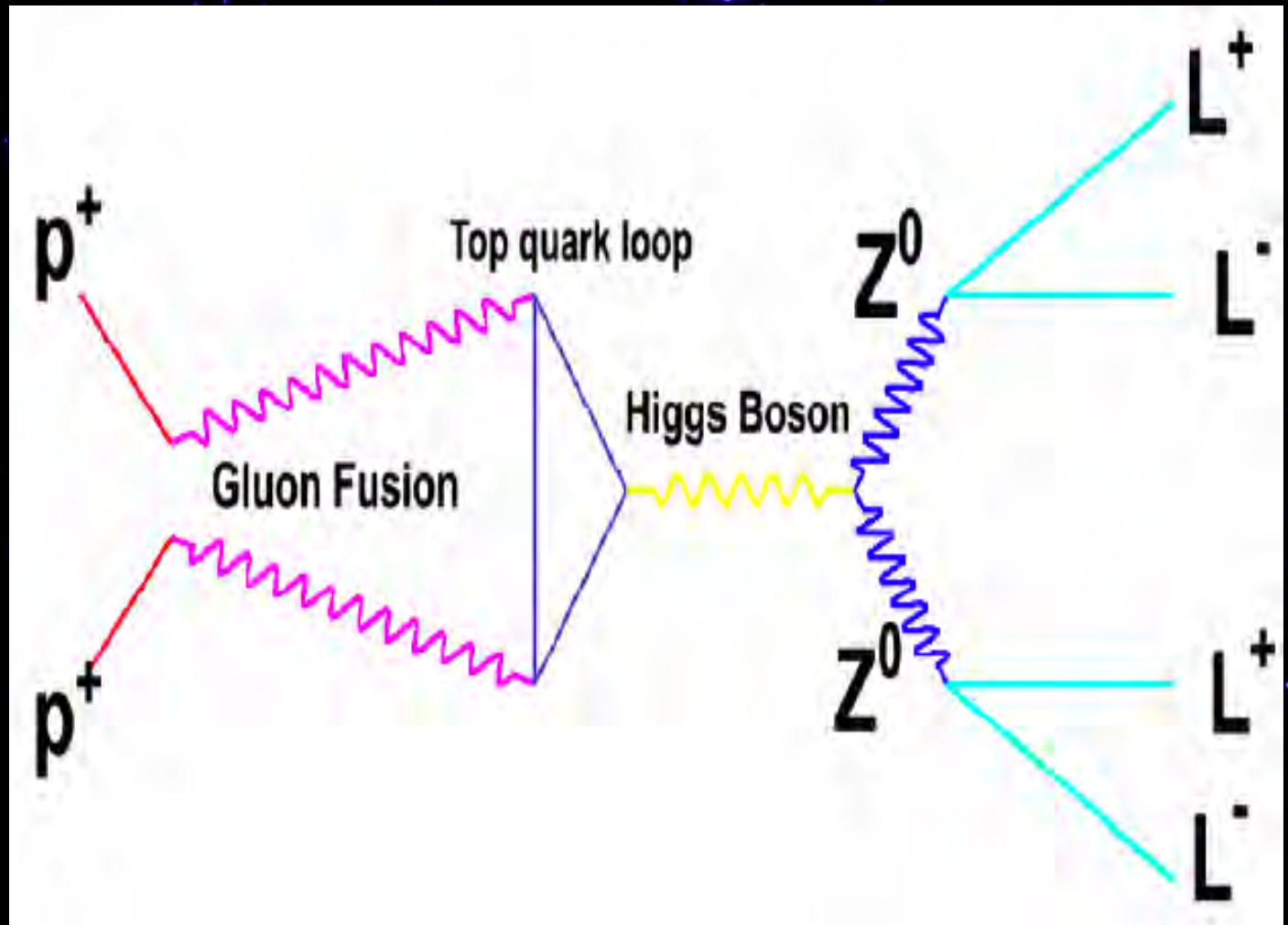
Overview of LHC Higgs Production Factory



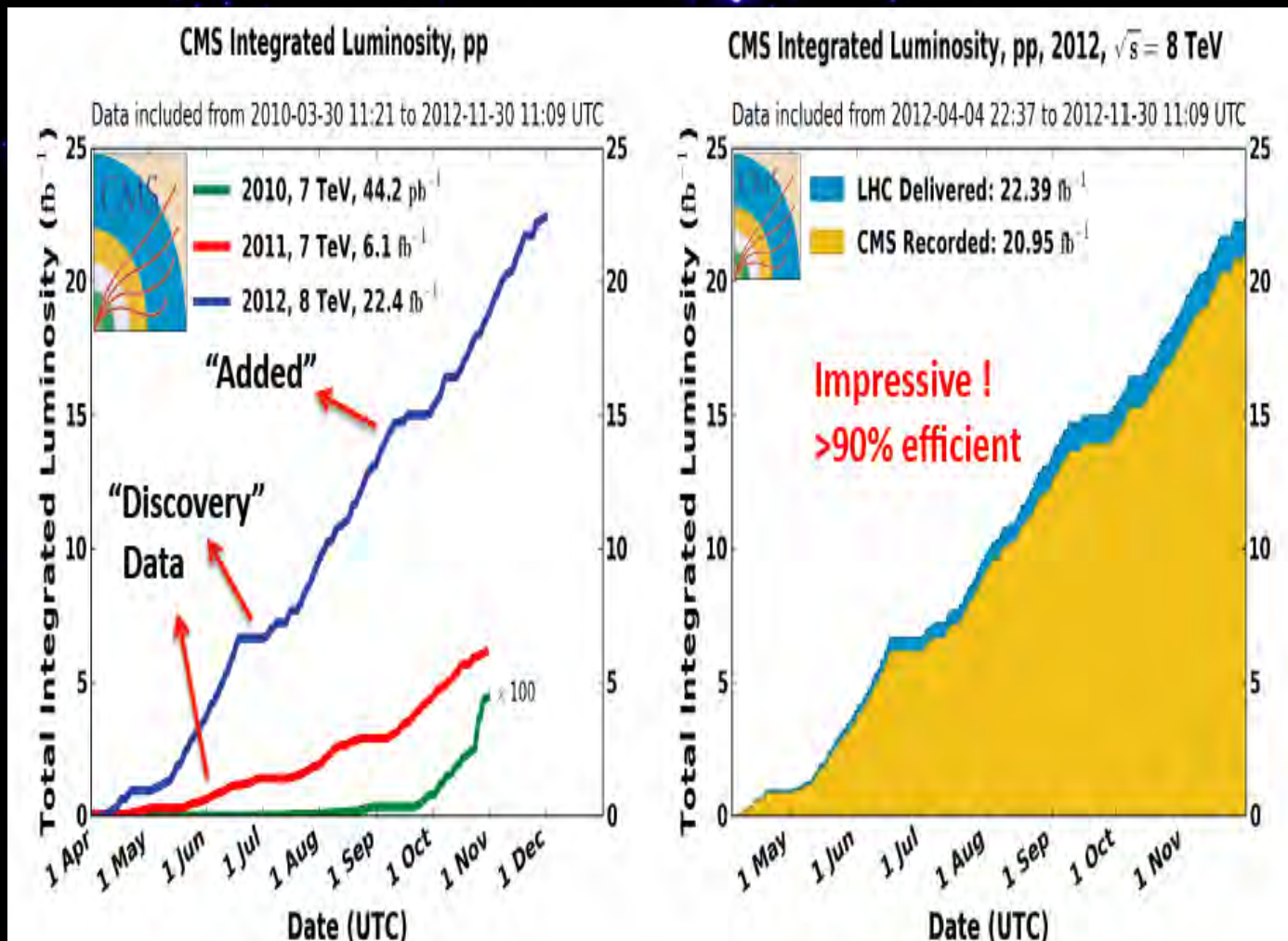
A Higgs Production & Decay Process



A Higgs Production & Decay Process



Productivity & Performance



‘Born’ On The Fourth of July

In 2012, there was an announcement of the discovery of a previously unknown boson where:

(a.) the ATLAS collaboration measured at a mass of $126.5 \text{ GeV}/c^2$
and

(b.) the CMS collaboration measured at a mass $125.3 \pm 0.6 \text{ GeV}/c^2$

and using both ‘channels’ this is a ‘five sigma’ event – i.e. less than a 1-in-a-million chance of error.



From: Rolf Heuer <rolf.heuer@cern.ch>

Date: 14 March 2013 11:29:54 AM SAST

To: "cern-personnel (CERN Personnel - Members and Associate Members)" <cern-personnel@cern.ch>

Subject: CERN Press Release: New results indicate that particle discovered at CERN is a Higgs boson

La version française sera disponible ultérieurement ici: <http://press.web.cern.ch/fr/press-releases>

New results indicate that particle discovered at CERN is a Higgs boson

Geneva, 14 March 2013. At the Moriond Conference today, the ATLAS and CMS collaborations at CERN's Large Hadron Collider (LHC) presented preliminary new results that further elucidate the particle discovered last year. Having analysed two and a half times more data than was available for the discovery announcement in July, they find that the new particle is looking more and more like a Higgs boson, the particle linked to the mechanism that gives mass to elementary particles. It remains an open question, however, whether this is the Higgs boson of the Standard Model of particle physics, **or possibly the lightest of several bosons** predicted in some theories that go beyond the Standard Model. Finding the answer to this question will take time.

Whether or not it is a Higgs boson is demonstrated by how it interacts with other particles, and its quantum properties. For example, a Higgs boson is postulated to have no spin, and in the Standard Model its parity – a measure of how its mirror image behaves – should be positive. CMS and ATLAS have compared a number of options for the spin-parity of this particle, and these all prefer no spin and positive parity. This, coupled with the measured interactions of the new particle with other particles, strongly indicates that it is a Higgs boson.



From The SM
To The
MSSM

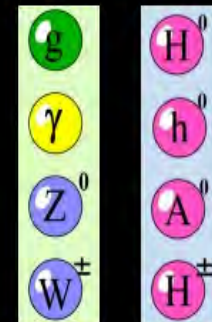
	FERMION	BOSON
ENERGY		
MATTER		

ENERGY

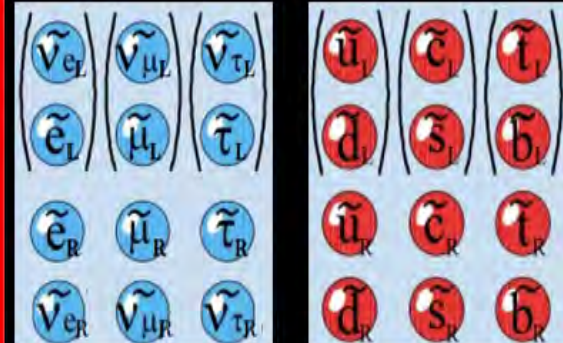
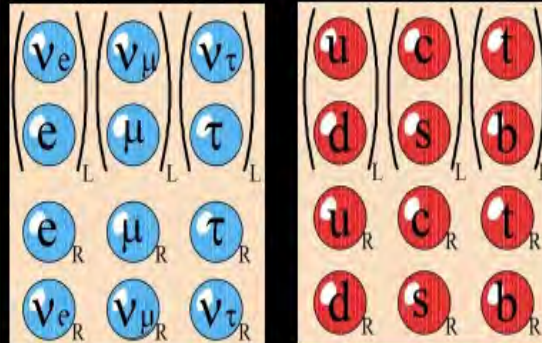
FERMION



BOSON



MATTER



Bohr 1913

$$|\vec{L}| = 2\pi\hbar n \quad .$$

Wilson-Sommerfeld 1916

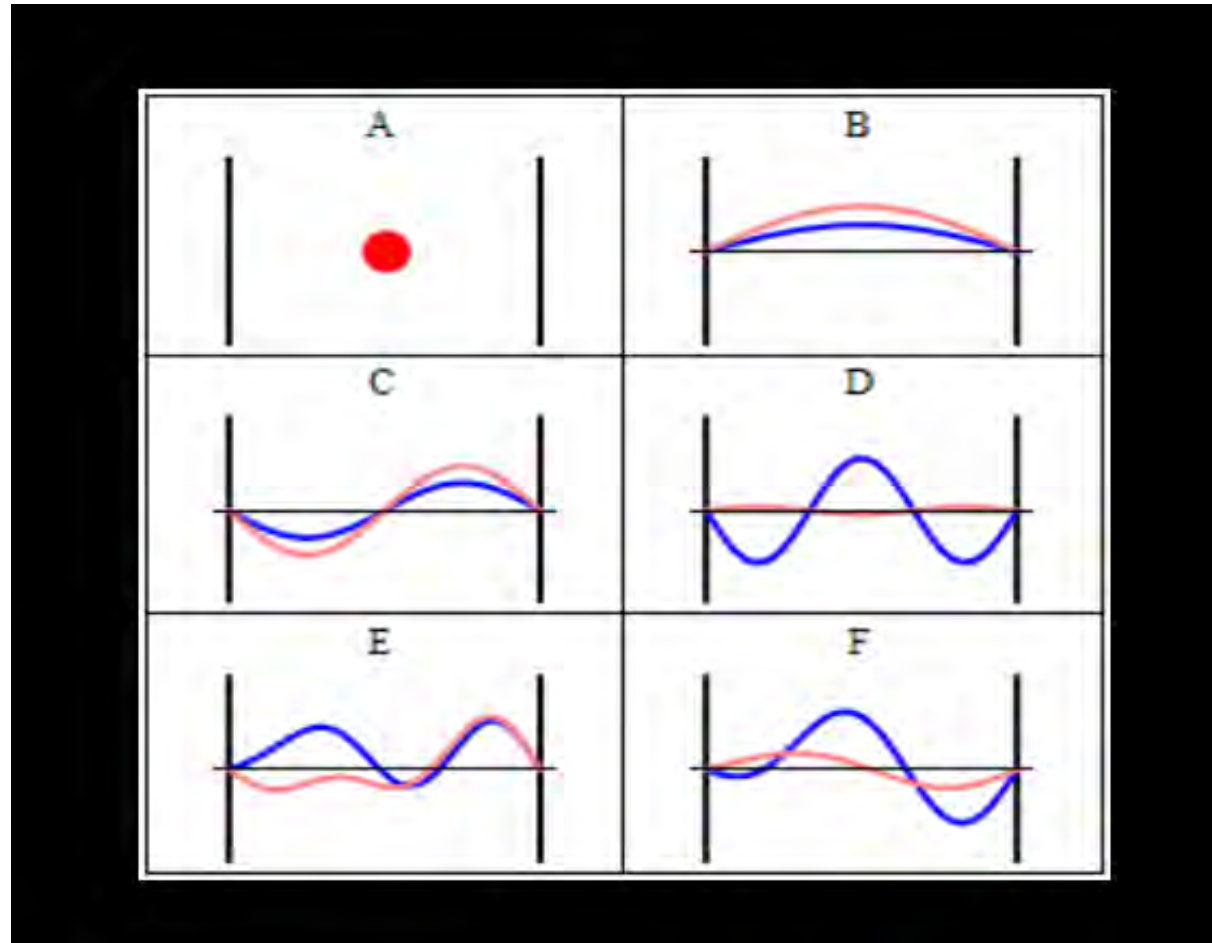
$$\int P dq = 2\pi\hbar n \quad .$$

de Broglie 1924

$$\vec{p} = \hbar \vec{k} \quad .$$

Schroedinger 1925

$$i\hbar \frac{\partial}{\partial t} \Psi = -\frac{\hbar^2}{2m} \nabla^2 \Psi + V(\vec{r}) \Psi$$



https://en.wikipedia.org/wiki/Particle_in_a_box#/media/File:InfiniteSquareWellAnimation.gif

Two Identical Particles In A Box

$$E_{n_1, n_2} = \frac{\hbar^2 \pi^2}{2 M_0 L^2} [n_1^2 + n_2^2]$$

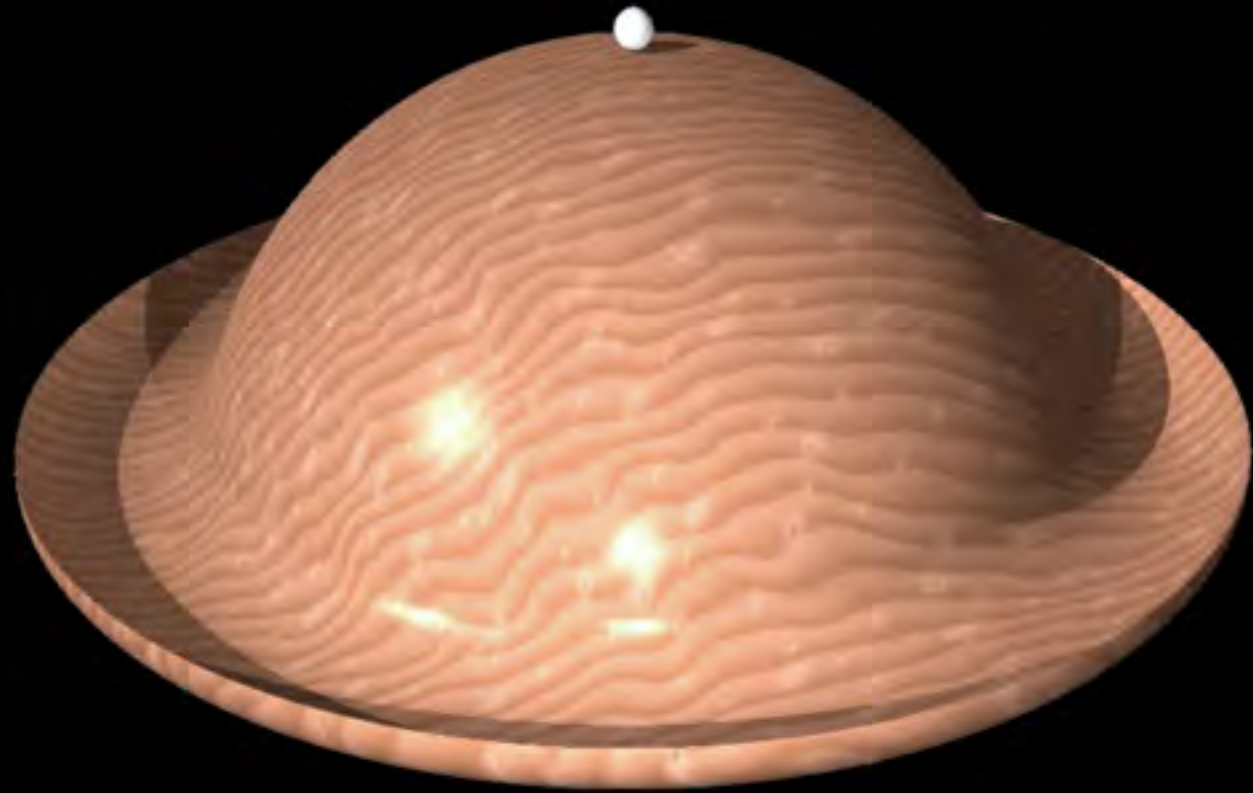
Two Identical Bosons Ground State : $n_1 = n_2 = 1$

Two Identical Fermions Ground State : $n_1 = 1, n_2 = 2$ OR
 $n_1 = 2, n_2 = 1$



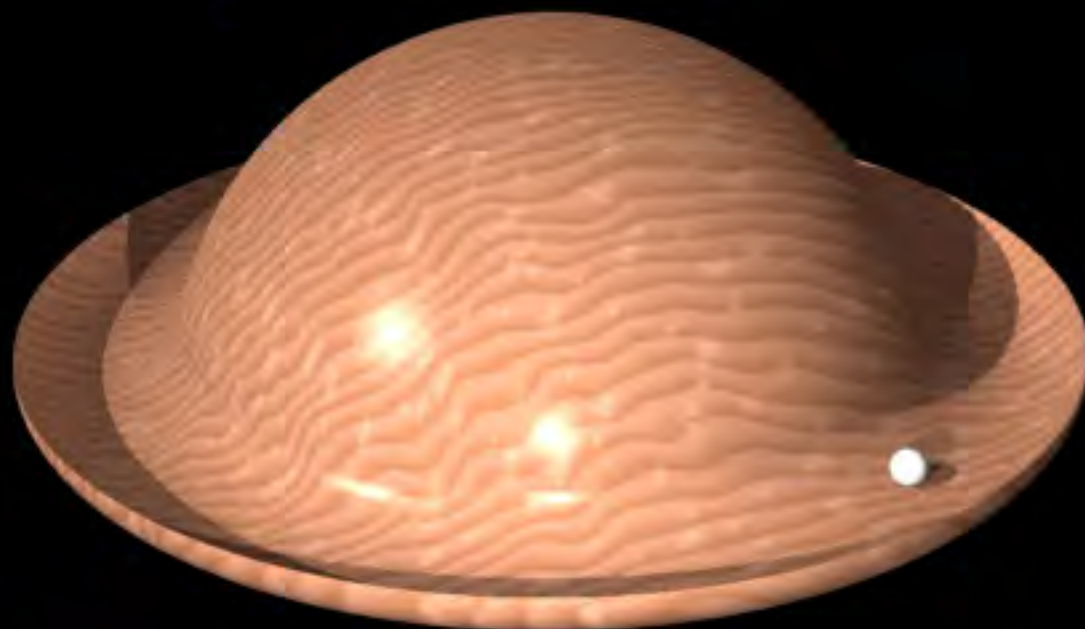
Goldstino, Gravitino & Superpartner Masses

Methods
'Hidden Sector,'
AMSB,
Gaugino Condensates,
etc.





Superpartner Mass & The Goldstino





Force Carriers (Gauge Particles)

	M	Q	S	
$g_{\mu\nu}$ (graviton)	0	0	2	
Ψ_{μ}^d (gravitino)	0	0	3/2	
	80.6	+1	1	(charged IVB) W_{μ}^{+}
	?	+1	1/2	(+charged Wino) \tilde{W}^{+}
G_{μ}^i (gluon)	0	0	1	
$\tilde{\lambda}^i$ (gluino)	0	0	1/2	
	91.2	0	1	(neutral IVB) Z_{μ}^0
	?	0	1/2	(neutral Zeno) \tilde{Z}
A_{μ} (photon)	0	0	1	
$\tilde{\lambda}$ (photino)	?	0	1/2	
	80.6	-1	1	(charged IVB) W_{μ}^{-}
	?	-1	1/2	(-charged Wino) \tilde{W}^{-}





SQuarks & Quarks

	M	Q	S	
u	4×10^{-3}	$2/3$	$1/2$	
\tilde{u} (up-squark)	?	$2/3$	0	
	7×10^{-3}	$-1/3$	$1/2$	d
	?	$-1/3$	0	(down-squark) \tilde{d}
c	1.5	$2/3$	$1/2$	
\tilde{c} (charmed-squark)	?	$2/3$	0	
	0.15	$-1/3$	$1/2$	s
	?	$-1/3$	0	(strange-squark) \tilde{s}
t	173	$2/3$	$1/2$	
\tilde{t} (top-squark)	?	$2/3$	0	
	4.7	$-1/3$	$1/2$	b
	?	$-1/3$	0	(bottom-squark) \tilde{b}





SLeptons & Leptons

mass unit $\frac{\text{GeV}}{c^2}$

$m_\nu \rightarrow 10^{-8}/10^{-4}/10^{-2}$

	M	Q	S	
ν_e	~ 0	0	1/2	
$\tilde{\nu}_e$ (e-sneutrino)	?	0	0	
$\tilde{\nu}_e$	5×10^{-4}	-1	1/2	e
$\tilde{\nu}_e$?	-1	0	(selectron) \tilde{e}
ν_μ	~ 0	0	1/2	
$\tilde{\nu}_\mu$ (μ -sneutrino)	?	0	0	
$\tilde{\nu}_\mu$	0.106	-1	1/2	μ
$\tilde{\nu}_\mu$?	-1	0	(smuon) $\tilde{\mu}$
ν_τ	~ 0	0	1/2	
$\tilde{\nu}_\tau$ (τ -sneutrino)	?	0	0	
$\tilde{\nu}_\tau$	1.784	-1	1/2	τ
$\tilde{\nu}_\tau$?	-1	0	(staon) $\tilde{\tau}$





LHC Search
For The MSSM
(Sci Run-1)

ATLAS SUSY Searches* - 95% CL Lower Limits

Status: SUSY 2018

ATLAS Preliminary

$\int \mathcal{L} dt = (4.6 - 22.9) \text{ fb}^{-1}$ $\sqrt{s} = 7, 8 \text{ TeV}$

Model	e, μ, τ, γ	Jets	E_T^{miss}	$[\mathcal{L} dt][\text{fb}^{-1}]$	Mass limit	Reference	
Inclusive Searches	MSUGRA/CMSSM	0	2-6 jets	Yes	20.3	1.7 TeV	$m(\tilde{g})=m(\tilde{u}_L)$ ATLAS-CONF-2013-047
	MSUGRA/CMSSM	1 e, μ	3-6 jets	Yes	20.3	1.2 TeV	any $m(\tilde{g})$ ATLAS-CONF-2013-069
	MSUGRA/CMSSM	0	7-10 jets	Yes	20.3	1.1 TeV	any $m(\tilde{g})$ 1308.1841
	$q\bar{q}, \bar{q} \rightarrow q\bar{q} \chi^0$	0	2-6 jets	Yes	20.3	740 GeV	$m(\tilde{t}_1^+)=0 \text{ GeV}$ ATLAS-CONF-2013-047
	$q\bar{q}, \bar{q} \rightarrow q\bar{q} \chi^0$	0	2-6 jets	Yes	20.3	1.3 TeV	$m(\tilde{t}_1^+)=0 \text{ GeV}$ ATLAS-CONF-2013-047
	$q\bar{q}, \bar{q} \rightarrow q\bar{q} \chi^0$	1 e, μ	3-6 jets	Yes	20.3	1.38 TeV	$m(\tilde{t}_1^+)=200 \text{ GeV}, m(\tilde{t}_2^+)=0.5 m(\tilde{t}_1^+) \text{ cm}(\tilde{g})$ ATLAS-CONF-2013-062
	$q\bar{q}, \bar{q} \rightarrow q\bar{q}(\ell\ell/\nu\nu) \chi^0$	2 e, μ	0-3 jets	-	20.3	1.12 TeV	$m(\tilde{t}_1^+)=0 \text{ GeV}$ ATLAS-CONF-2013-089
	GMSB ($\tilde{\tau}$ NLSP)	2 e, μ	2-4 jets	Yes	4.7	1.24 TeV	$ \text{Im}(A) =15$ 1308.4598
	GMSB ($\tilde{\tau}$ NLSP)	1-2 τ	0-2 jets	Yes	20.7	1.4 TeV	$ \text{Im}(A) =18$ ATLAS-CONF-2013-026
	GGM (bino NLSP)	2 γ	-	Yes	4.6	1.87 TeV	$m(\tilde{t}_1^+)=50 \text{ GeV}$ 1209.0753
	GGM (wino NLSP)	1 $e, \mu + \gamma$	-	Yes	4.8	819 GeV	$m(\tilde{t}_1^+)=50 \text{ GeV}$ ATLAS-CONF-2012-144
	GGM (higgsino bino NLSP)	γ	1 b	Yes	4.8	380 GeV	$m(\tilde{t}_1^+)=220 \text{ GeV}$ 1211.1167
GGM (higgsino NLSP)	2 $e, \mu + Z$	0-3 jets	Yes	5.8	880 GeV	$m(\tilde{H})=200 \text{ GeV}$ ATLAS-CONF-2012-152	
Gravitino LSP	0	mono-jet	Yes	10.5	643 GeV	$m(\tilde{g})=10^{-4} \text{ eV}$ ATLAS-CONF-2012-147	
3 rd gen. \tilde{g}, \tilde{q} med.	$\tilde{g} \rightarrow b\bar{b} \chi^0$	0	3 b	Yes	20.1	1.2 TeV	$m(\tilde{t}_1^+)=600 \text{ GeV}$ ATLAS-CONF-2013-081
	$\tilde{g} \rightarrow t\bar{t} \chi^0$	0	7-10 jets	Yes	20.3	1.1 TeV	$m(\tilde{t}_1^+)=380 \text{ GeV}$ 1308.1841
	$\tilde{q} \rightarrow t\bar{t} \chi^0$	0-1 e, μ	3 b	Yes	20.1	1.34 TeV	$m(\tilde{t}_1^+)=400 \text{ GeV}$ ATLAS-CONF-2013-061
	$\tilde{q} \rightarrow b\bar{b} \chi^0$	0-1 e, μ	3 b	Yes	20.1	1.2 TeV	$m(\tilde{t}_1^+)=300 \text{ GeV}$ ATLAS-CONF-2013-061
3 rd gen. squarks direct production	$\tilde{d}_1 \tilde{d}_1, \tilde{d}_1 \rightarrow b\bar{b} \chi^0$	0	2 b	Yes	20.1	100-520 GeV	$m(\tilde{t}_1^+)=90 \text{ GeV}$ 1308.2831
	$\tilde{d}_1 \tilde{d}_1, \tilde{d}_1 \rightarrow t\bar{t} \chi^0$	2 e, μ (SS)	0-3 b	Yes	20.7	273-430 GeV	$m(\tilde{t}_1^+)=2 m(\tilde{t}_2^+)$ ATLAS-CONF-2013-007
	$\tilde{t}_1 \tilde{t}_1$ (light), $\tilde{t}_1 \rightarrow b\bar{b} \chi^0$	1-2 e, μ	1-2 b	Yes	4.7	110-167 GeV	$m(\tilde{t}_1^+)=55 \text{ GeV}$ 1208.4305, 1209.2102
	$\tilde{t}_1 \tilde{t}_1$ (light), $\tilde{t}_1 \rightarrow W\bar{b} \chi^0$	2 e, μ	0-2 jets	Yes	20.3	100-220 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+)=m(W)+50 \text{ GeV}, m(\tilde{t}_1^+)=m(\tilde{t}_2^+)$ ATLAS-CONF-2013-048
	$\tilde{t}_1 \tilde{t}_1$ (medium), $\tilde{t}_1 \rightarrow t\bar{t} \chi^0$	2 e, μ	2 jets	Yes	20.3	225-326 GeV	$m(\tilde{t}_1^+)=0 \text{ GeV}$ ATLAS-CONF-2013-065
	$\tilde{t}_1 \tilde{t}_1$ (medium), $\tilde{t}_1 \rightarrow b\bar{b} \chi^0$	0	2 b	Yes	20.1	150-580 GeV	$m(\tilde{t}_1^+)=200 \text{ GeV}, m(\tilde{t}_2^+)=m(\tilde{t}_1^+)=5 \text{ GeV}$ 1308.2831
	$\tilde{t}_1 \tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow t\bar{t} \chi^0$	1 e, μ	1 b	Yes	20.7	200-410 GeV	$m(\tilde{t}_1^+)=0 \text{ GeV}$ ATLAS-CONF-2013-037
	$\tilde{t}_1 \tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow b\bar{b} \chi^0$	0	2 b	Yes	20.5	300-600 GeV	$m(\tilde{t}_1^+)=0 \text{ GeV}$ ATLAS-CONF-2013-034
	$\tilde{t}_1 \tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow t\bar{t} \chi^0$	0	mono-jet/c-tag	Yes	20.3	90-200 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+)=85 \text{ GeV}$ ATLAS-CONF-2013-068
	$\tilde{t}_1 \tilde{t}_1$ (natural GMSB)	2 $e, \mu + Z$	1 b	Yes	20.7	500 GeV	$m(\tilde{t}_1^+)=150 \text{ GeV}$ ATLAS-CONF-2013-025
	$\tilde{t}_2 \tilde{t}_2, \tilde{t}_2 \rightarrow \tilde{t}_1 + Z$	3 $e, \mu + Z$	1 b	Yes	20.7	271-320 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+)=180 \text{ GeV}$ ATLAS-CONF-2013-025
	EW direct	$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow b\bar{b} \chi^0$	2 e, μ	0	Yes	20.3	85-375 GeV
$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow t\bar{t} \chi^0$		2 e, μ	0	Yes	20.3	125-480 GeV	$m(\tilde{t}_1^+)=0 \text{ GeV}, m(\tilde{t}_2^+)=0.5(m(\tilde{t}_1^+)+m(\tilde{t}_2^+))$ ATLAS-CONF-2013-049
$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow \tau\bar{\tau} \chi^0$		2 τ	-	Yes	20.7	190-330 GeV	$m(\tilde{t}_1^+)=0 \text{ GeV}, m(\tilde{t}_2^+)=0.5(m(\tilde{t}_1^+)+m(\tilde{t}_2^+))$ ATLAS-CONF-2013-035
$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow \nu\bar{\nu} \chi^0$		3 e, μ	0	Yes	20.7	600 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+), m(\tilde{t}_1^+)=0, m(\tilde{t}_2^+)=0.5(m(\tilde{t}_1^+)+m(\tilde{t}_2^+))$ ATLAS-CONF-2013-035
$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow W\bar{t} \chi^0$		3 e, μ	0	Yes	20.7	315 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+), m(\tilde{t}_1^+)=0, \text{ stopions decoupled}$ ATLAS-CONF-2013-036
$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow H\bar{t} \chi^0$		1 e, μ	2 b	Yes	20.3	280 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+), m(\tilde{t}_1^+)=0, \text{ stopions decoupled}$ ATLAS-CONF-2013-060
Long-lived particles	Direct $\tilde{t}_1 \tilde{t}_1$ prod., long-lived \tilde{t}_1^+	Disapp. trk	1 jet	Yes	20.3	270 GeV	$m(\tilde{t}_1^+)=m(\tilde{t}_2^+)=160 \text{ MeV}, \tau(\tilde{t}_1^+)=0.2 \text{ ns}$ ATLAS-CONF-2013-089
	Stable, stopped \tilde{g} R-hadron	0	1-5 jets	Yes	22.9	832 GeV	$m(\tilde{t}_1^+)=100 \text{ GeV}, 10 \mu\text{s} < \tau(\tilde{g}) < 1000 \text{ s}$ ATLAS-CONF-2013-057
	GMSB, stable $\tilde{F}, \tilde{F}_1 \rightarrow \tilde{F}(\tilde{g}, \tilde{u}) + \tau(\tilde{e}, \mu)$	1-2 μ	-	Yes	15.9	> 875 GeV	$10^{-4} \text{ s} < \tau < 50$ ATLAS-CONF-2013-058
	GMSB, $\tilde{F}_1 \rightarrow \gamma G, \text{ long-lived } \tilde{F}_1$	2 τ	-	Yes	4.7	230 GeV	$0.4 < \tau(\tilde{F}_1) < 2 \text{ ns}$ 1304.8310
$q\bar{q}, \tilde{F}_1 \rightarrow q\bar{q} \chi^0$ (RPV)	1 $\mu, \text{ displ. vtx.}$	-	-	20.3	1.0 TeV	$1.5 < c\tau < 156 \text{ nm}, \text{BR}(\tilde{F}_1 \rightarrow t) = 1, m(\tilde{F}_1) = 108 \text{ GeV}$ ATLAS-CONF-2013-092	
RPV	LFV $pp \rightarrow \tilde{e}_i + X, \tilde{e}_i \rightarrow e + \mu$	2 e, μ	-	-	4.6	1.81 TeV	$\lambda_{111}^e=0.10, \lambda_{112}^e=0.05$ 1212.1272
	LFV $pp \rightarrow \tilde{e}_i + X, \tilde{e}_i \rightarrow e(\mu) + \tau$	1 $e, \mu + \tau$	-	-	4.6	1.1 TeV	$\lambda_{111}^e=0.10, \lambda_{121}^e=0.05$ 1212.1272
	Bilinear RPV CMSSM	1 e, μ	7 jets	Yes	4.7	1.2 TeV	$m(\tilde{g})=m(\tilde{u}_L), \text{cm}(\tilde{g})=1 \text{ mm}$ ATLAS-CONF-2013-140
	$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow W\bar{t} \chi^0, \tilde{t}_1 \rightarrow e\bar{e} \nu, \text{ cm}(\tilde{g})$	4 e, μ	-	Yes	20.7	760 GeV	$m(\tilde{t}_1^+)=300 \text{ GeV}, \lambda_{121}^e > 0$ ATLAS-CONF-2013-036
	$\tilde{t}_1 \tilde{t}_1, \tilde{t}_1 \rightarrow W\bar{t} \chi^0, \tilde{t}_1 \rightarrow \tau\bar{\tau} \nu, \text{ cm}(\tilde{g})$	3 $e, \mu + \tau$	-	Yes	20.7	350 GeV	$m(\tilde{t}_1^+)=80 \text{ GeV}, \lambda_{121}^e > 0$ ATLAS-CONF-2013-036
	$\tilde{g} \rightarrow q\bar{q} \chi^0$	0	6-7 jets	-	20.3	916 GeV	$\text{BR}(\tilde{g}) \rightarrow B R(\tilde{g}) \rightarrow B R(\tilde{g}) = 0\%$ ATLAS-CONF-2013-091
$\tilde{g} \rightarrow \tilde{t}_1 \bar{t}_1, \tilde{t}_1 \rightarrow b\bar{s}$	2 e, μ (SS)	0-3 b	Yes	20.7	800 GeV	- ATLAS-CONF-2013-067	
Other	Scalar gluon pair, sgluon $\rightarrow q\bar{q}$	0	4 jets	-	4.6	100-267 GeV	incl. limit from 1116.2893 1210.4826
	Scalar gluon pair, sgluon $\rightarrow t\bar{t}$	2 e, μ (SS)	1 b	Yes	14.3	800 GeV	ATLAS-CONF-2013-081
	WIMP interaction (DS, Dirac χ)	0	mono-jet	Yes	10.5	700 GeV	$m(\tilde{t}_1^+)=80 \text{ GeV}, \text{ limit at } \approx 687 \text{ GeV}/h/c\tau$ ATLAS-CONF-2012-147

*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed limits. τ = theoretical signal cross section uncertainty.

√s = 7 TeV √s = 8 TeV √s = 8 TeV
full data partial data full data

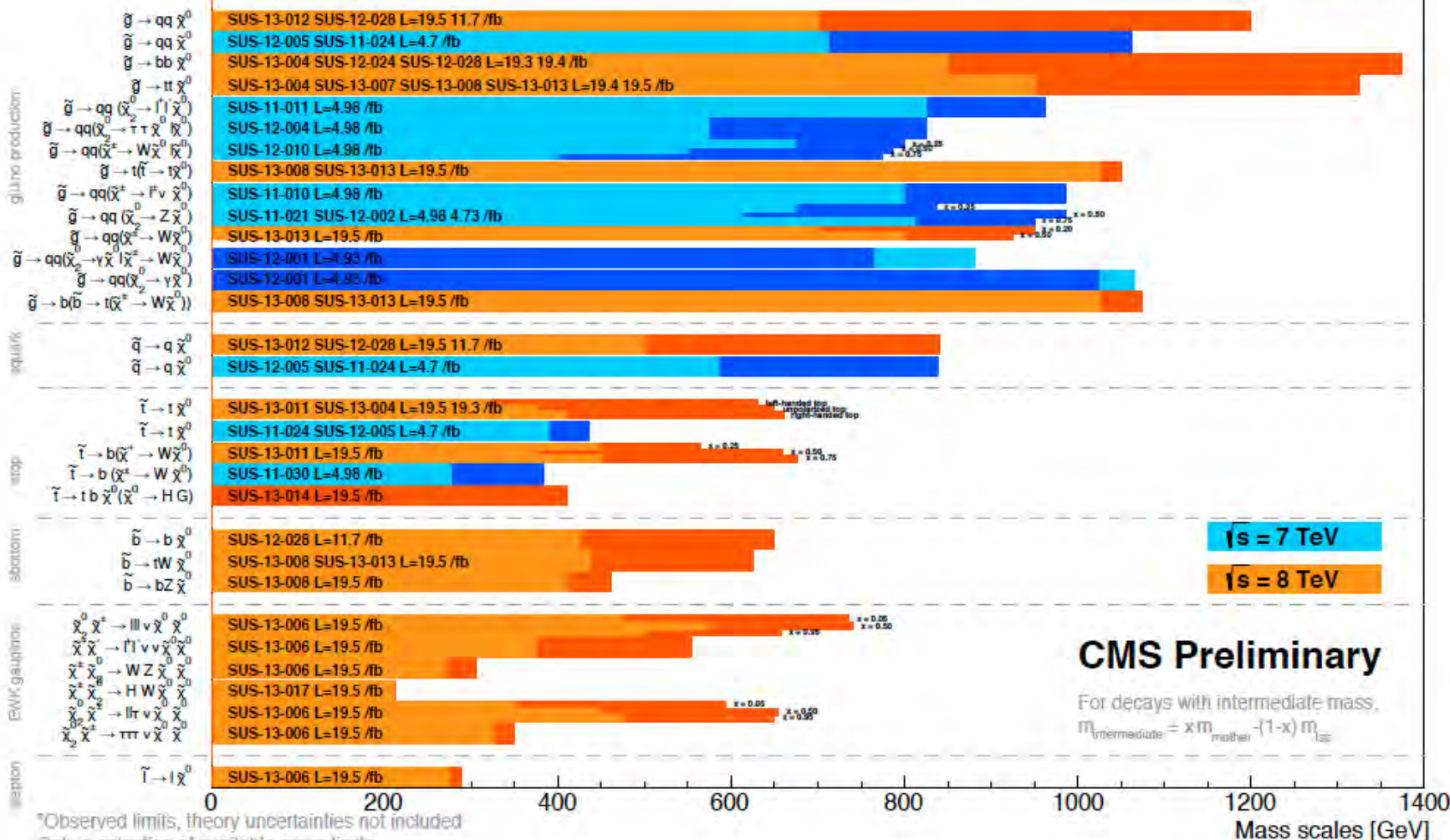
Mass scale [TeV]

Summary of CMS SUSY Results* in SMS framework

SUSY 2013

$m(\text{mother})-m(\text{LSP})=200 \text{ GeV}$

$m(\text{LSP})=0 \text{ GeV}$



$\sqrt{s} = 7 \text{ TeV}$
 $\sqrt{s} = 8 \text{ TeV}$

CMS Preliminary

For decays with intermediate mass,
 $m_{\text{intermediate}} = x m_{\text{mother}} - (1-x) m_{\text{LSP}}$

*Observed limits, theory uncertainties not included
 Only a selection of available mass limits
 Probe "up to" the quoted mass limit

Constrained Minimal Supersymmetric Standard Model (CMSSM)

G. L. Kane, C. F. Kolda, L. Roszkowski and J. D. Wells, Phys. Rev. D 49 (1994) 6173

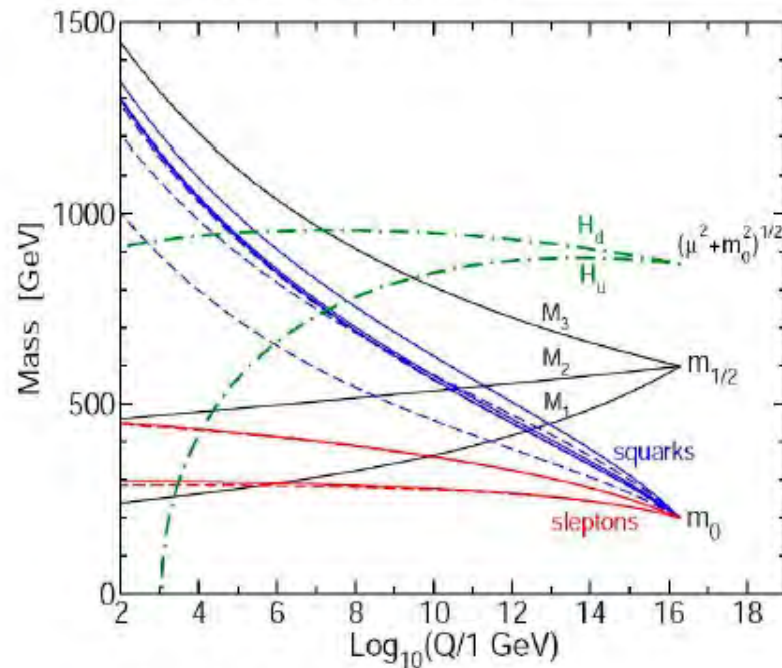


figure from hep-ph/9709356

At $M_{\text{GUT}} \simeq 2 \times 10^{16}$ GeV:

- gauginos $M_1 = M_2 = m_{\tilde{g}} = m_{1/2}$
- scalars $m_{\tilde{q}_i}^2 = m_{\tilde{l}_i}^2 = m_{H_b}^2 = m_{H_t}^2 = m_0^2$
- 3-linear soft terms $A_b = A_t = A_0$
- radiative EWSB
$$\mu^2 = \frac{m_{H_b}^2 - m_{H_t}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \frac{m_Z^2}{2}$$
- five independent parameters: $m_{1/2}, m_0, A_0, \tan \beta, \text{sgn}(\mu)$
- well developed machinery to compute masses and couplings



In general supersymmetric SM too many free parameters

Phenomenological Minimal Supersymmetric

Symbol	Description	number of parameters
$\tan \beta$	the ratio of the vacuum expectation values of the two Higgs doublets	1
M_A	the mass of the pseudoscalar Higgs boson	1
μ	the higgsino mass parameter	1
M_1	the bino mass parameter	1
M_2	the wino mass parameter	1
M_3	the gluino mass parameter	1
$m_{\tilde{q}}, m_{\tilde{u}_R}, m_{\tilde{d}_R}$	the first and second generation squark masses	3
$m_{\tilde{l}}, m_{\tilde{e}_R}$	the first and second generation slepton masses	2
$m_{\tilde{Q}}, m_{\tilde{t}_R}, m_{\tilde{b}_R}$	the third generation squark masses	3
$m_{\tilde{L}}, m_{\tilde{\tau}_R}$	the third generation slepton masses	2
A_t, A_b, A_τ	the third generation trilinear couplings	3

...and from the media...

Is Supersymmetry Dead?

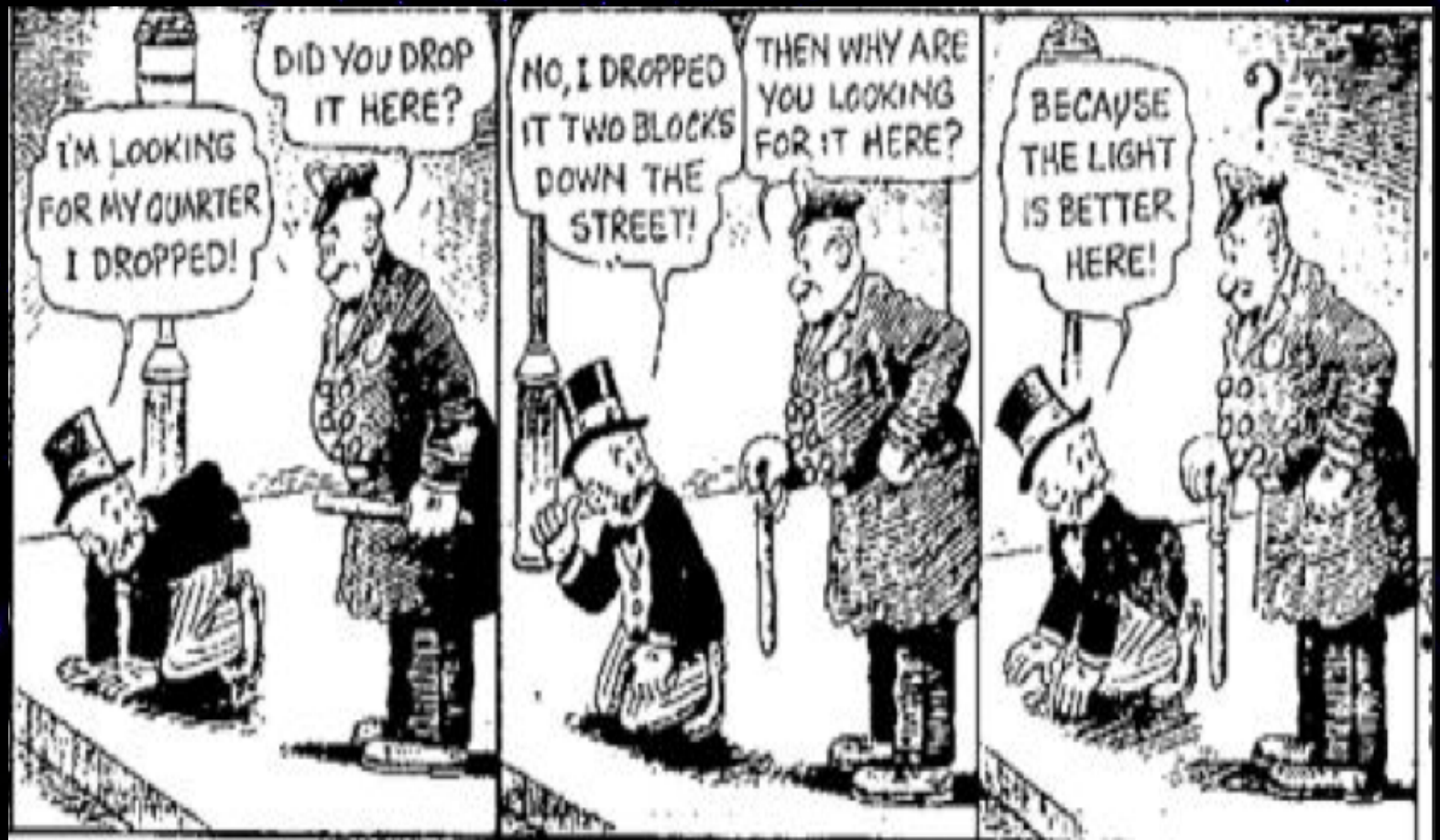
The grand scheme, a stepping-stone to string theory, is still high on physicists' wish lists. But if no solid evidence surfaces soon, it could begin to have a serious PR problem

**SCIENTIFIC
AMERICAN™**

April 2012

A dark blue starry night sky background with the word "Wrong!" in red serif font.

Wrong!





Features

Physics World **October 2014**



Sticking with SUSY



In my view, the current situation is akin to that of an explorer who, having scoured the eastern seaboard of North America, concludes that no groves of *Sequoiadendron giganteum* exist in the entire continental USA.

As with this hypothetical hunt for giant sequoia trees, finding evidence for SUSY depends on the observer looking in the right place.



Another example concerns the possible extension of something similar to quark–lepton symmetry. This occurs between quarks and the family of particles known as leptons, which includes the electron and its heavier cousins, the muon and the tau. When this symmetry – which explains why pairs of leptons appear in the Standard Model alongside pairs of quarks – is applied to a version of the Standard Model that possesses SUSY, the implication is that the Higgs boson discovered at the LHC is not the only one. **Instead, there must be a minimum of five Higgs bosons. This might seem like an embarrassment of riches, but if at some future point a second Higgs boson is observed, it could be a sign of SUSY appearing in nature.**

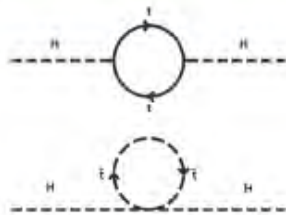
The 125 GeV Higgs Boson and SUSY

A curse...

In SUSY Higgs mass is a calculated quantity

➤ 1 loop correction

$$\Delta m_h^2 = \frac{3m_t^4}{4\pi^2 v^2} \left[\ln \left(\frac{M_{\text{SUSY}}^2}{m_t^2} \right) + \frac{X_t^2}{M_{\text{SUSY}}^2} \left(1 - \frac{X_t^2}{12M_{\text{SUSY}}^2} \right) \right]$$



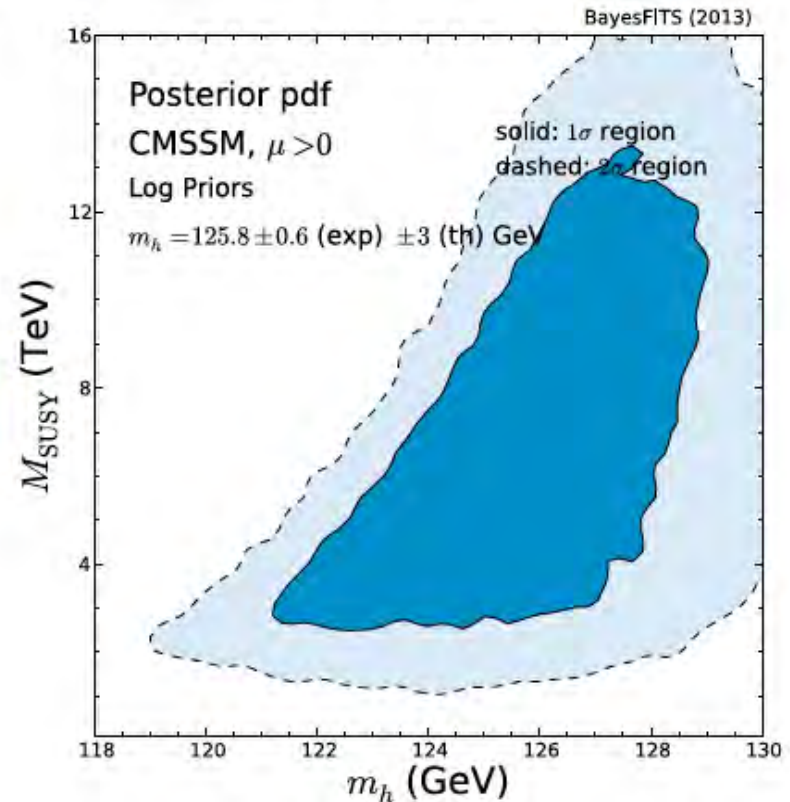
$$X_t = A_t - \mu \cot \beta$$

$$M_{\text{SUSY}} \equiv \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}}$$

Only $m_h \sim 125$ GeV and CMS lower bounds on SUSY applied here.

$$\mathcal{L} \sim e^{-\frac{(m_h - 125.8 \text{ GeV})^2}{\sigma^2 + \tau^2}}$$

$$\sigma = 0.6 \text{ GeV}, \tau = 2 \text{ GeV}$$



125 GeV Higgs -> multi-TeV SUSY



Effects:
MSSM vs. SM
Five Higgses

Q: Why Would Nature
Possess More Than
One Higgs?

A: More Local Symmetries
or ...



$$L_{e_1} \equiv \frac{1-\gamma^5}{2} \begin{bmatrix} \nu_{e_1} & \nu_{\mu_1} \\ e_1 & \mu_1 \end{bmatrix} \quad \gamma = -1 \quad H = -1$$

$$R_{e_1} \equiv \frac{1}{2}(1+\gamma^5)e_1 \quad \gamma = -2 \quad H = 0 \quad R_{\mu_1} \equiv \frac{1}{2}(1+\gamma^5)\mu_1 \quad \begin{matrix} \gamma = -2 \\ H = 0 \end{matrix}$$

$$L_{e_2} \equiv \frac{1-\gamma^5}{2} \begin{bmatrix} e_2 & \mu_2 \\ \nu_{e_2} & \nu_{\mu_2} \end{bmatrix} \quad \gamma = 1 \quad H = 1$$

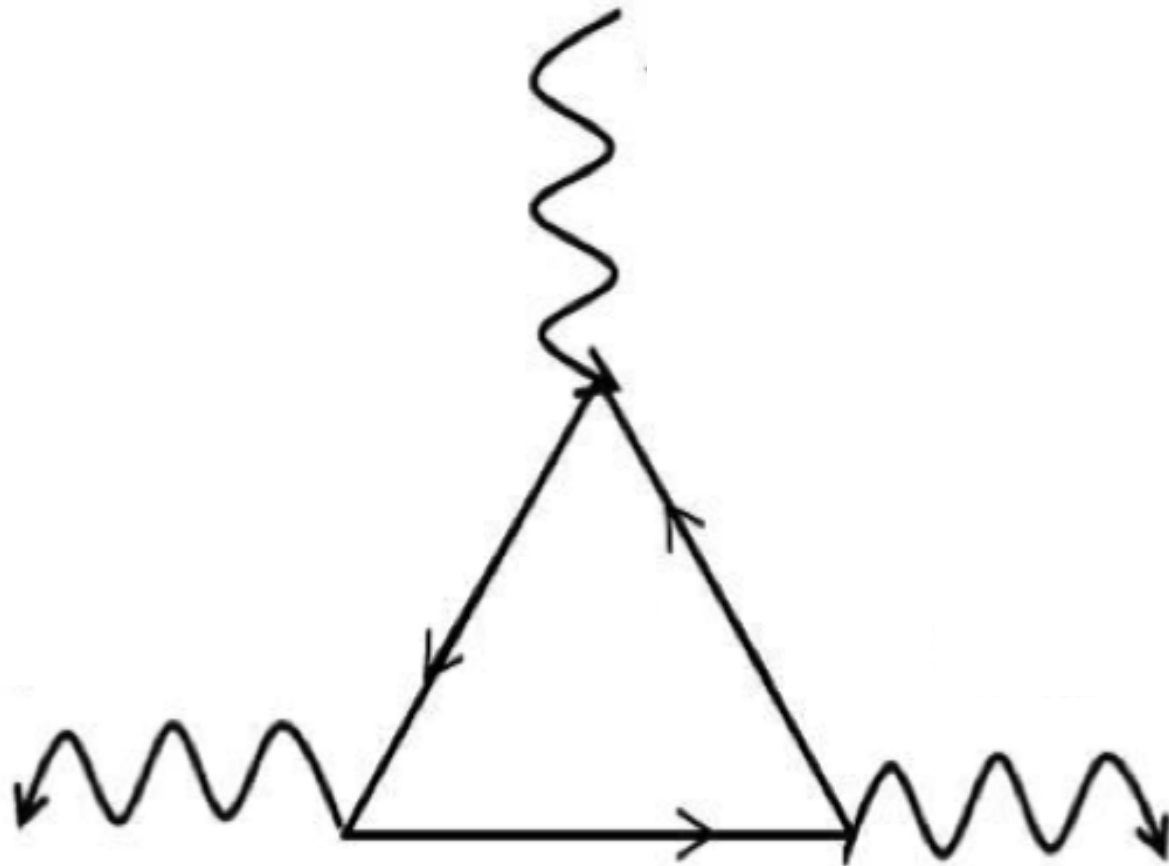
$$R_{e_2} \equiv \frac{1}{2}(1+\gamma^5)e_2 \quad \gamma = 2 \quad H = 0 \quad R_{\mu_2} \equiv \frac{1}{2}(1+\gamma^5)\mu_2 \quad \begin{matrix} \gamma = 2 \\ H = 0 \end{matrix}$$



Q: Why Does SUSY
Possess More Than
One Higgs?

A: Anomalies!

But There Are Quantum Dangers: Anomalies



But There Are Quantum Dangers: Anomalies

Anomalies and Anomaly-Freedom Conditions

$$Q_u = Q_d + 1 = \frac{1}{2} \left[1 - \frac{1}{3} (2Q_e + 1) \right]$$

$$Q_c = Q_s + 1 = \frac{1}{2} \left[1 - \frac{1}{3} (2Q_\mu + 1) \right]$$

$$Q_t = Q_b + 1 = \frac{1}{2} \left[1 - \frac{1}{3} (2Q_\tau + 1) \right]$$

“ $g_e - 2$ ”

The Best Known Theoretical Number in All of Science

Electron Anomalous Magnetic Moment

Measurement

$$g_e = 2.0023193038$$

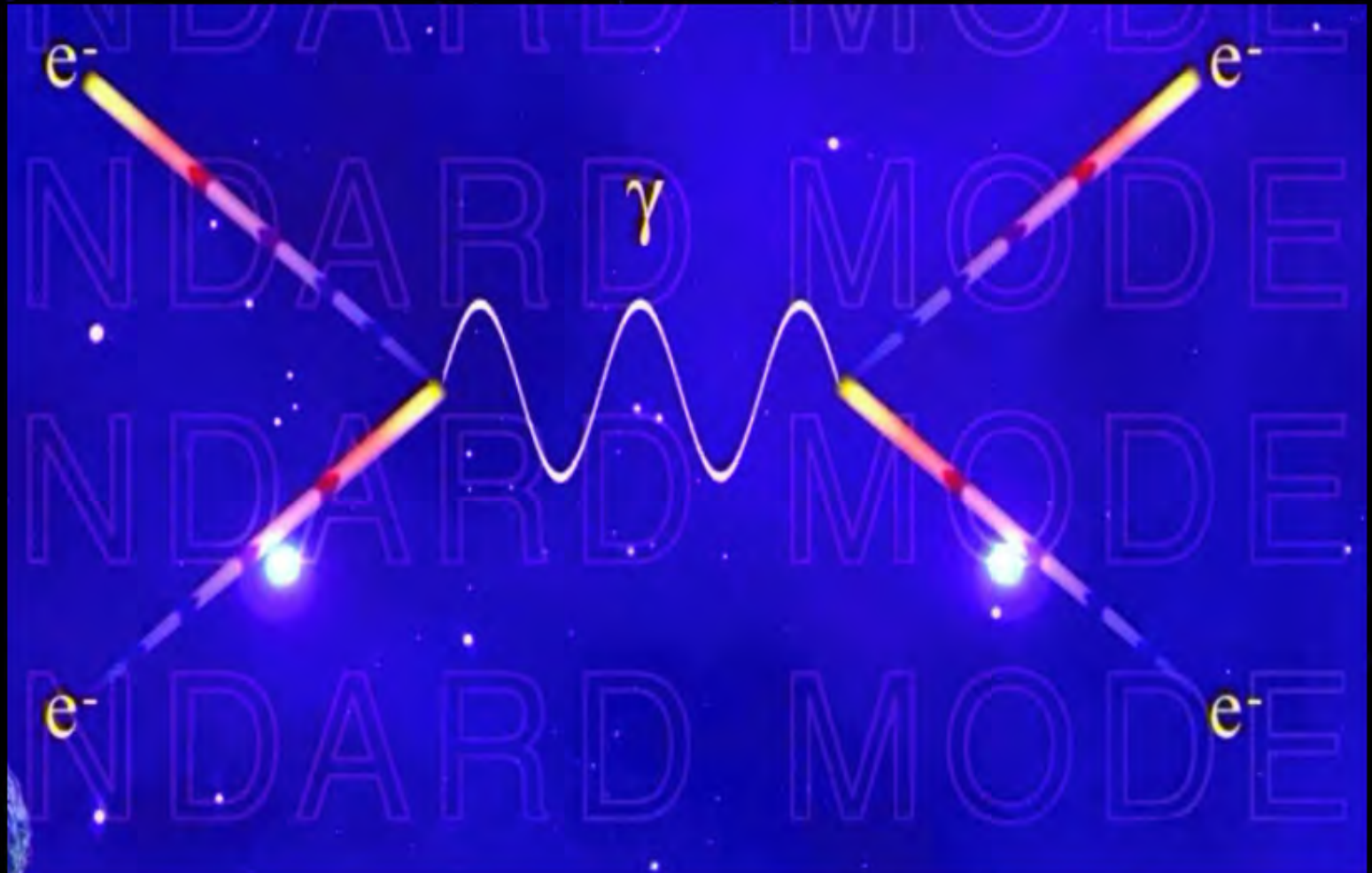
Uncertainty

$$\Delta g_e = \pm 0.0000000040$$

Theory

$$g_e = 2.0023193044$$

Quantum Loops &
The Interaction Paradigm



Quantum Loops

The Interaction Paradigm



Quantum Loops

The Interaction Paradigm



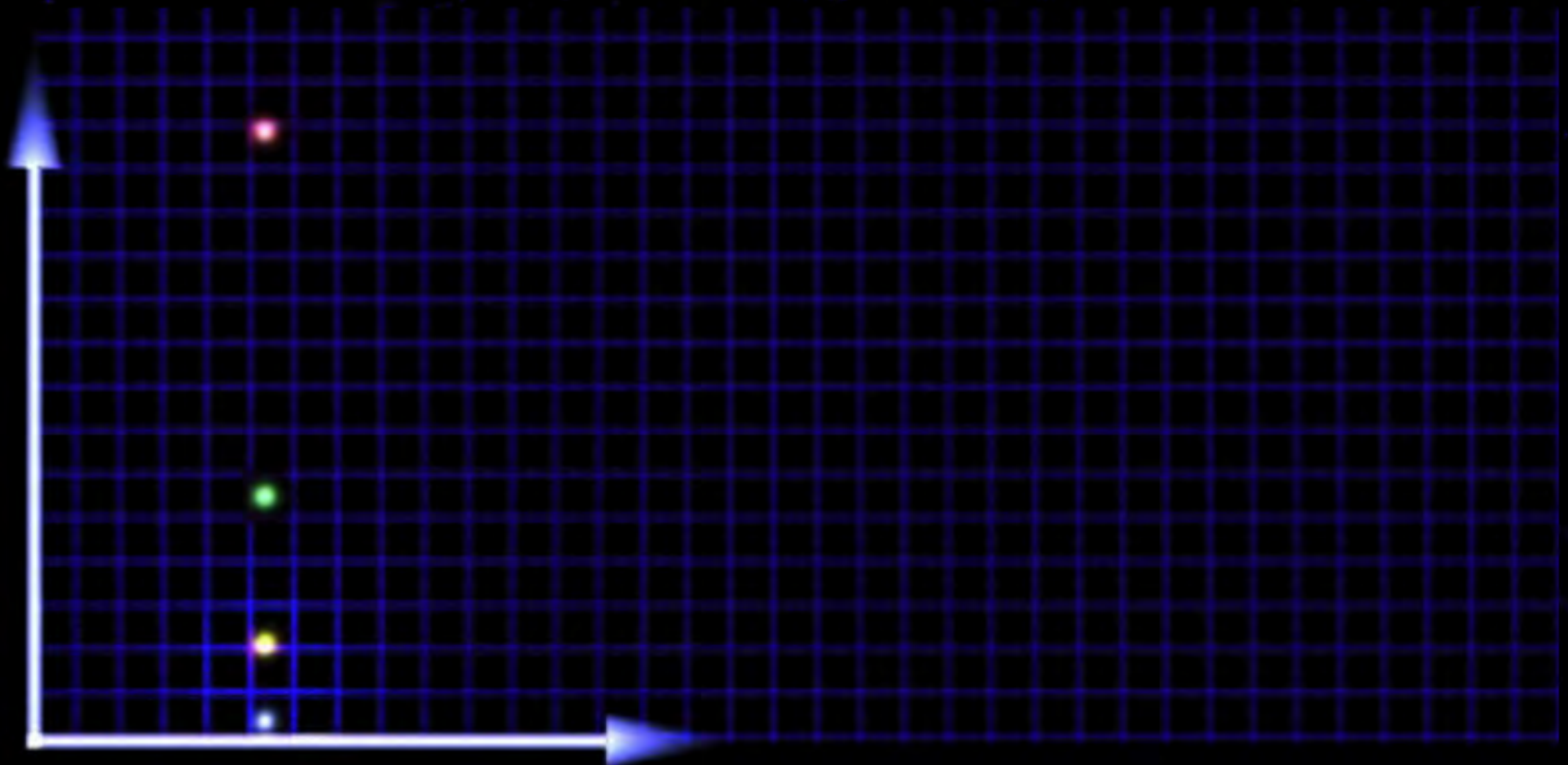


Effects:
MSSM vs. SM
Couplings

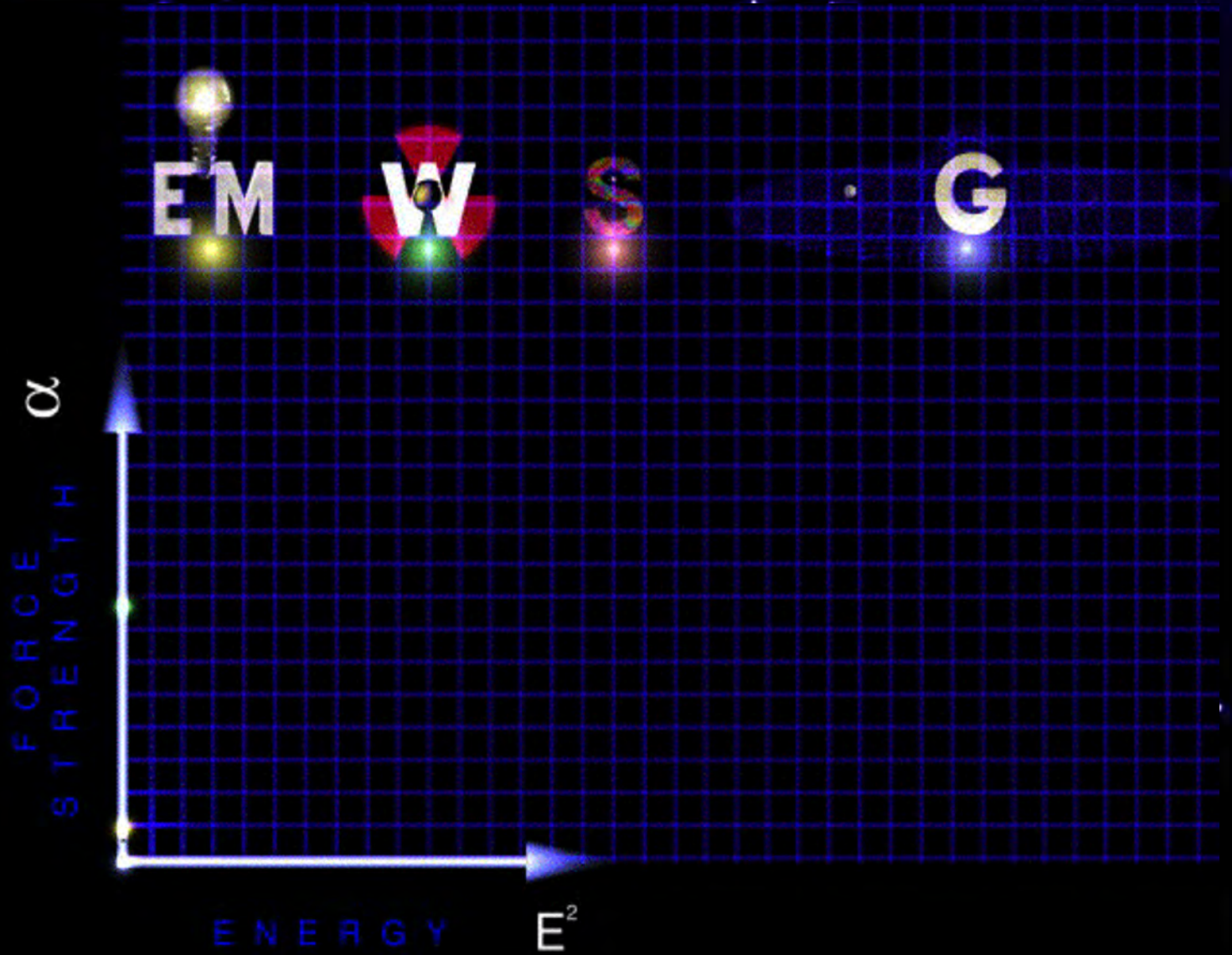


'Running Constants' with Superpartners

FORCE
STRENGTH α

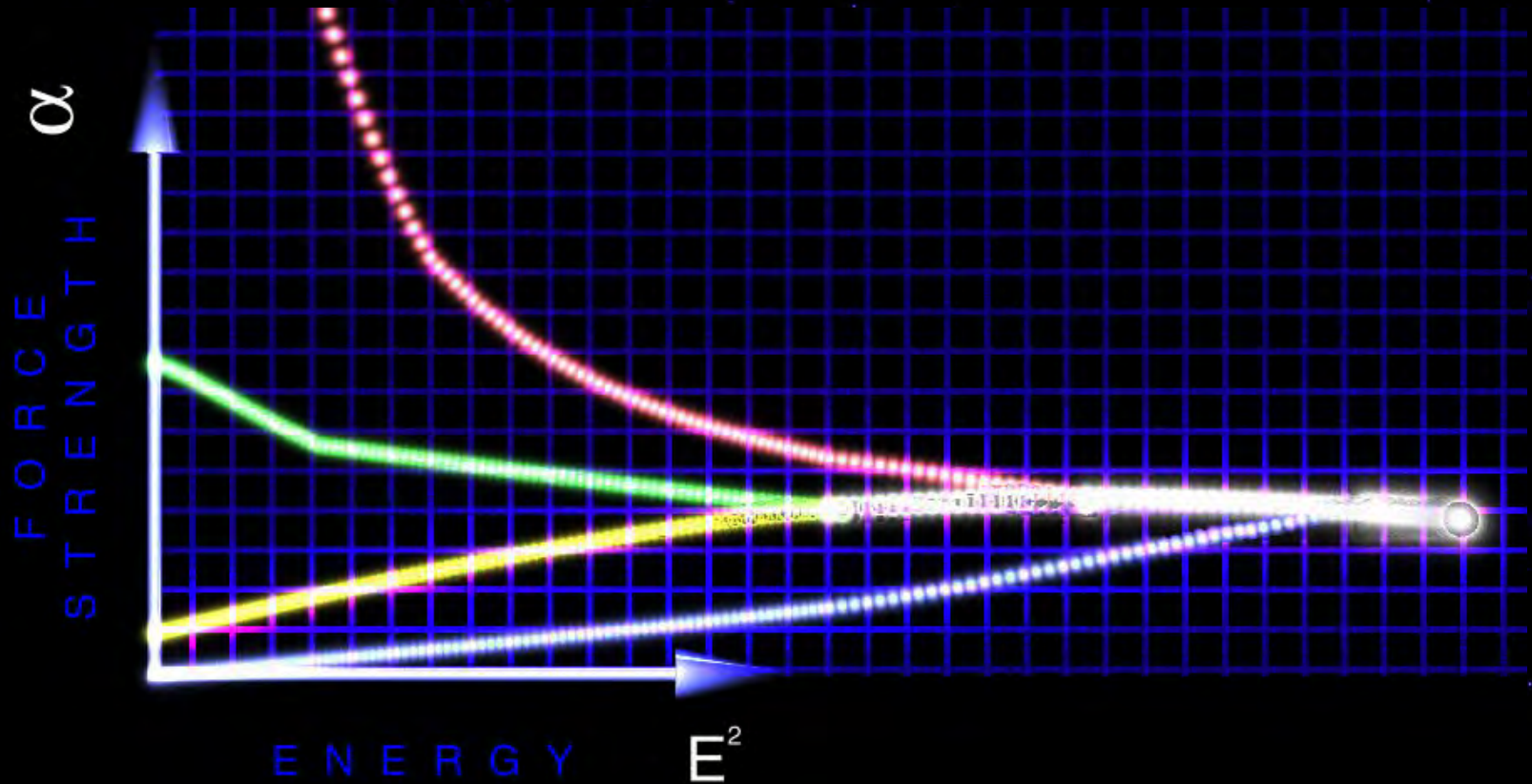


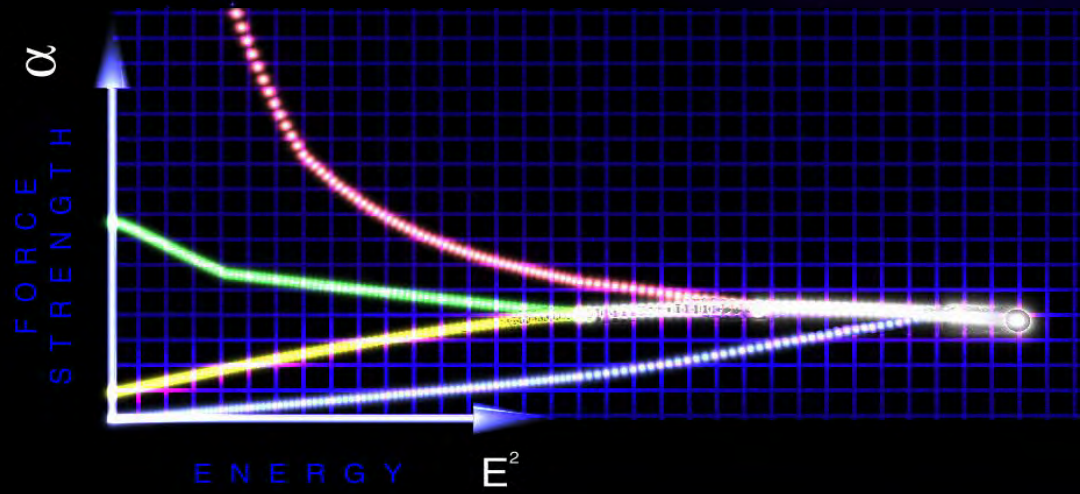
ENERGY E^2



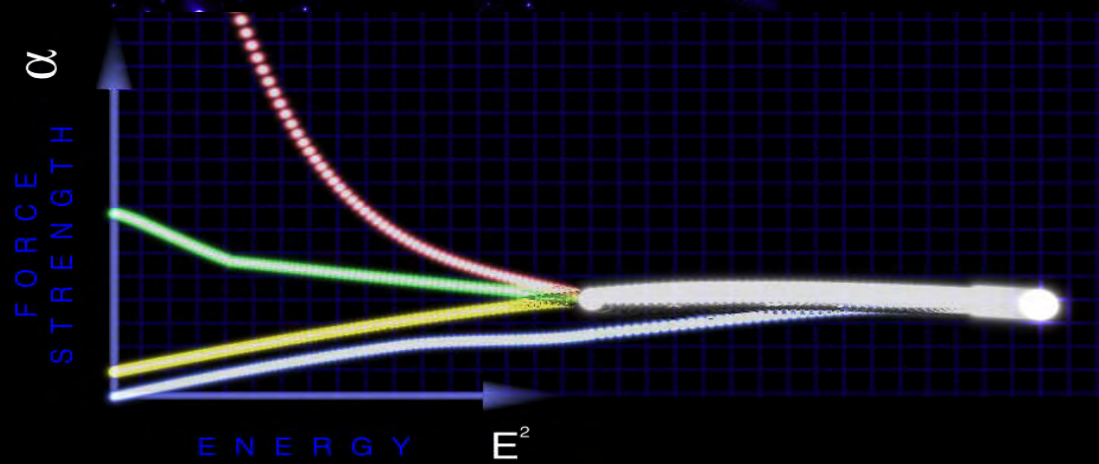


'Running Constants'





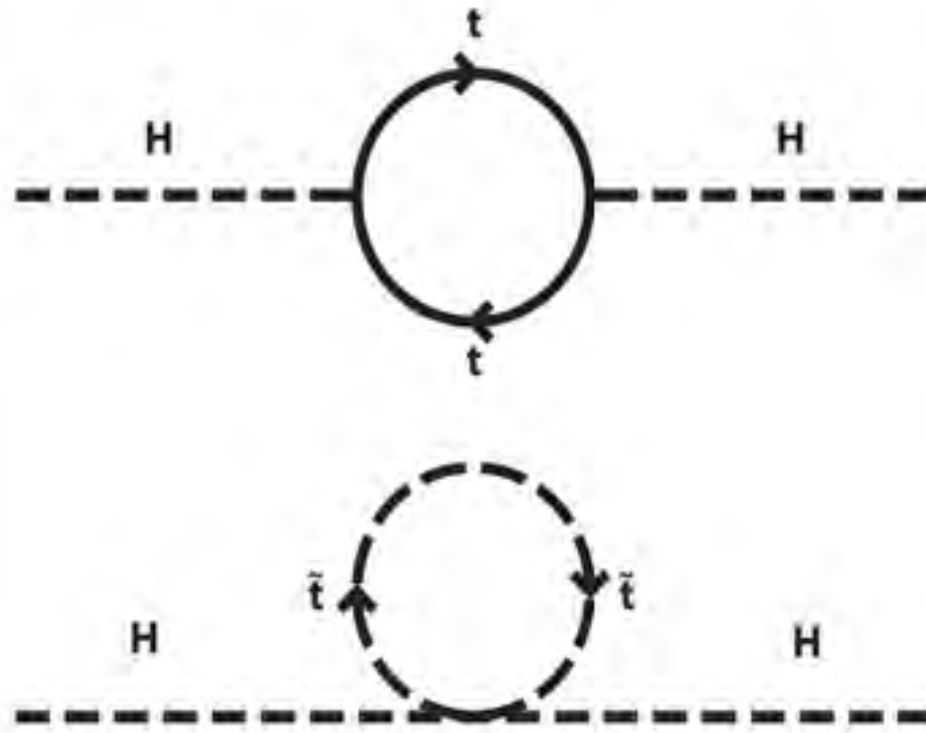
A Comparison





Effects:
MSSM vs. SM
Naturalness

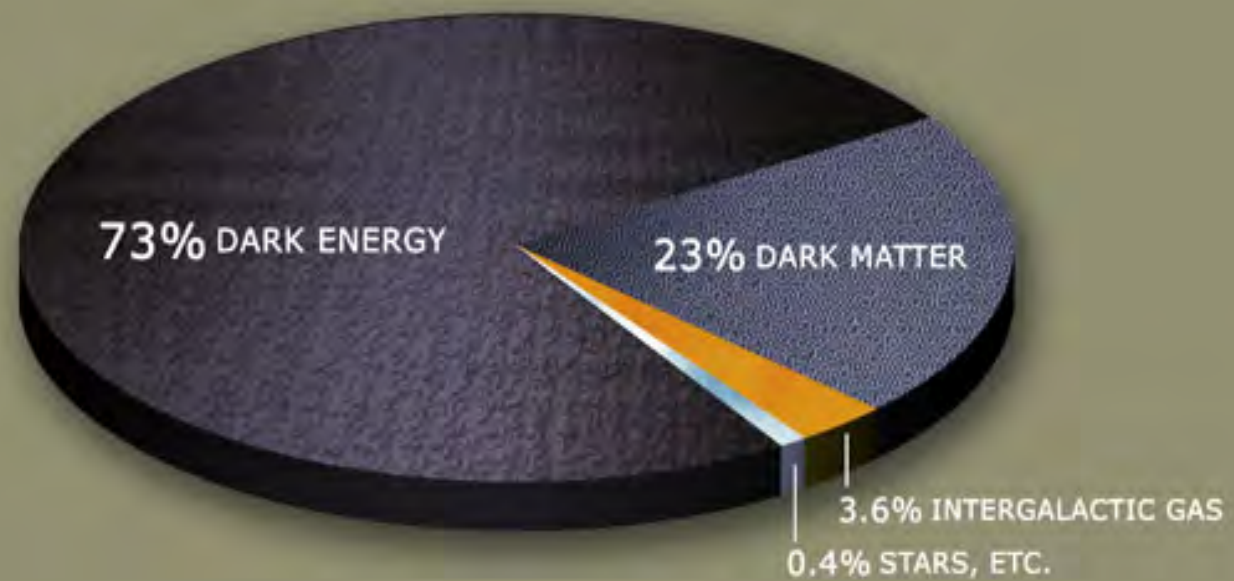




Cancellation of the Higgs boson quadratic mass renormalization between fermionic top quark loop and scalar top squark Feynman diagrams in a supersymmetric extension of the Standard Model



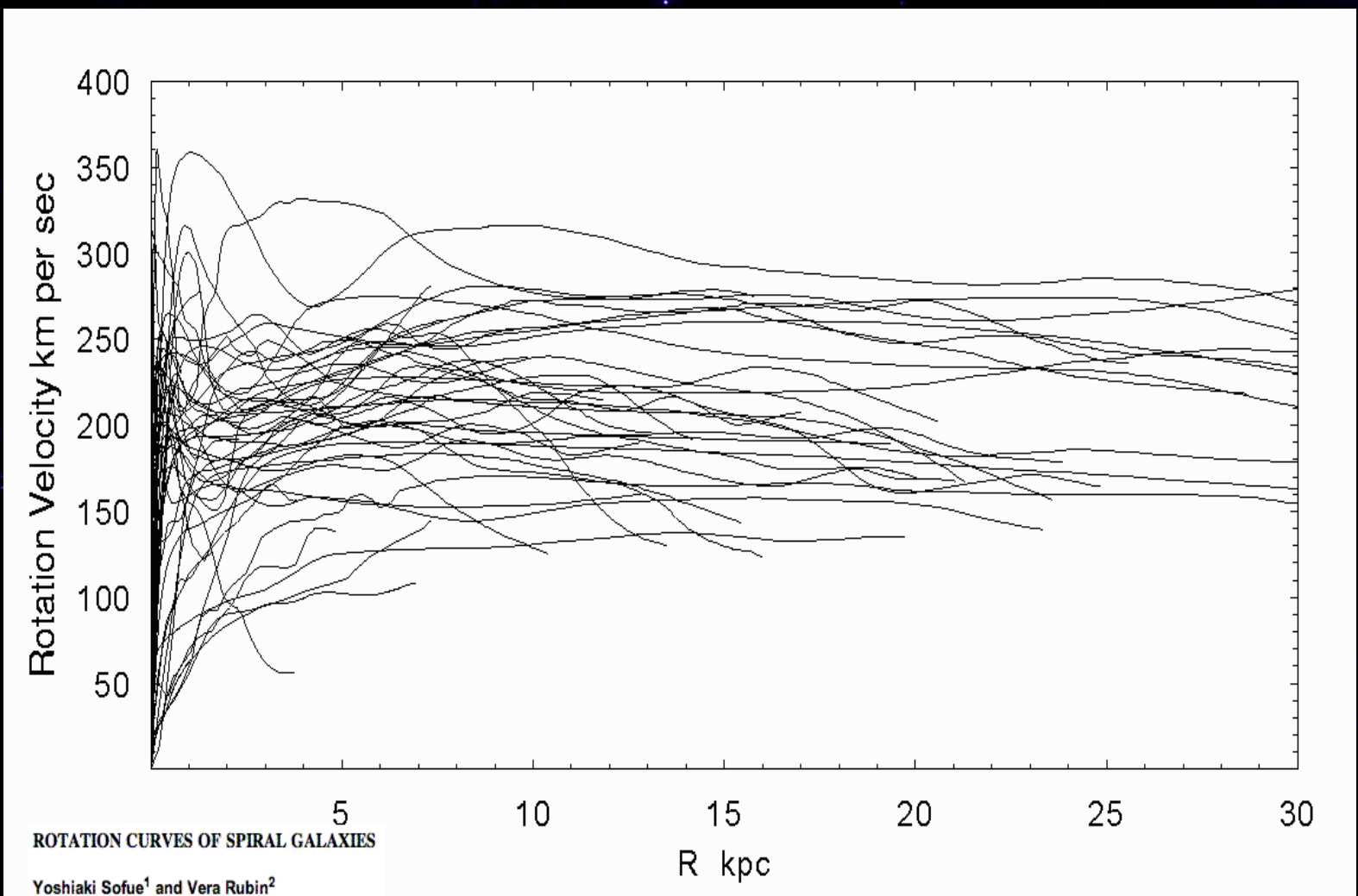
Effects:
MSSM vs. SM
Dark Matter



Lightest Supersymmetric Particle

From Wikipedia, the free encyclopedia

In [particle physics](#), the **lightest supersymmetric particle (LSP)** is the generic name given to the lightest of the additional hypothetical particles found in [supersymmetric models](#). In models with [R-parity](#) conservation, the LSP is stable. There is extensive observational evidence for an additional component of the matter density in the Universe that goes under the name [dark matter](#). The LSP of supersymmetric models is a dark matter candidate and is a [Weakly interacting massive particle \(WIMP\)](#).^[1]



ROTATION CURVES OF SPIRAL GALAXIES

Yoshiaki Sofue¹ and Vera Rubin²



Much Older Then
But
Much Younger Now



Is string theory phenomenologically viable?

S. James Gates Jr

String theory is entering an era in which its theoretical constructs will be confronted by experimental data. Some cherished ideas just might fail to pass the test.

June 2006 Physics Today

© 2006 American Institute of Physics, S-0031-9228-0606-060-1



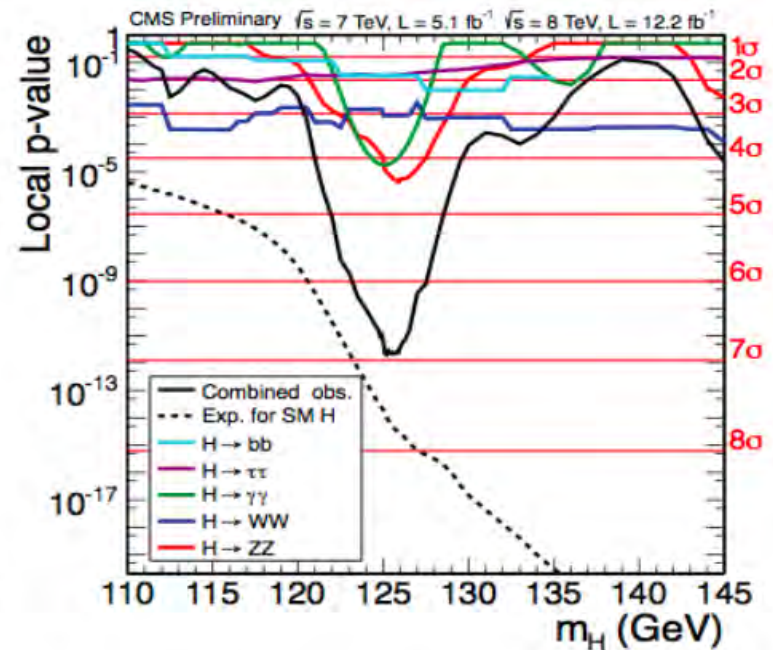
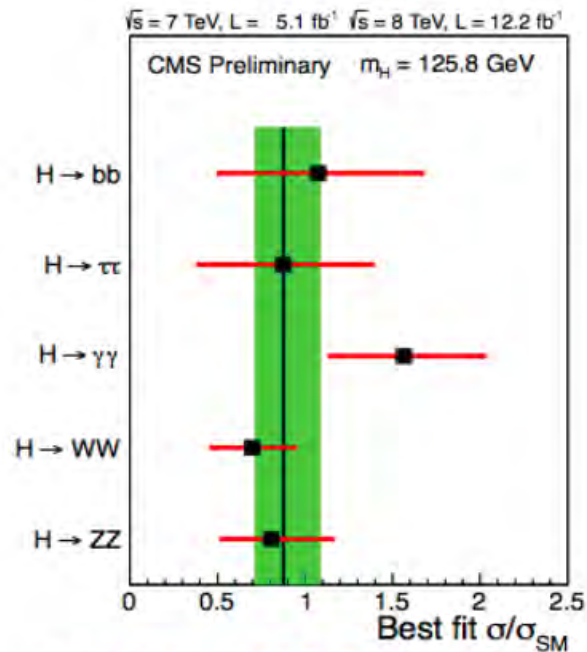
However, it will take great good fortune for a superparticle to be directly observable. The range of masses discussed in the literature is something like 1,000 to 30,000 times the mass of the proton, which is roughly $1 \text{ GeV}/c^2$

With the dates of discovery and masses of the neutron and W bosons as benchmarks, one can crudely estimate the rate at which humanity is progressing in its ability to detect massive particles: about $1.5 \text{ GeV}/c^2$ year. Thus, if Nature is kind enough to provide light superpartners, one might still expect about a century to pass before a superparticle is directly observed.

Much more likely, evidence for supersymmetry will emerge by indirect means. Such evidence might be provided by precision measurements of the rates of change of the coupling constants, anomalies in lifetimes or branching ratios in decays of known particles, and so forth.



Combined Limit & Global Picture



For $M_H = 125.8 \text{ GeV}$

Observed: 6.9; Expected: 7.8 → Signal strength: 0.88 ± 0.21



PHYSICS HIGHLIGHTS - PLAIN ENGLISH SUMMARIES



See also LHCb public webpage: <http://lhcb-public.web.cern.ch/lhcb-public/>

LHCb photo gallery <https://cdsweb.cern.ch/collection/LHCb%20Photos?ln=en>

Discovery of Ultra-Rare Decay at LHC

July 24th 2013

Summary: The LHC experiments LHCb and CMS have announced the observation of one of the rarest processes in fundamental physics, concluding a search that has lasted almost 30 years.

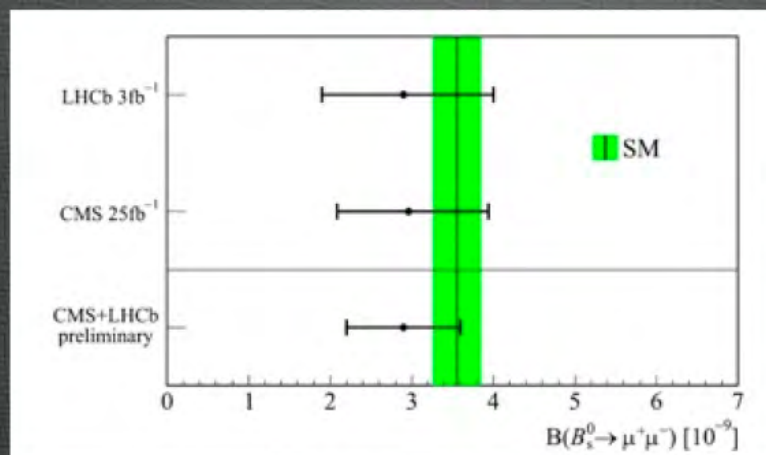


Image: Results of the LHCb and CMS experiments and the combination of these. By combining the results the threshold to announce discovery is passed. (Credit LHCb and CMS)




EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH (CERN)



CERN-PH-EP-2015-314
LHCb-PAPER-2015-051
December 14, 2015

Angular analysis of the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decay

The LHCb collaboration 



On the anomalies in the latest LHCb data

T. Hurth^[a], F. Mahmoudi^[b,c], S. Neshatpour^[d]

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Johannes Gutenberg University, D-55099 Mainz, Germany*


^b*Univ Lyon, Univ Lyon 1, ENS de Lyon, CNRS, Centre de Recherche Astrophysique de Lyon
UMR5574, F-69230 Saint-Genis-Laval, France*

^c*Theoretical Physics Department, CERN, CH-1211 Geneva 23, Switzerland*

^d*School of Particles and Accelerators, Institute for Research in Fundamental Sciences (IPM)
P.O. Box 19395-5531, Tehran, Iran*



If the ‘anomalies in the branching ratios’ grow after more analysis of data, then the post-Standard Model Era will have begun -- a rich spectrum of Higgs-like fields could be the avatars for the existence of symmetries beyond those of the SM...
maybe even **SUPERSYMMETRY**.



Effects:
Taming The
Quantum
Vacuum



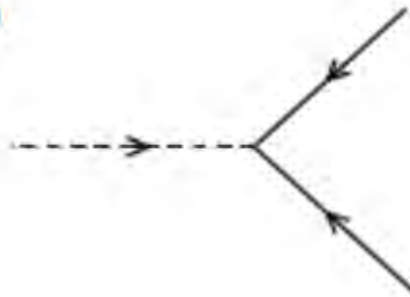
$N = 4$ supersymmetric Yang–Mills theory

$$L = \text{tr} \left\{ -\frac{1}{2g^2} F_{\mu\nu} F^{\mu\nu} + \frac{\theta_I}{8\pi^2} F_{\mu\nu} \bar{F}^{\mu\nu} - i\bar{\lambda}^a \bar{\sigma}^\mu D_\mu \lambda_a - D_\mu X^i D^\mu X^i \right. \\ \left. + gC_i^{ab} \lambda_a [X^i, \lambda_b] + g\bar{C}_{iab} \bar{\lambda}^a [X^i, \bar{\lambda}^b] + \frac{g^2}{2} [X^i, X^j]^2 \right\}$$

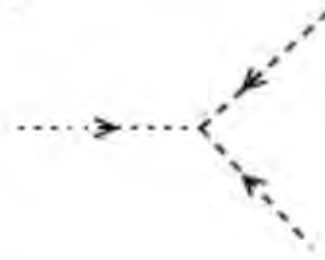


$N = 4$ supersymmetric Yang–Mills theory

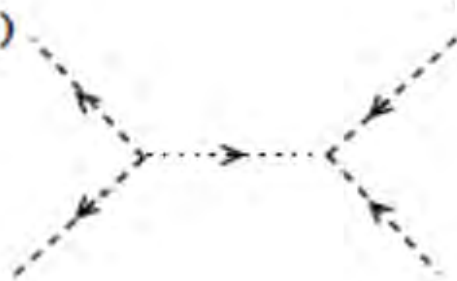
(a)



(b)

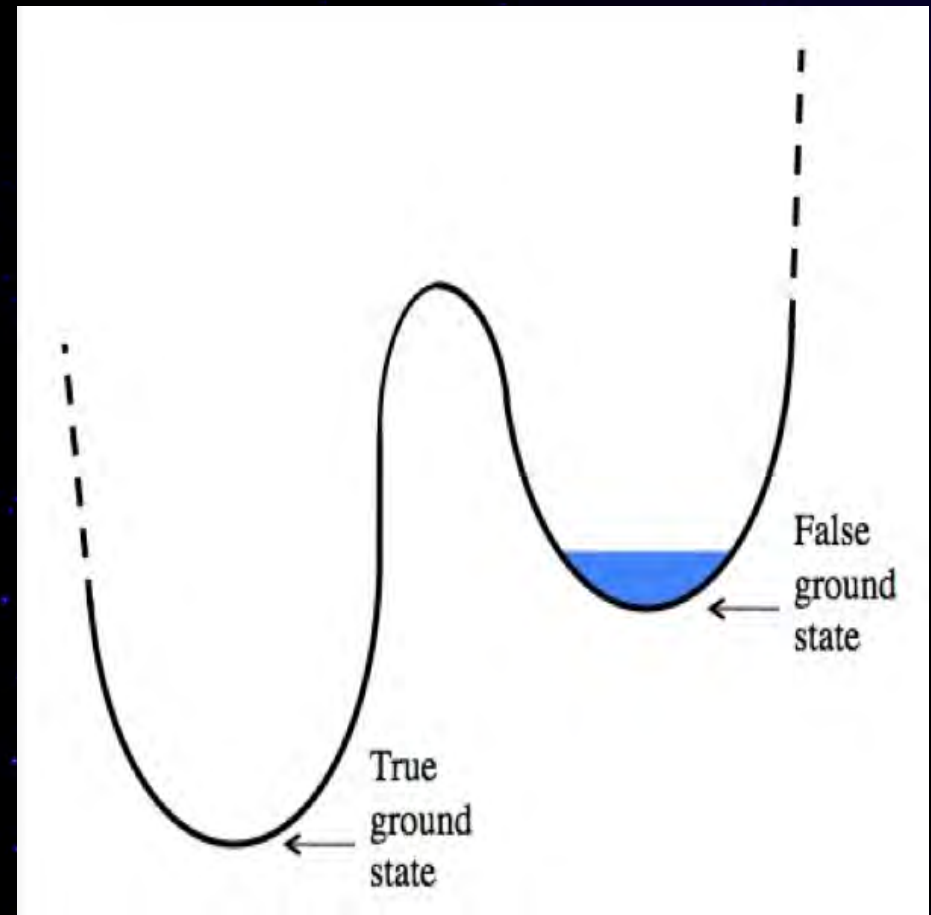
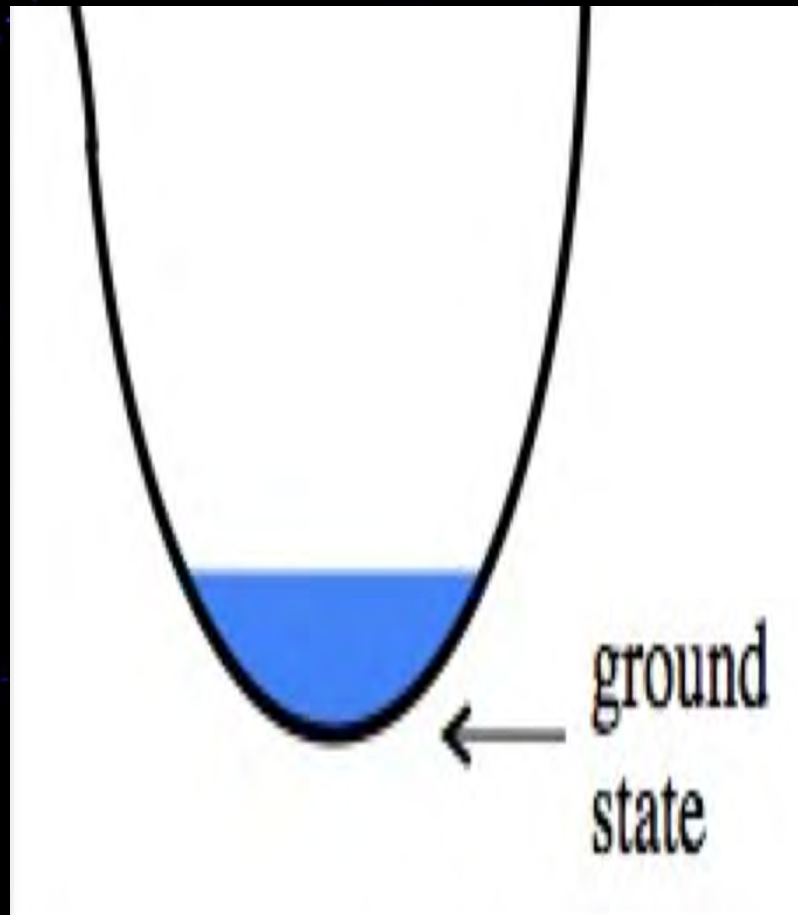


(c)

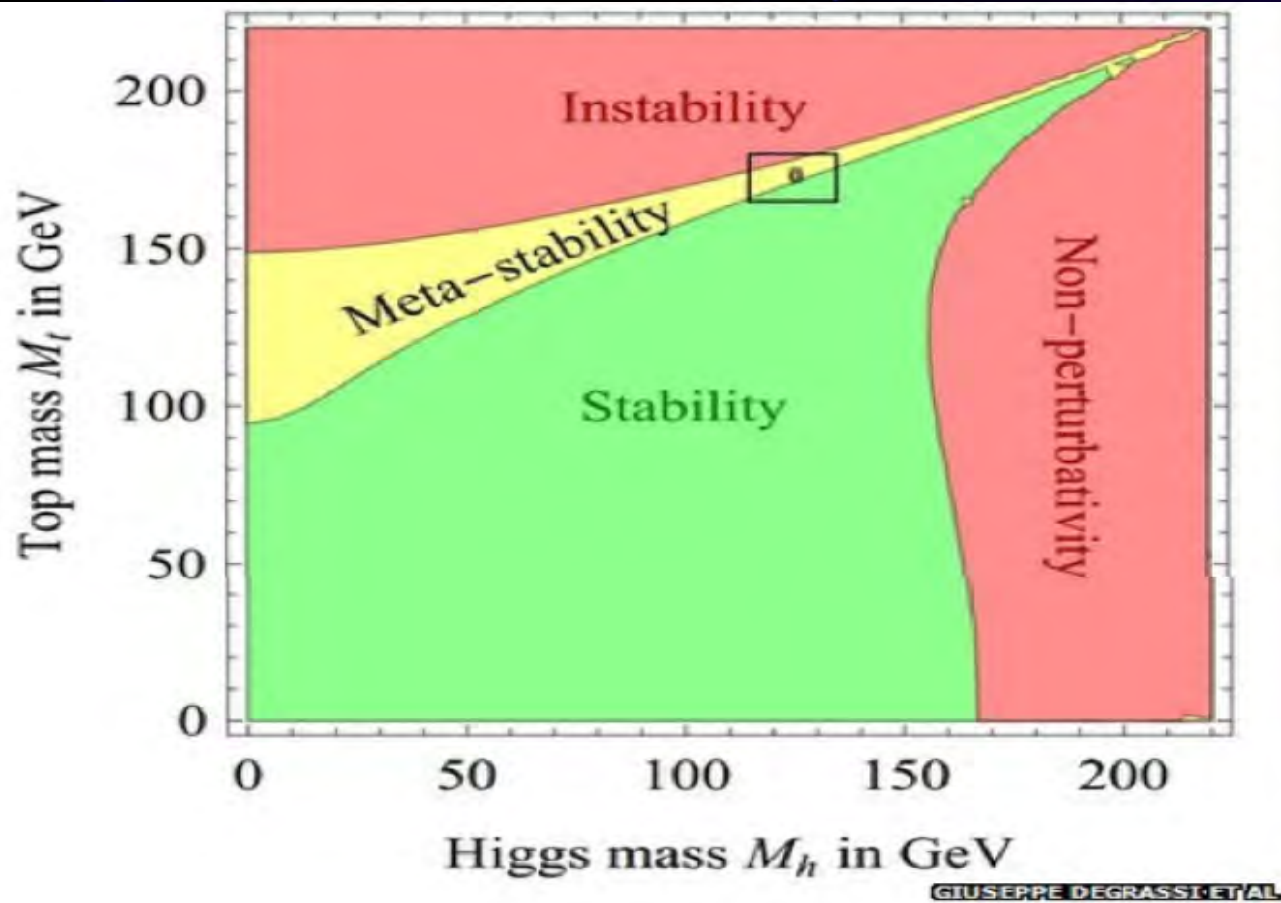


(d)



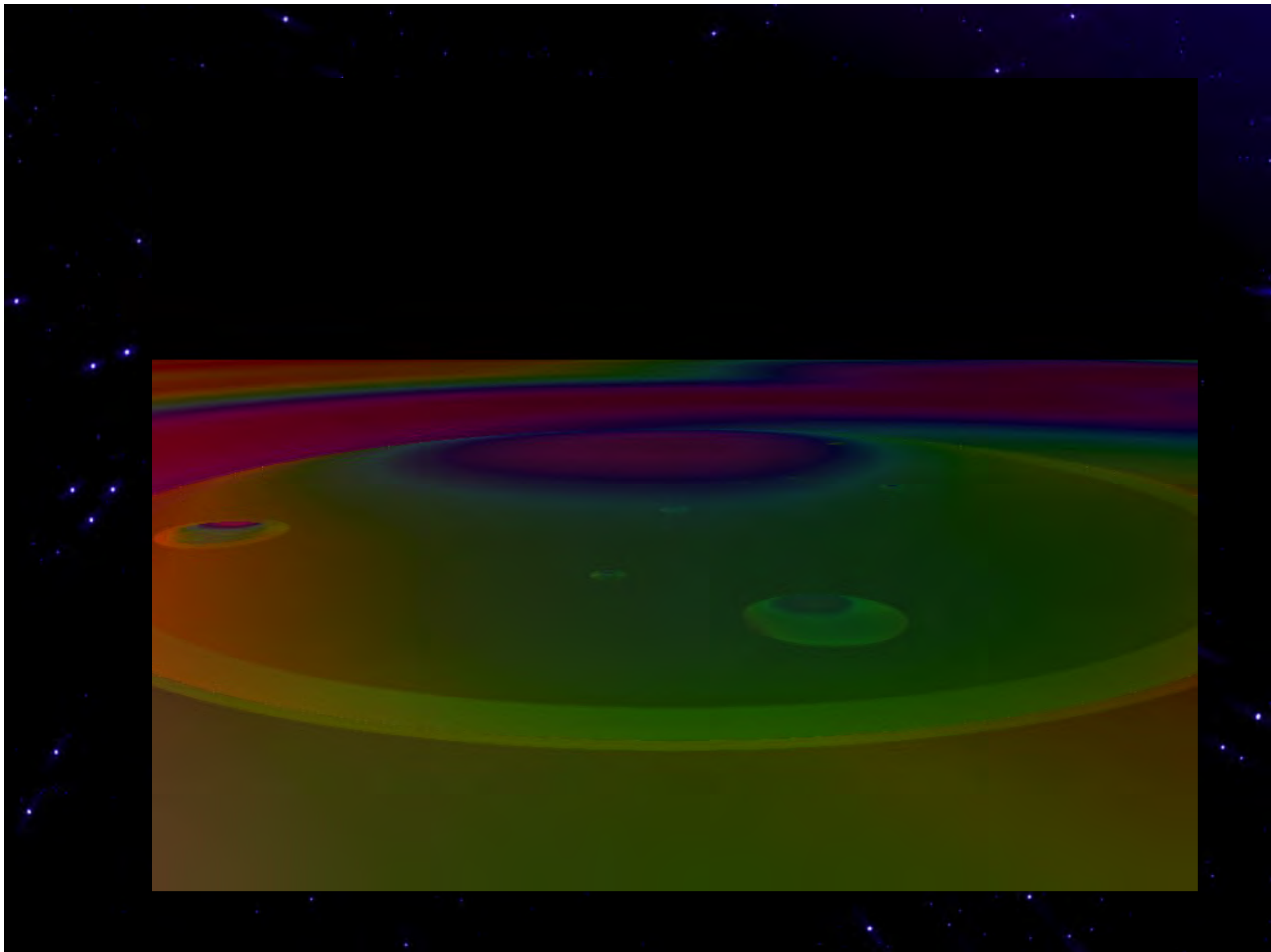


Ask a Mathematician / Ask a Physicist



Higgs mass and vacuum stability in the Standard Model at NNLO

Giuseppe Degrandi^a, Stefano Di Vita^a, Joan Elias-Miró^b, José R. Espinosa^{b,c},
Gian F. Giudice^d, Gino Isidori^{d,e}, Alessandro Strumia^{g,h}





SUSY & The Quantum Vacuum Energy

$$E_{vacuum} = \frac{1}{2} \sum_{\vec{p}, bosons} \sqrt{|\vec{p}|^2 + M_{boson}^2} - \frac{1}{2} \sum_{\vec{p}, fermions} \sqrt{|\vec{p}|^2 + M_{fermion}^2}$$

$$\sqrt{|\vec{p}|^2 + M^2} = |\vec{p}| \left[1 + \frac{1}{2} \frac{M^2}{|\vec{p}|^2} - \frac{1}{8} \frac{M^4}{|\vec{p}|^4} + \dots \right]$$

$$\sum_{bosons} M_{boson}^2 - \sum_{fermions} M_{fermion}^2 = 0$$

$$\sum_{bosons} M_{boson}^4 - \sum_{fermions} M_{fermion}^4 = 0$$



THANK

YOU

Acknowledgment

Prof. Gates also wishes to acknowledge
The Teaching Company for the use of
some CGI units that appear in

“Superstring Theory: The DNA of Reality.”

Animations: Copyright 2005 Kenneth A. Griggs.